

COMPUTER RECOGNITION OF THREE-DIMENSIONAL OBJECTS

IN A VISUAL SCENE

by

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I. C. E. Instituto Politécnico Nacional  
(ESIME) México, 1965

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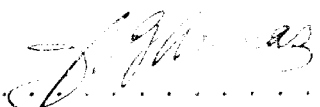
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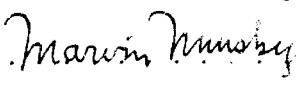
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December 1968

Signature of Author . . . . .  . . . . .  
Department of Electrical Engineering, Dec. 1968

Defended by . . . . .  . . . . .  
Thesis Supervisor

Accepted by . . . . .  
Chairman, Departmental Committee on Graduate Studies

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COMPUTER RECOGNITION OF THREE-DIMENSIONAL OBJECTS

IN A VISUAL SCENE

by

A d o l f o   G u z m á n - A r e n a s

Submitted to the Department of Electrical Engineering  
on December 30, 1968 in partial fulfillment of the  
requirements for the Degree of Doctor of Philosophy

A B S T R A C T

Methods are presented (1) to partition or decompose a visual scene into the bodies forming it; (2) to position these bodies in three-dimensional space, by combining two scenes that make a stereoscopic pair; (3) to find the regions or zones of a visual scene that belong to its background; (4) to carry out the isolation of objects in (1) when the input has inaccuracies. Running computer programs implement the methods, and many examples illustrate their behavior. The input is a two-dimensional line-drawing of the scene, assumed to contain three-dimensional bodies possessing flat faces (polyhedra); some of them may be partially occluded. Suggestions are made for extending the work to curved objects. Some comparisons are made with human visual perception.

The main conclusion is that it is possible to separate a picture or scene into the constituent objects exclusively on the basis of monocular geometric properties (on the basis of pure form); in fact, successful methods are shown.

Thesis Supervisor: Marvin L. Minsky.  
Title: Professor of Electrical Engineering.

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*Adolfo Guzmán*

To the reader: Comments, corrections and criticisms are encouraged, and should be sent to the author to the address below.

Project MAC, M. I. T.  
545 Technology Square  
Cambridge, Mass., USA., December 30, 1968.

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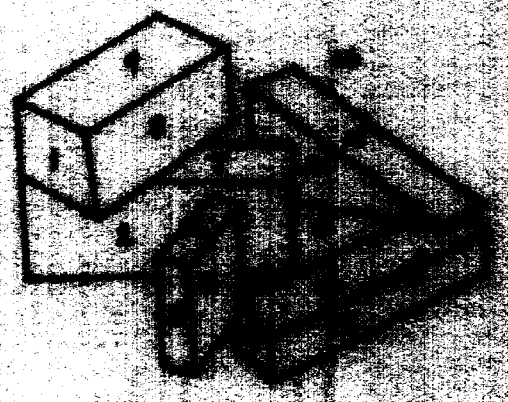
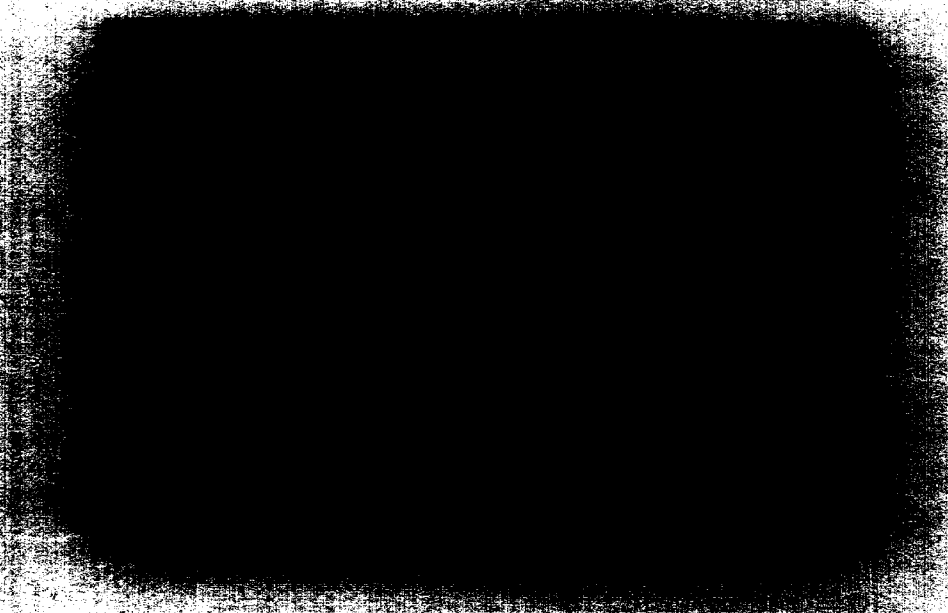
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SECRET

SECRET NO. 1111

This chart contains information of a confidential nature and its disclosure to unauthorized persons is prohibited. It is to be used only for the purposes stated herein.

III. REFERENCES



if the machine is asked to separate the bodies, it must say  
(BODIES ARE AS FOLLOWS : (1 8 9) (2 7) (3 5 6) (10 15)  
(4 13 14) )

If asked to report the triangular prisms, it should answer  
(10 15 IS A TRIANGULAR PRISM)

- This thesis discusses the problems involved in this task.  
What should be done when the information is noisy, some lines are missing, etc?  
How can the computer separate the background from the objects forming the scene?  
How should shadows be handled?  
How can stereoscopic vision be used?  
What about ambiguities and optical illusions?
- This thesis also discusses some related aspects of human visual perception
- Key words and phrases related to this study are as follows:

artificial intelligence	pattern matching
body	pattern recognition
background	photography
background discrimination	photo-interpretation
classification of images	picture
CONVERT	picture abstraction
cybernetics	picture processing
feature recognition	picture transformations
geometric objects	pictorial structures
geometric processing	polyhedra
graphic processing	recognition
graphical communication	robot
graphical data	scene
heuristic procedures	scene analysis
heuristic programming	solids
identification	stereoscopic
image	symbol manipulation
intelligence	three-dimensional
line drawing	three-dimensional scenes
LISP	three-dimensional solids
list processing	two-dimensional patterns
machine aided cognition	vision
machine perception	visual
mechanization of visual	visual information processing
perception	visual object recognition
object identification	visual perception
optical	visual scenes
optical illusion	
pattern	

== Computer Review (A. C. M.) index numbers: C.R. 3.61, 3.63, 4.22, 5.20.

Why this work was chosen as a thesis topic

The present work was carried out using the facilities of the Artificial Intelligence Group of Project MAC, at M. I. T. Currently, the main goal of the Artificial Intelligence Group (AI group) is «to extend the way computers can interact with the real world: specifically to develop better sensory and motor equipment, and programs to control them.» {Minsky, Status Report II}. From such efforts, a robot or mechanical manipulator has been constructed, consisting of a PDP-6 computer, an image dissector camera mechanical arm and hand (see pictures).

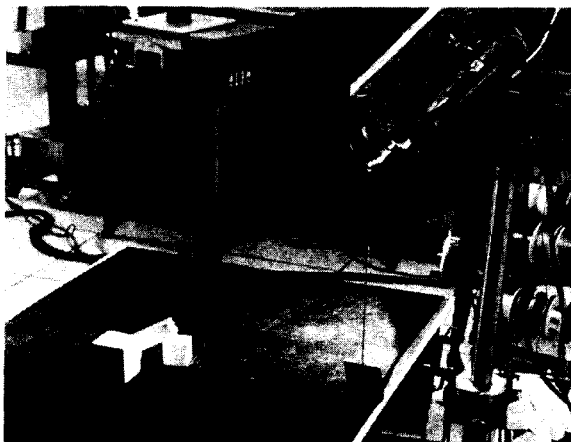
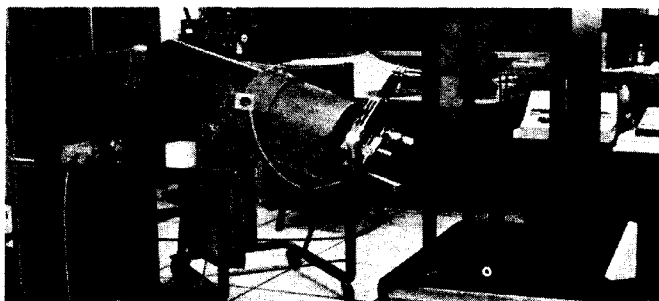


IMAGE DISSECTOR CAMERA

«These "eyes and hands" are eventually to be able to do reasonably intelligent things but first, of course, it is difficult enough to get them to do things that are easy for people to do.» {Ibid.}

An image dissector  
silently watches  
a triangular prism  
in the vision labo  
ratory of the A.I.  
Group.





The work was naturally divided into visual information processing (computer vision) and manipulation and control of the arm-hand. Thus, when I came as a graduate student from the Politécnico de México to M. I. T. (Sept. 65) and became associated with the AI Group, I found a great interest there in graphical communication with computers. Moreover, it was felt that symbol manipulation techniques would be relevant to this area. I was fortunate enough to have had some contact with the LISP language in some of its implementations: MB - LISP {McIntosh 1963} \* and Hawkinson-Yates- LISP {Hawkinson 64}\* at the Centro Nacional de Cálculo of the Politécnico; in fact, I became interested in the area because I felt that it would be possible to handle two-dimensional structures much in the same fashion as one handles lists (that is, one-dimensional structures or strings of symbols) in a pattern-driven language, such as CONVERT {1965}, recently finished at that time.

The area also offered a good opportunity to understand and evaluate several techniques, computers, equipment, etc. Consequently I decided to work in it.

---

(\*) The parentheses {            } always indicate a reference to the bibliography at the end of this thesis, where the complete title, date, etc., of the paper can be found.

## SIMPLIFIED VIEW OF SCENE ANALYSIS

TO THE BUSY READER

This section presents a general view of the problems in the thesis and their solutions; if you are short of time,

- (1) Read the abstract and this section.
- (2) Choose some scenes from section 'Analysis of many scenes', and observe how the computer perceives them.
- (3) Look through the table of contents, select additional topics.

Scene Analysis Scene analysis is the result of interaction between optical data coming from the Eye, and knowledge about the visual world stored in the programs. In all that follows, the optical data entering through the Eye is reduced to a line drawing; this pass is called pre-processing, and it will be only briefly sketched here.

After preprocessing, such a line drawing is analyzed in order to discover and recognize given objects in it. The process is called recognition.

This thesis is concerned with recognition.

We now give a simplified exposition of both processes. Recognition will be discussed abundantly in the remainder of this thesis, since it is the main topic; readers who wish for more information on pre-processing or other approaches should consult the references, for instance {my MS Thesis} and {A C Shaw FJCC 68}. See also page 60.

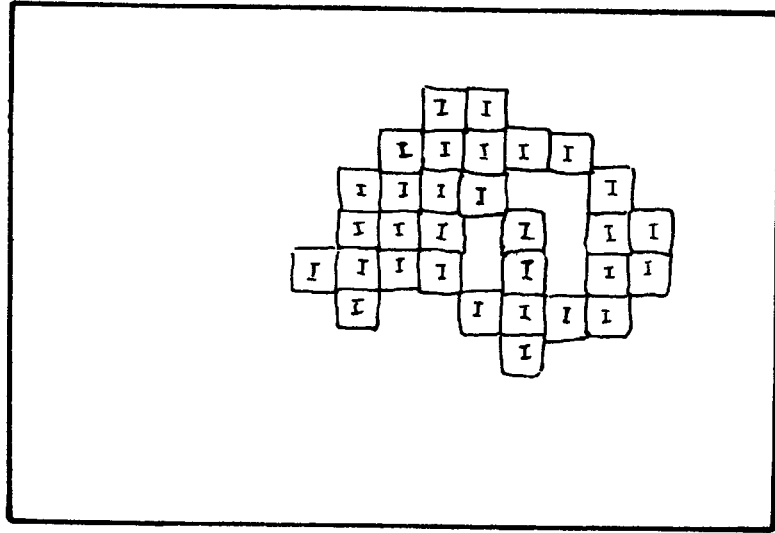
The stylized presentation that follows is only an example; in particular, scene analysis does not need to follow the sequence pre-processing → recognition. See 'Division of work in Computer Vision' in page 60.


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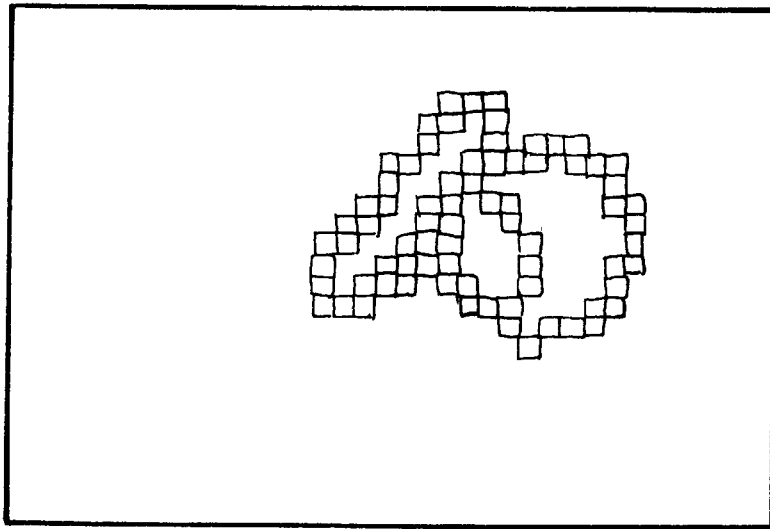
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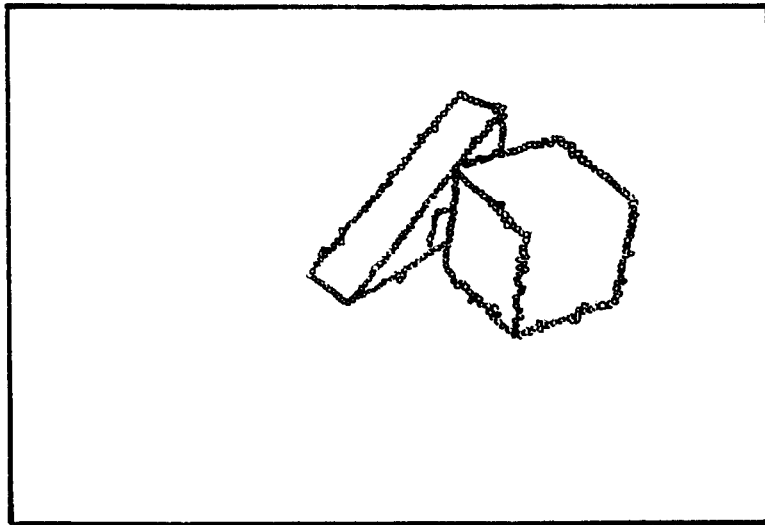
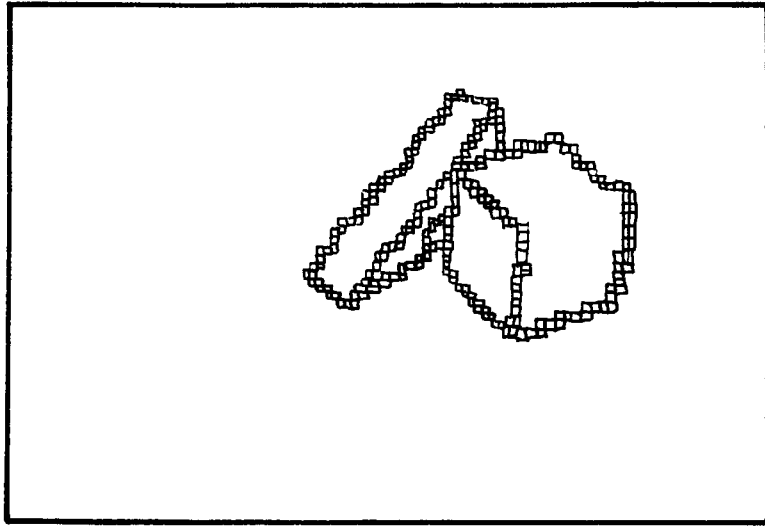
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Each inhomogeneous square **I** is divided in four , ignoring again the homogeneous sub-squares.

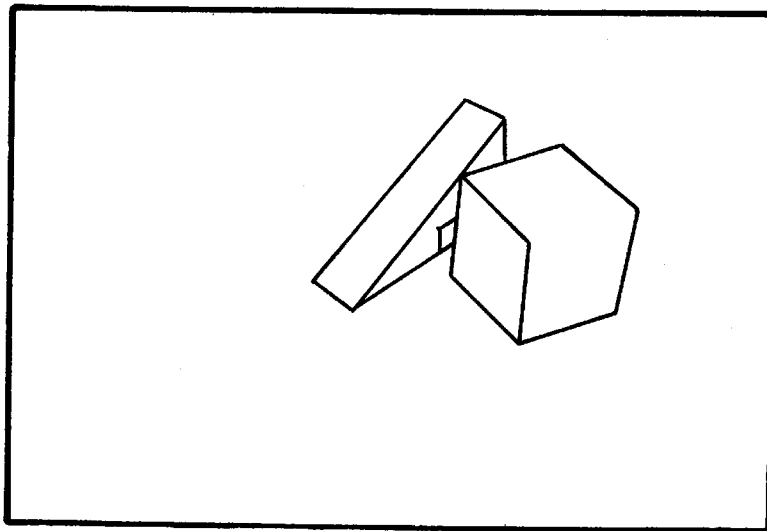


The process is repeated a few times more.



The squares are now reduced to lines and vertices.

The resulting analysis gives us the first chance to start working abstractly now, instead of continuing in "picture-point space." Preprocessing is finished.

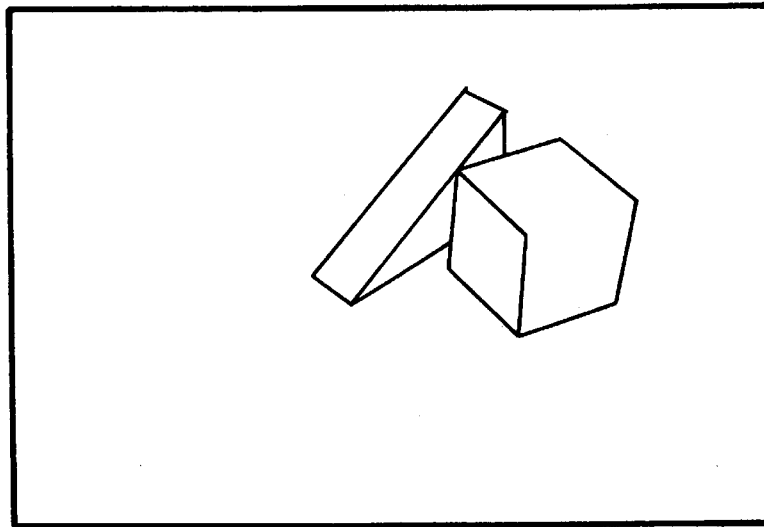


This and the next page describe proposed, but still unfinished, parts of the system.

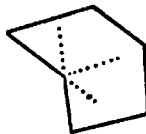
### Recognition

What follows is merely a brief summary of the processes in recognition. A more systematic presentation and classification of processes in recognition is found in 'Division of work in Computer Vision', on page 60.

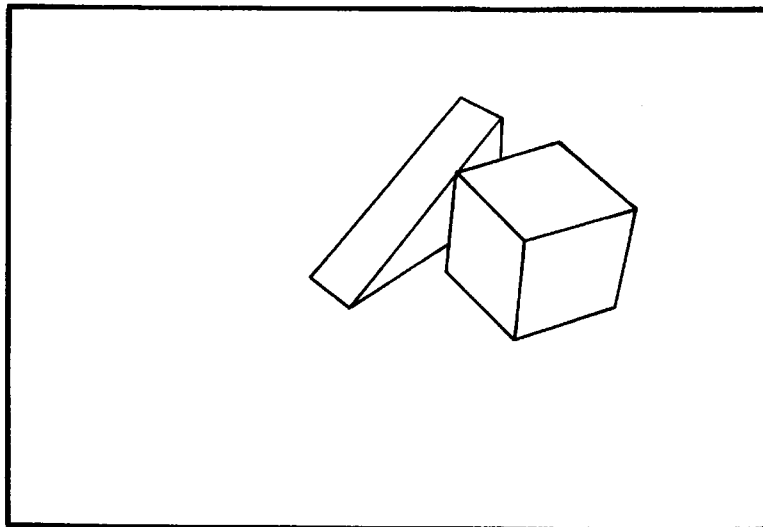
A program would check in the original scene, on both sides of each line, for continuation across the line, of textures, local cracks, etc. On these and other grounds, shadows would be picked up and erased:



A line-proposer program studies the abstract or "symbolic" scene and, using some heuristics and general principles, proposes places where it is quite probable that a line is missing:



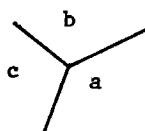
These places are searched by a line-verifying program, which is an specially sensitive test that uses fine measurements from the original scene, and often it will pick up a boundary that was missed in the less-intelligent homogeneity phase. Here it can be practical to apply a very strict and sensitive test, because the program knows very accurately where the line should be, if it really exists at all. For example, even if the two faces have almost equal illumination the Eye can pick up a thin, faint highlight from the edge of the cube. It would have been hopelessly expensive to look for such detailed phenomena over the whole picture at the start.



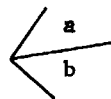
At this stage our program SEE (page 58) comes into action. This program treats different kinds of local configurations as providing different degrees of evidence for 'linking' the faces. This evidence is obtained mainly at vertices, and at boundaries between regions.

A vertex is in general a point of intersection of two or more boundaries of regions. These regions might or might not be faces of a single body. SEE examines the configuration of lines meeting at the vertex to obtain evidence relevant to whether the regions involved belong to some object.

For instance, in the vertex configurations "ARROW" and "FORK" (a complete classification of vertices can be found below in table 'VERTICES'),



"FORK"



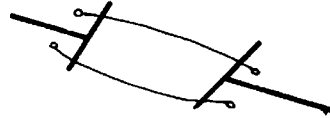
"ARROW"



the "FORK" suggests linking face a to face b, b to c, c to a. The "ARROW" links a with b. A "leg" (which depends on nearly parallel lines) would add a weak link, in addition to the ordinary

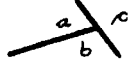


'LEG'  
(Weak link shown dotted)

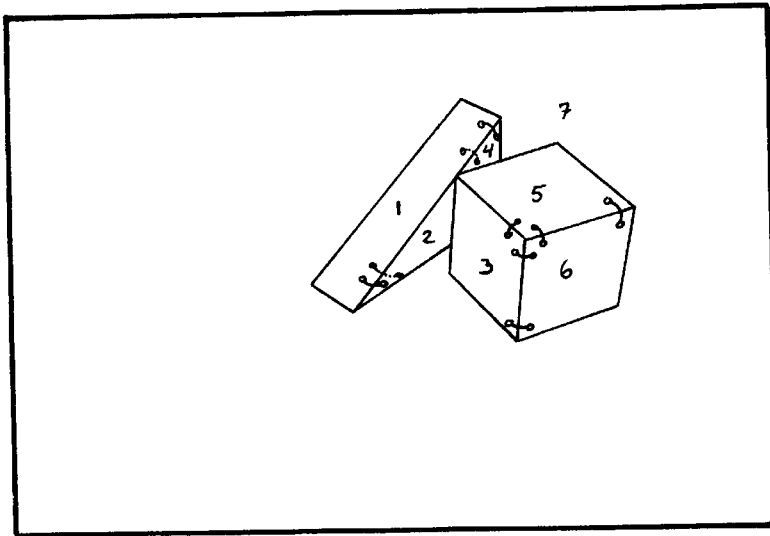


Matching T's.  
(two strong links)

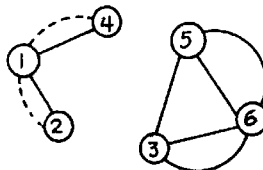
(or strong) link placed by its 'arrow'; a "T" looks for a matching "T", and if found, two strong links are placed as shown. Also, a "T" counts against (inhibiting, that is) linking a with c, or b with c.



These links, for our example, are



and may be represented as



[weak links are dotted]

indicating two groups of linked faces, that is, two bodies:

(BODY 1. IS 1 2 4)

(BODY 2. IS 3 5 6)

If in addition we give at this point to the computer the definition or concept of a 'triangular prism', through an abstract model of it {my MS Thesis}, we can get

(1 2 4 IS A TRIANGULAR-PRISM)

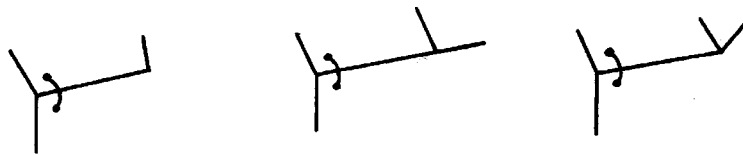
(3 5 6 IS A CUBE)

Recognition has finished.



#### Analysis of several examples

A larger variety of kinds of evidence is used in more complicated scenes, making the program more intelligent in its answers:

- (1) The links themselves are inhibited by conditions or configurations at the neighbor vertices and faces; for instance, in the case of a "FORK", the (strong) links indicated below are inhibited:

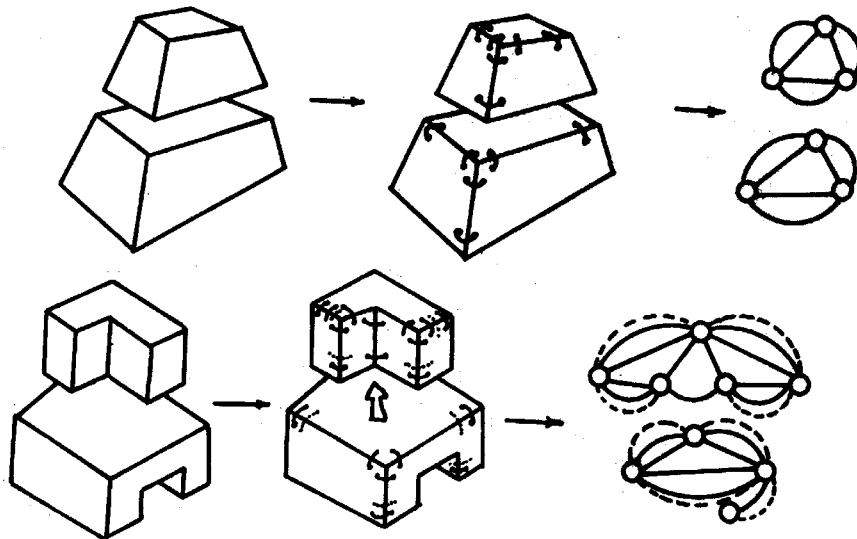


- (2) The links to the background are ignored [complete descriptions of conditions for producing and cancelling links are to be found in section 'SEE, a program that finds bodies in a scene'].
- (3) A hierarchical scheme is used that first finds subsets of faces that are very tightly linked (e. g., by two or more links).

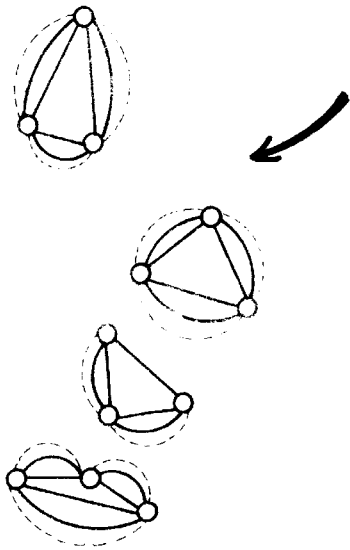
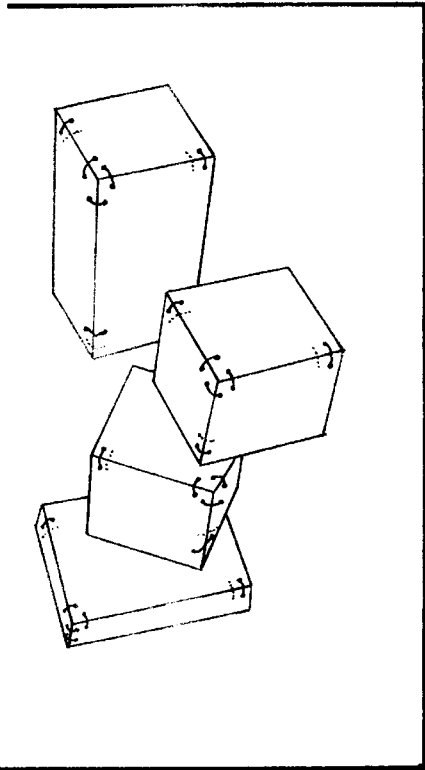
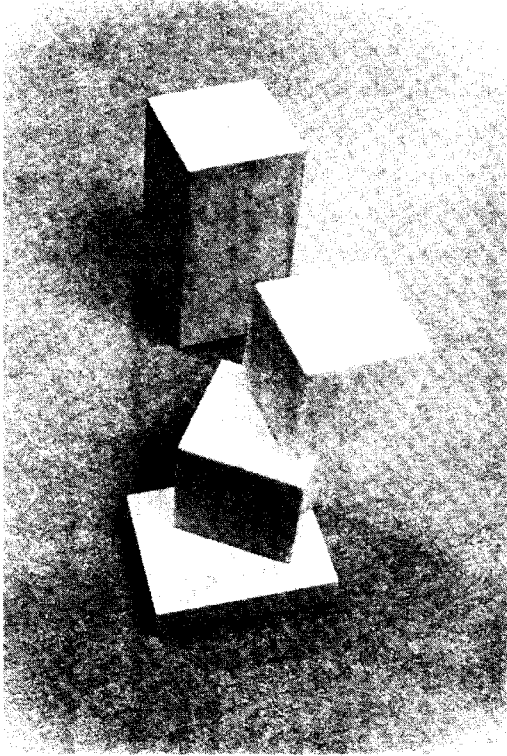
These "nuclei" then compete for more loosely linked faces (faces linked through one weak link and one strong link , or one face completely unlinked, except by one strong link ).

By not considering a single link, weak or strong, as enough evidence for assigning two faces as part of the same object, this algorithm requires two "mistakes" (that is, two careless placements of links between regions that should not be considered as forming the same body) to make an identification error.

The bodies of the following scenes are found by SEE without difficulty.

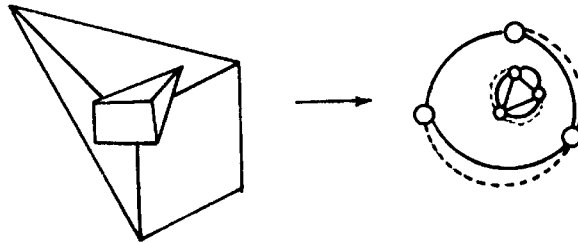


Note that of the strong links available to the "FORK" marked with an arrow, two were prohibited or inhibited and only one is produced by SEE.



Dotted links are weak.

In the following figure, the "FORK" of the big object is missing.



Statement of Rules We will re-state the rules under (3) of page 22 .

Region (definition). Surface bounded by simply closed curves.

We will consider the outer background (:16 in fig 'L10', page 59 )<sup>\*</sup> to be also a region.

Nucleus (definition). A nucleus (of a body) is a set of regions.

Linked nuclei (definition). Two nuclei A and B are linked if regions a and b are linked where  $a \in A$  and  $b \in B$ .

First rule: If two nuclei are linked by two or more strong links, they are merged into a larger nucleus.

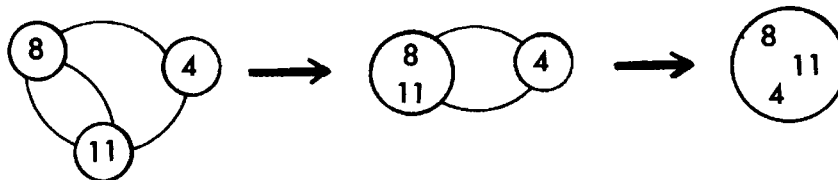
For instance, regions :8 and :11 are put together, because there



exist two strong links among them, to form the nucleus :8-11.

Maximal nuclei: Starting from nuclei containing individual regions, we let the nuclei grow and merge under the First rule, until no new nuclei can be formed. When this is the case, the scene has been partitioned into several "maximal" nuclei; between any two of these there is at most one strong link.

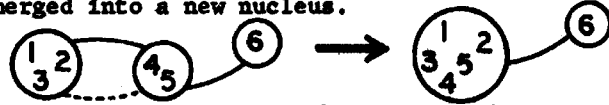
For instance, regions :8 and :11 are put together by the First rule; now we see that region :4 has two links with nucleus :8-11, and therefore the new nucleus :8-11-4 is formed. This last is a maximal nucleus.



<sup>\*</sup>For the moment, ignore the colons (:) in front of numbers. The name of a region is a number preceded by a colon, such as :16.

The First rule is applied again and again, until all nuclei are maximal nuclei; then the following rule is applied:

**Second Rule:** If nuclei A and B are joined by a strong and a weak link they are merged into a new nucleus.



The Third rule is applied after the Second rule.

**Third Rule:** If nucleus A consists of a single region, has one link with nucleus B and no links with any other nucleus, A and B are merged.

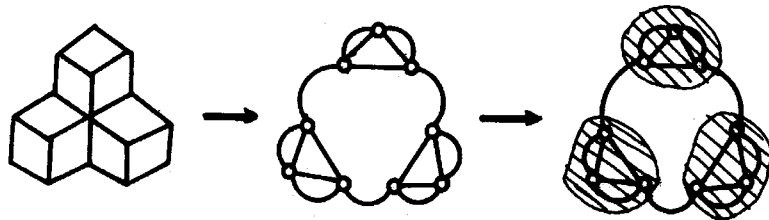


(10 11) does not join the bigger nucleus because (10 11) does not consist of a single region. Below, 9 does not join (7 8) or (4 5) because 9 has two links:



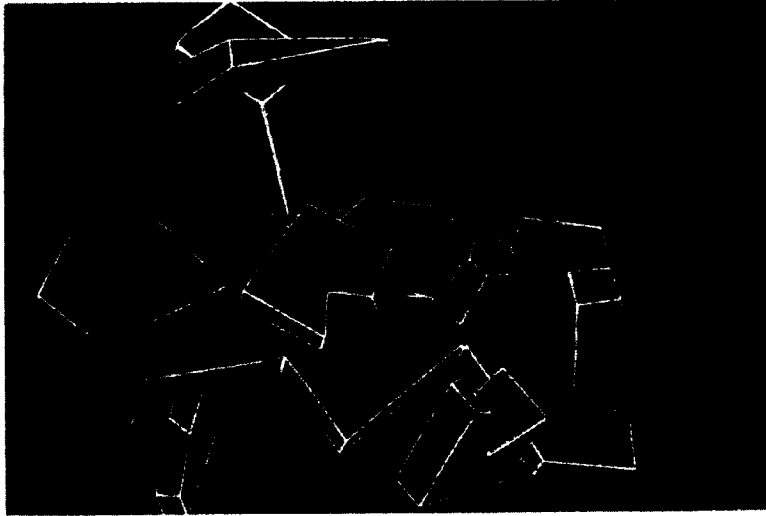
The Third rule tends to avoid proposing bodies consisting of a single region.

The next example shows how three "false" links failed to lead SEE into error:

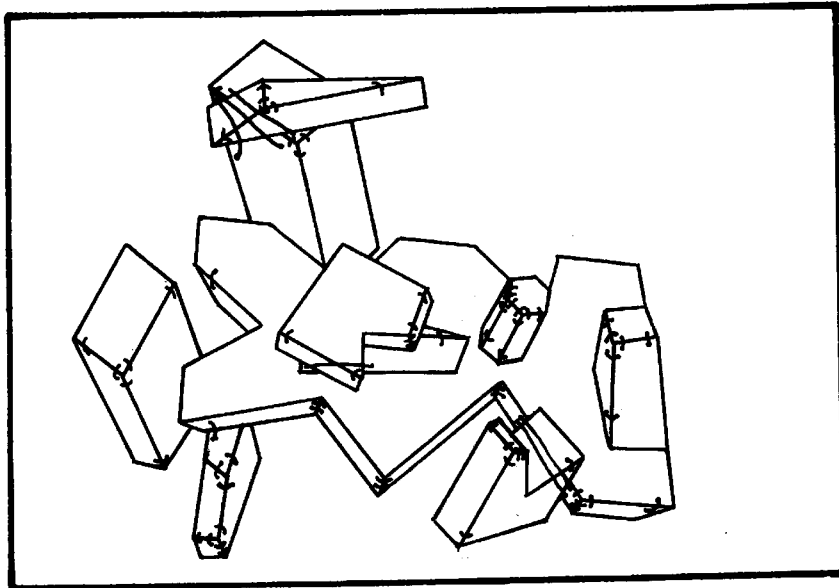


Here three links were erroneously placed but SEE did not get confused by them.

In complicated scenes, coincidences cause two objects to line up. As a result, vertices of different objects are merged, two objectively different lines appear as one and so on. The next example illustrates these phenomena and shows how SEE copes with the problem.



SEE transforms the above scene as follows:





As we see, the nuclei are going to be correctly formed, and SEE will also analyze this scene correctly.

The bodies do not need to be rectangular, prismatic, convex. They only need to be rectilinear. As we will see later, even curved objects may be identified, under certain restrictions (cf. Table 'ASSUMPTIONS').

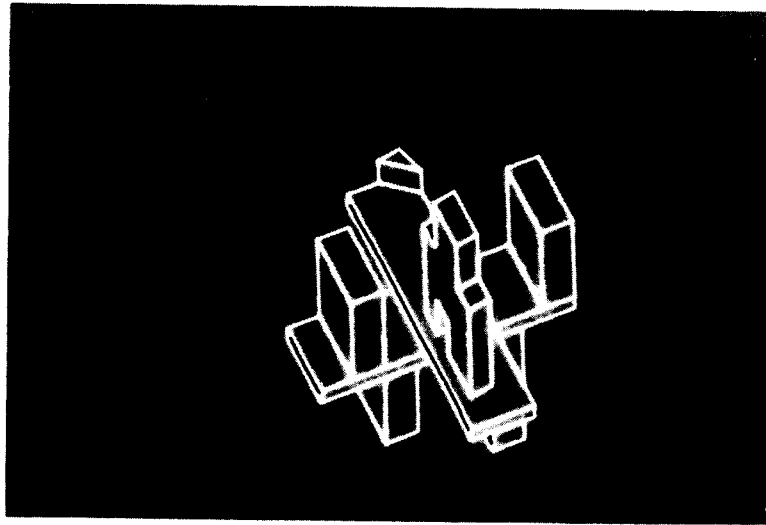


Figure 'BRIDGE'

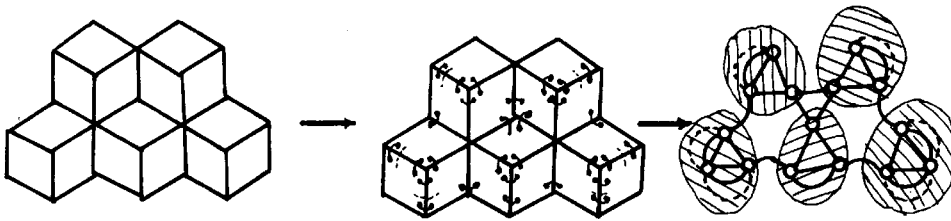


All the bodies in "BRIDGE" are adequately found. A new heuristic is used here:



three parallel lines comprising regions that are not background, and having the background as a neighbor, and a 'T' in the center line, originate a strong link, as shown above.

The following locally ambiguous scene is correctly parsed by our program:



If we add another block to the right, the program makes a mistake and fails to see one of the inner cubes:

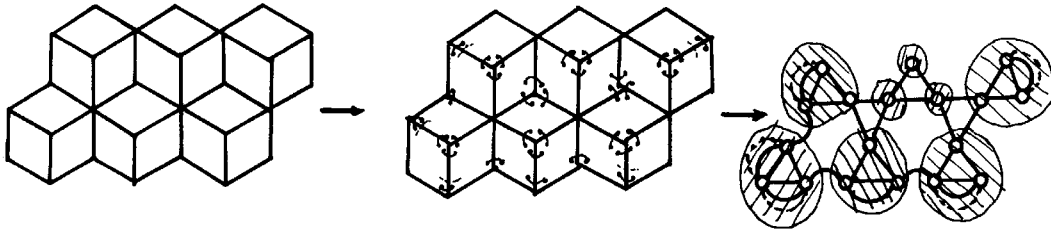


Figure 'MOMO' also gets decomposed accurately:

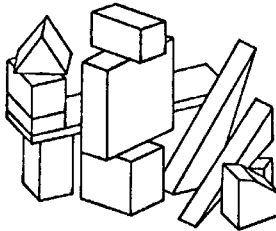
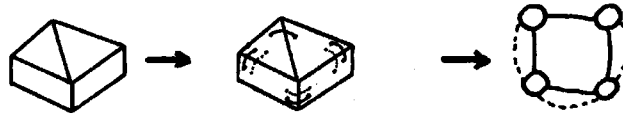
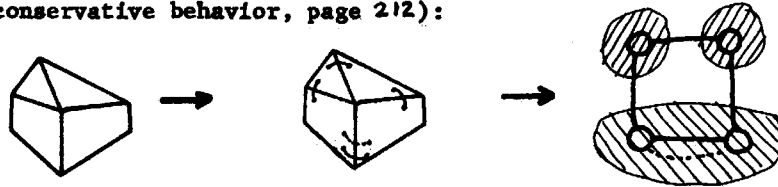


Figure 'MOMO'

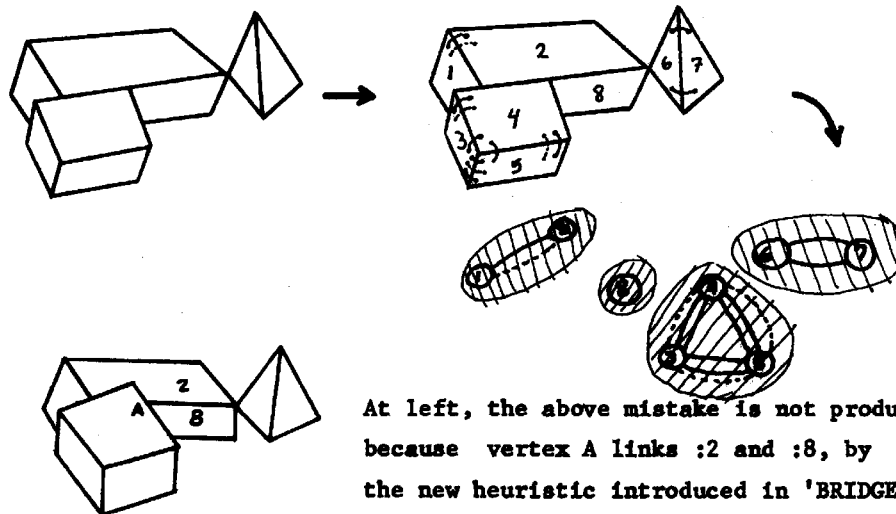
The local links allow correct identification of the following body:



If the lateral faces do not have parallel edges, a mistake occurs (conservative behavior, page 212):



Another mistake occurs in the following scene:



At left, the above mistake is not produced because vertex A links :2 and :8, by the new heuristic introduced in 'BRIDGE'.

### Conclusion

The performance of this program shows that it is possible to separate a scene into the objects forming it, without needing to know the objects in detail; SEE does not need to know the 'definitions' or descriptions of a pyramid, or a pentagonal prism, in order to isolate these objects in a scene containing them, even in the case where they are partially occluded.

The program will be fully analyzed in the following pages.

Problems in analyzing a visual scene \*

The problem of taking a two-dimensional image (or several such images), and constructing from it a three-dimensional interpretation, involves many operations that have never been studied, to say nothing of being realized on a computer. We will list some of these here; a more complete list is found in my M.S. Thesis {MAC TR 37}; some have been side-stepped or ignored by the present recognition system; the problems which we did solve are discussed in the text.

Among the facilities that must be available are:

- a) Spatial frame-of-reference: setting up a model of the relation between the eye(s) and the general framework of the physical task, i. e., where are the background, the "table" or working surface, and the mechanical hand(s)?
- b) Finding visual objects, and localizing them in space with respect to the eye-table-background-hand model.
- c) Recognizing or describing the objects seen, regardless of their position, accounting for partly-hidden objects, recognizing objects already "known" by descriptions in memory and representing the three-dimensional form of new objects.
- d) Building an internal "structural model" of what has been seen, for the purpose of task-goal analysis.

Among the important factors are the effects of:

1. Both the camera's focus and its depth-of-focus.
2. Illumination of the objects. Light affects the appearance of objects in obvious and subtle ways -- in scenes with multiple objects and lights we get complicated shadows, which have to be detected or rejected. The boundary between two faces may disappear if they get equal illumination from a diffuse light source.
3. Perspective and distance effects. Even for geometric objects with flat surfaces, the two-dimensional projection of their surface

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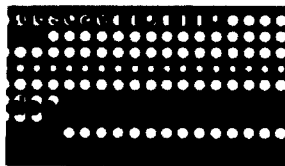
\* Adapted from Status Report II {Minsky 67}. See also Project MAC Progress Report {1967, 1968}.

features can take many forms, and the system has to be able to deal with all of them. It works both ways, of course: once identified, the appearance can give valuable information about the object's orientation, size, and even (under some conditions) its absolute spatial locations [Roberts 1963].

4. Accidental vs. essential visual features. Two objects of the same shape and location can have very different visual presentations because of their surface textures and markings. We need to distinguish these two-dimensional "decorations" from real three-dimensional spatial features.

#### Other projects

Here are the main robot groups at a panel discussion.



Chairman:  
**DR. BERTRAM RAPHAEL**  
*Stanford Research Institute  
Menlo Park, California*

### problems in the implementation of intelligent robots

This session, the second of three sessions on robotics, will consist of a panel discussion among technical people involved in the design and construction of mechanical devices that are capable of significant independent "intelligent" behavior, usually by means of computer control. The projects represented on this panel have drawn upon state-of-the-art capabilities in many technologies including mechanical engineering, pattern recognition, heuristic programming, neural networks and computer systems. Thus, the discussion which will be conducted at a fairly technical level should be of interest to engineers and scientists concerned with the problems of interfacing a variety of disciplines, as well as to those interested in learning about the nature of current embryonic "robot" systems.

NOTE: Tickets priced at \$5.00 each (including lunch) for the all-day tour of "live robot" installations on Wednesday, Dec. 11th, will be available at this session.

Panel Members

**MR. L. CHAITIN**

*Artificial Intelligence Group  
Stanford Research Institute*

**ROBOT STUDIES AT STANFORD RESEARCH INSTITUTE**

**PROF. J. A. FELDMAN**

*Computer Science Department  
Stanford University*

**THE ROBOT PROJECT  
AT STANFORD UNIVERSITY**

**DR. T. SHERIDAN**

*Dept. of Mechanical Engineering  
MIT*

**HUMAN CONTROL OF REMOTE COMPUTER  
MANIPULATORS**

**MR. R. J. LEE**

*Air Force Avionics Lab.  
Wright-Patterson AFB*

**GENERAL PURPOSE MAN-LIKE ROBOTS**

**PROF. S. PAPER**

*Artificial Intelligence Project  
MIT, Project MAC*

**THE MIT HAND-EYE PROJECT**

**MR. L. SUTRO**

*Dept. Aeronautics and Astronautics  
MIT*

**ROBOT DEVELOPMENT AT THE  
MIT INSTRUMENTATION LABORATORY**

**1968  
fall joint  
computer  
conference**

**DECEMBER 9-10-11  
san francisco  
civic center**

## RELATED RESEARCH

### Previous work by the author

#### CONVERT

A programming language is described which is applicable to problems conveniently described by transformation rules. By this is meant that patterns may be prescribed, each being associated with a skeleton, so that a series of such pairs may be searched until a pattern is found which matches an expression to be transformed. The conditions for a match are governed by a code which also allows subexpressions to be identified and eventually substituted into the corresponding skeleton. The primitive patterns and primitive skeletons are described, as well as the principles which allow their elaboration into more complicated patterns and skeletons. The advantages of the language are that it allows one to apply transformation rules to lists and arrays as easily as strings, that both patterns and skeletons may be defined recursively, and that as a consequence programs may be stated quite concisely.

Abstract of Convert paper in Comm. A.C.M.

Because it is easy to write and modify a program in Convert, the language has been extensively used to quickly test 'good' and "great" ideas, new algorithms, etc. It is embedded in the LISP of the PDP-6 computer (A.I. Group), in the IBM-7094 (Project MAC-MIT); in the CDC-3600 (Uppsala University, Sweden), in the SDS-940 (Univ. of California, Berkeley). A paper in the A. C. M. and {MAC M 305} describe the language; examples of simple programs written in Convert are in {MAC M 346}; a book article {Patterns and Skeletons in Convert} is oriented toward the Lisp consumers. For our Spanish readers, two Bachelor's Theses {Guzmán 1965} {Segovia 1967} describe the language and processors, and give examples.

#### SCENE ANALYSIS

(1) Polybrick {MAC M 308} {Hawaii 69} is a Convert program that works on a scene or picture, expressed as a line drawing, and finds parallelepipeds in it.

(2) We would like to be able to specify in some suitable notation models of the classes of objects we are interested in (such as 'cube', 'triangular prism', 'chair'), and make a program look for all instances of any given model in a given scene or figure. Two arguments would have to be supplied to our program: the model of the object we are interested in, and the scene that we want to analyze. Programs to do this are described in {AFCRL-67-0133} and {MAC M 342}. In these early programs, partially occluded objects get incorrectly identified. These programs are also written in Convert, and work by transforming or compiling the model, written in a picture description language, into a Convert pattern, which searches the scene for instances of the model.

(3) A Master's Thesis {MAC TR 37} discusses many ways to identify objects of known forms. Different kinds of models and their properties are analyzed.

(4) It is important to be able to find the bodies that form a scene, without knowing their exact description or model. SEE is a program that works on a scene presumably composed of three-dimensional rectilinear objects, and analyzes the scene into a composition of three-dimensional objects. Partially occluded objects are usually properly handled. This program was discussed in {MAC M 357}, {Guzmán FJCC 68} and {Pisa 68}, and this thesis discusses a later version.

(5) The present thesis goes beyond these topics to discuss also handling of stereo information (two views, left and right, of the same scene), improvements to deal with noisy (imperfect) input, figure-background discrimination, and a few other subjects.

#### Canaday

Rudd H. Canaday in 1962 analysed scenes composed of two-dimensional overlapping objects, "straight-sided pieces of cardboard." His program breaks the image into its component parts (the pieces of cardboard), describes each one, gives the depth of each part in the image (or scene), and states which parts cover which.

## Roberts

The problem of machine recognition of pictorial data has long been a challenging goal, but has seldom been attempted with anything more complex than alphabetic characters. Many people have felt that research on character recognition would be a first step, leading the way to a more general pattern recognition system. However, the multitudinous attempts at character recognition, including my own, have not led very far. The reason, I feel, is that the study of abstract, two-dimensional forms leads us away from, not toward, the techniques necessary for the recognition of three-dimensional objects. The perception of solid objects is a process which can be based on the properties of three-dimensional transformations and the laws of nature. By carefully utilizing these properties, a procedure has been developed which not only identifies objects, but also determines their orientation and position in space.

Three main processes have been developed and programed in this report. The input process produces a line drawing from a photograph. Then the three-dimensional construction program produces a three-dimensional object list from the line drawing. When this is completed, the three-dimensional display program can produce a two-dimensional projection of the objects from any point of view. Of these processes, the input program is the most restrictive, whereas the two-dimensional to three-dimensional and three-dimensional to two-dimensional programs are capable of handling almost any array of planar-surfaced objects. {from Roberts }

Roberts in 1963 described programs that (1) convert a picture (a scene) into a line drawing and (2) produce a three-dimensional description of the objects shown in the drawing in terms of models and their transformations. The main restriction on the lines is that they should be a perspective projection of the surface boundaries of a set of three-dimensional objects with planar surfaces. He relies on perspective and numerical computations, while SEE uses a heuristic and symbolic (i.e., non-numerical ) approach. Also, SEE does not need models to isolate bodies. Roberts' work is probably the most important and closest to ours.

## Mechanical Manipulator Groups

(see also page 32 ).

Actually, several research groups (at Massachusetts Institute of Technology, <sup>10</sup> at Stanford University, <sup>11</sup> at Stanford Research Institute <sup>12</sup>) work actively towards the realization of a mechanical manipulator, i.e., an intelligent automata who could visually perceive and successfully interact with its environment, under the control of a computer. Naturally, the mechanization of visual perception forms part of their research, and important work begins to emerge from them in this area.

## THE CONCEPT OF A BODY

In this section definitions of a body or object will be proposed.

The criterion is that they agree in general with the common use of the word 'body', while at the same time they should lead themselves to implementation into a computer program.

### Introduction

Our ultimate interest is to examine a two-dimensional scene (a picture, line drawing, or painting), presumably a representation (projection, photograph) of a three-dimensional scene (a subset of the "universe" or "real world") and to find in it objects or bodies contained in the real scene. More specifically, the aim is to find the two-dimensional representations (projections, photographs) of the different three-dimensional bodies present in the scene.

The phrase "two-dimensional representation of a three-dimensional body" will be shortened to "two-dimensional body" or even to "body", when no confusion arises.

That is, we have to analyze a two-dimensional scene into collections of two-dimensional entities (surfaces, regions, lines), each of which makes "three-dimensional sense" as a two-dimensional projection of a three-dimensional body.

### The problem is inherently ambiguous

A scene can be considered as a set of surfaces (faces or regions), a body belonging to that scene is then an "appropriate" subset of this collection. Therefore, the problem of finding bodies in a scene is equivalent to the problem of partitioning the set into appropriate subsets, each one of them representing or forming a body (scene "CHURCH").

The problem is inherently ambiguous, since different collections of three-dimensional bodies can produce the same 2-dim scene, therefore a given scene can be partitioned in many ways into bodies.



It is desired to make a "natural" partition or decomposition of the scene, natural in the sense that will agree with human opinion.\*

To define a three-dimensional body is no problem [a philosopher may disagree, perhaps in singular cases]:

Three-dimensional body (definition):

A connected volume limited by a continuous, two-sided surface composed of portions of planes.

Restriction: The above definition covers only polyhedral bodies, that is, those having flat faces.

Restriction: No holes.

No-restriction: Bodies do not need to be convex.

Roughly speaking, a three-dimensional body is something that does not fall apart into pieces when lifted [this may be used as an operational definition of a body, given a mechanical manipulator to make the necessary tests].

Given a three-dimensional body, we generate a two-dimensional body by taking a picture of it, as follows.

Two-dimensional body (definition). Figure formed by the projection of a three-dimensional body. Generally, the projection is isometric or perspective.

Thus, this is a view in two dimensions of a solid body, from some particular point of view.

Unfortunately, a two-dimensional body could come in this way from any of several different 3-dim bodies or, what is worse, two 3-dim bodies together can give rise to a single 2-dim body. For instance, in fig. "BENT",

\*Without such a requirement, the problem has a trivial solution (see Metatheorem in page 39).

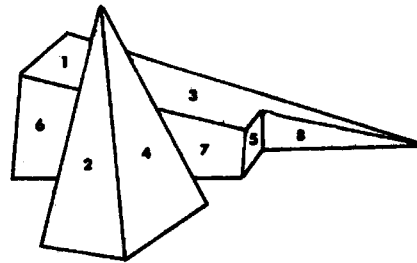


Figure 'CHURCH'

Set of eight elements. Adequate subsets (bodies) are [2 4], [1 3 5 6 7 8]. In a more complicated example, people may differ in their parsing of scenes.

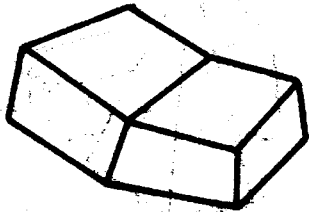


Figure 'B R N T'  
Two blocks, or a bent brick.

this two-dimensional body could be generated by a "bent brick" or by two blocks adjacent to each other. We are dealing with one three-dimensional body in the first case, with two in the second. But the 2-dim entity (namely, the drawing of figure 'BENT') is the same, and we are confronted with an inherent ambiguity.

Sibelius' Monument A more striking example is given in Fig. 'SIBELIUS', which could be the representation of 365 cylindrical bodies, or the picture of a sculpture (one body) in Helsinki.

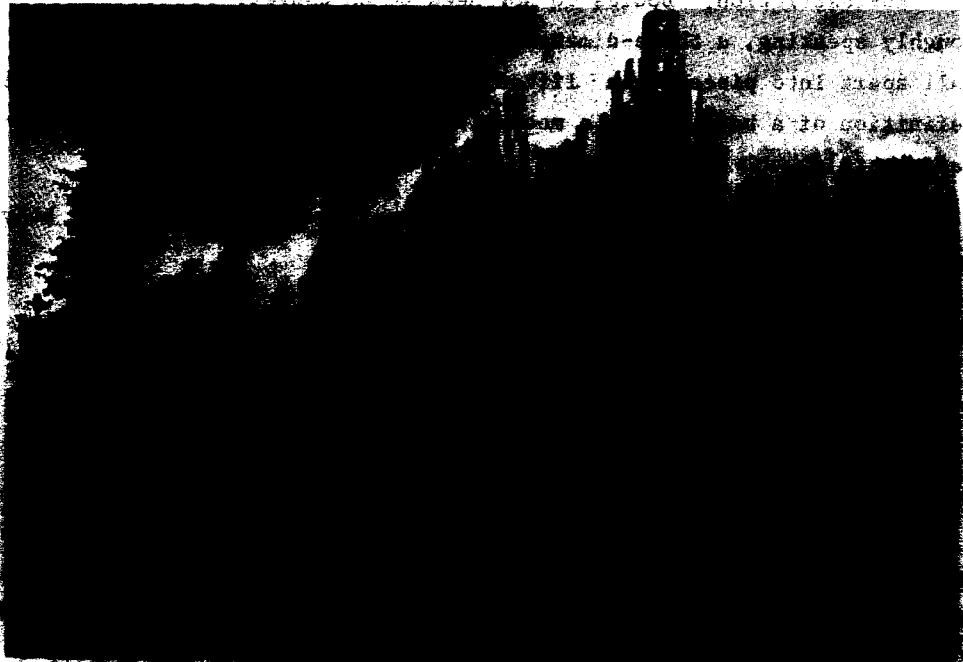


Figure 'SIBELIUS'

Such colorful contradictions point towards the need to lay down a more careful definition of our task. For instance, no one would think that figure 'CUBE'

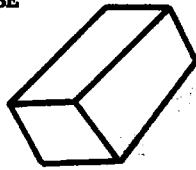


Fig. 'C U B E'  
No one would think...

contains three bodies. Nevertheless (see fig. 'PARALLELEPIPED' in next page), that could be the case.

These two extremes are to be avoided by an appropriate definition of a body and the corresponding computer program.

Legal scene That 2-dim scene in which each line is boundary of some region.



Legal scene.




Illegal.



Illegal.

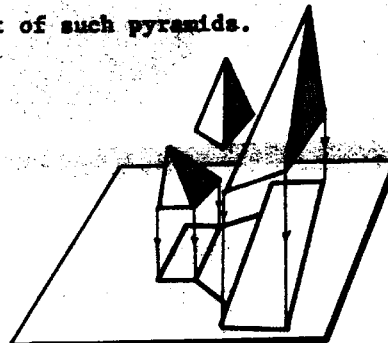
See also comments to scene R3, and 'Illegal Scenes' (page 217), in section 'On noisy input'.

Metatheorem "Any legal scene can always be the projection of one or more three-dimensional objects."

To prove it, it suffices to note that each legal scene is composed of regions , and each of them could be interpreted as the basis of a pyramid, all the faces meeting at the cuspid occluded by the basis.



Therefore, each legal scene can be obtained by projecting or photographing an adequate arrangement of such pyramids.



We can always construct a legal scene by photographing (or projecting) suitable 3-dim polyhedra.

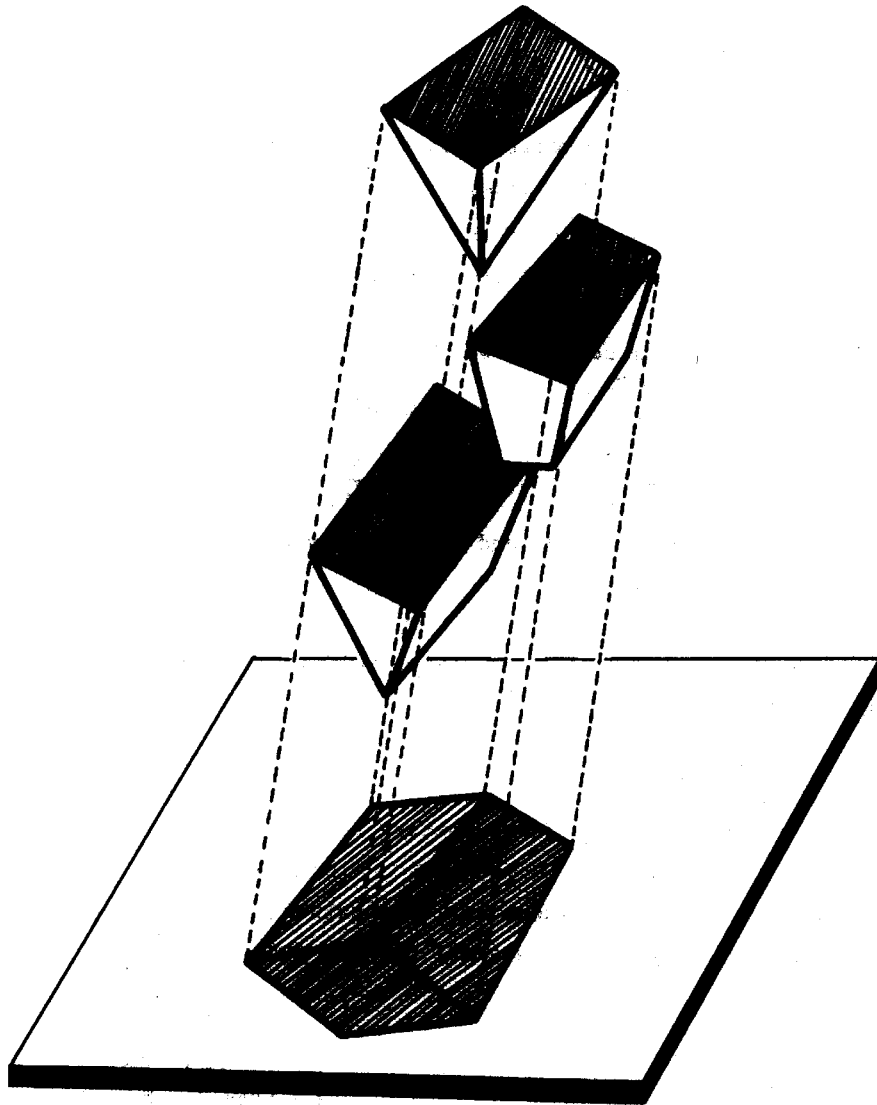


Figure 'PARALLELEPIPED'  
An improbable decomposition of a scene.

Trivial partition <sup>the</sup> By use of the metatheorem, we can always find a decomposition of a visual scene into three-dimensional bodies; we call this answer "trivial". Humans do not split scenes this way. Our program should not, either.

But the metatheorem points out that "impossible scenes" are never found among the legal scenes (see section 'On Optical Illusions'); these always have at least one interpretation. [end of "trivial partition"].

We are trying to give criteria for proposing bodies that will suit our ends, which are to define a "reasonable" or "standard" body. This will permit us to judge the performance of a program designed to find objects in a scene.

Several criteria are possible:

1. Roberts {1963} suggests: given several models of three-dimensional bodies, use some numerical techniques, such as least squares fitting, to find which model fits best through a suitable transformation, and accept this match if the error is tolerably small. Complicated compositions of elementary bodies are considered.
2. Ledley {1962} would propose: in terms of suitable primitive components (arcs, legs, etc.), make a syntactical analysis of the scene, with the help of a grammar, in such a way that the models of the object you want to identify are formed recursively from these primitive components and (perhaps) other bodies. Narasimhan {1962} and Kirsch {1964} would agree on this linguistical approach. A. C. Shaw {Ph. D. Thesis} assents.
3. Guzman {1967} suggests: prepare models which specify a fixed topology but where other relations (length of sides, parallelism of two lines, equality of angles) are specified through the use of open variables (UAR variables, in CONVERT). Evans {1968} would agree with that.

These approaches require the existence of a model which describes the object to be identified; the model specifies a particular 3-dim object (or a class of them). These approaches are answering more than what

was asked; they tell not only "yes, it is a body", but also "it is a pyramid". The current question is more general. It is desired to know if something is a body, any body, even one which has not been seen before.

If it were possible to implement a program to answer that question, then that would be a working definition of a body. SEE is a program which comes close to this goal, so that it could be pragmatically stated:

2-dim body "a la SEE" (definition). A body is each set of regions recognized by the program SEE as such.

This definition allows the following

Criticism: A perfect way to hunt lions is to capture any entity E, and to call that a lion, by definition.

That is, although this definition is precise, SEE may make decisions "contrary to common sense"; also, for purposes of judging the behavior of the program, this definition is useless, since SEE will be perfect 100 per cent of the time, irrespective of its answers.

We are, finally, tempted to conclude that 'common sense', or better, "human common sense" plays a role in the definition of a body, since what we are trying to characterize is a usual body, normal body, common body, etc. But even people may differ in their parsings of scenes. We could, of course, give a scene (such as 'MOMO' in page 77) to 100 subjects, ask them to identify the different bodies in it, and come up with some sort of 'average' or 'general consensus':

2-dim body (statistical and human-behavioral definition). Each one of the subsets into which a scene is partitioned by many subjects. It is understood that, in this spirit, the human objects should be motivated to satisfy a

Simplicity criterion: Of the several "reasonable" interpretations (decompositions) of a scene, the one which contains the smaller number of bodies is preferable.

That is, an explanation or decomposition is simpler (and preferable) if it can be done with fewer parts.

Simplicity is not to be achieved at any cost, since the parsing of the scene has to produce 'plausible' bodies, since "simplicity" could be always achieved if each scene is reported as a single, gigantic body, obtained perhaps from more familiar ones through liberal use of adhesives (cf. also Sibelius' Monument).

The chief choices are surely:

- To choose a parsing, or
- To list many (perhaps rank-ordered) in case of ambiguity.

If we select the first alternative, further choices are

- to have a natural parsing (human).
- to have a canonical parsing, in the sense of minimizing some variable (the minimization of the number of bodies leads us to Sibelius' Monument, its maximization to the Trivial Solution of the metatheorem [page 4]).

Other kinds of 2-dim data We have been discussing identification of 3-dim bodies (through their 2-dim projections) in a 2-dim scene, purely on the basis of geometric regions. Many other kinds of information could be used, such as texture, color, and shadows.

Nevertheless, it is interesting to see how far the identification of bodies can go if only geometric properties are used.

Conclusion Finding bodies in a 2-dim scene is a task not very precisely defined, because of the ambiguities inherent in any projection process. On these grounds, the concept of 'body' is best described through familiarity, human opinion and consensus. We are forced to this because any scene could be partitioned in several ways (cf. fig. 'PARALLELEPIPED') only some of which may be considered plausible or 'sensible' (natural, common, standard) partitions in regard to the bodies forming it.

## TOTAL ANALYSIS OF VERTICES

Synopsis Here a scene is considered as formed by several regions; bodies are adequate collections of regions. The problem of identifying bodies is restated as the problem of finding whether two regions belong or do not belong to the same body. This question is answered by examining the vertices of the scene.

It is shown that a single vertex never conveys conclusive evidence, so that at least a pair of vertices is required to isolate a body; familiar and unfamiliar configurations of objects help to understand how the vertices are to be used in this task.

### Vertices are the important feature

All faces of polyhedra are bounded by edges.

All edges terminate in vertices.

== This thesis deals with the analysis of visual scenes composed mainly by three-dimensional planar objects



== These are limited by flat surfaces



== All these bodies share as a common feature the edge: place where two planes [faces] meet (but see page 57 ).



== Wherever several edges or faces meet, a vertex appears. This is also a common feature for all the bodies.



A body is formed by vertices with edges connecting some of these. When a 3-dim body is projected into a 2-dim body, its 3-dim vertices (which we will call genuine 3-dim vertices) are transformed into genuine 2-dim vertices, known as images of the 3-dim vertices, as figure 'GENUINE' (in next page) indicates.

That is, a genuine 2-dim vertex has come from a genuine 3-dim vertex. Some 2-dim "false" vertices appear too; they do not come



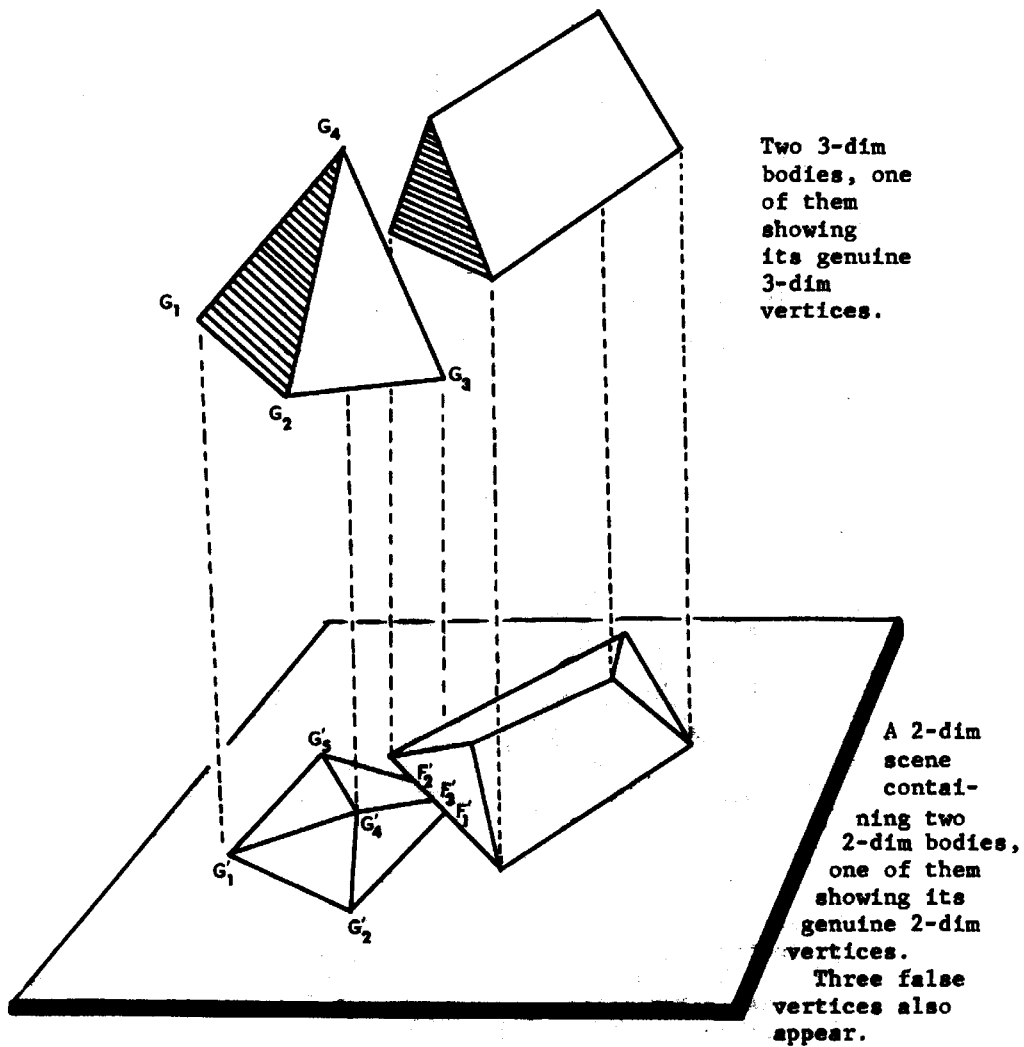


Figure 'GENUINE'

A genuine vertex (such as  $G_1'$ ) is one whose counterimage ( $G_1$  in this case) belongs to some body; a false vertex such as  $F_2'$ , is a virtual intersection, and generally has no counterimage in the 3-dim world. See fig. 'NODES'.

from genuine 3-dim vertices, but rather from the partial occlusion of parts of opaque bodies [transparent objects give rise to different kind of false vertices; Guzmán {MS Thesis} deals with them by using transparent models, and a mode of operation of TD, the recognizer, that re-interprets or ignores certain types of vertices. {AFCLR-67-0133}].

False vertices do not belong to any object.

Genuine and false vertices The classification of vertices into categories "genuine" and "false" will allow isolation of objects in a picture; in fig. 'GENUINE', elimination of vertices  $F_1'$ ,  $F_2'$ , and  $F_3'$  divides the genuine nodes of the network (see fig. 'NODES') into two non-connected components,  $\triangle$  and  $\square$ , correctly separating the two bodies.

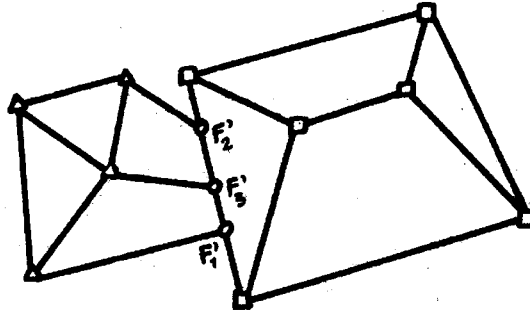


Figure 'N O D E S'

False vertices arise from the intersection of two projected edges, one of which is typically occluded in part by a face bordered by the other. Elimination of the false nodes  $F_1'$ ,  $F_2'$  and  $F_3'$  disconnects the network in two separate components, which are the bodies sought for.

This suggests the following

2-dim body (first approx. to definition). Set of regions possessing only genuine vertices, and separated from other bodies by false vertices.

In this way, the problem of identifying bodies is equivalent to the problem of identifying genuine vertices, segregating the false ones.

Problems to be solved The computation of this equivalence is challenged by several problems:

- = The distribution and position of bodies may be such that false vertices look like genuine vertices (fig. 'CAUTION').

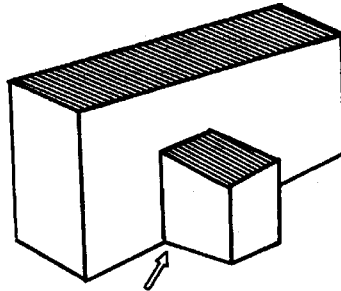


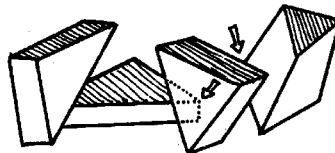
Fig. 'CAUTION'  
That vertex looks genuine, but is false.

Global information (analysis of more than one vertex) is needed in general to distinguish them. In other words, although false vertices are those which separate two bodies, and 2-dim genuine vertices originate from 3-dim genuine vertices, to segregate them requires more than the simple analysis of their shape.

- = Some genuine vertices look like false vertices.



- = Genuine vertices of a body may not be present in the scene, or may be supplanted by false vertices.



- = A single body may have totally disconnected sections (portions).



- = Continuation is not clear; some doubts arise if the object in the foreground covers one or two bodies (fig. 'CONTINUATION'); the simplicity criterion prefers the single body interpretation.

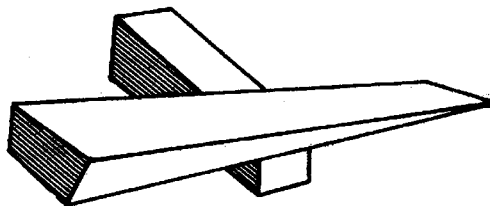


Fig. 'CONTINUATION'  
Continuation is not clear.

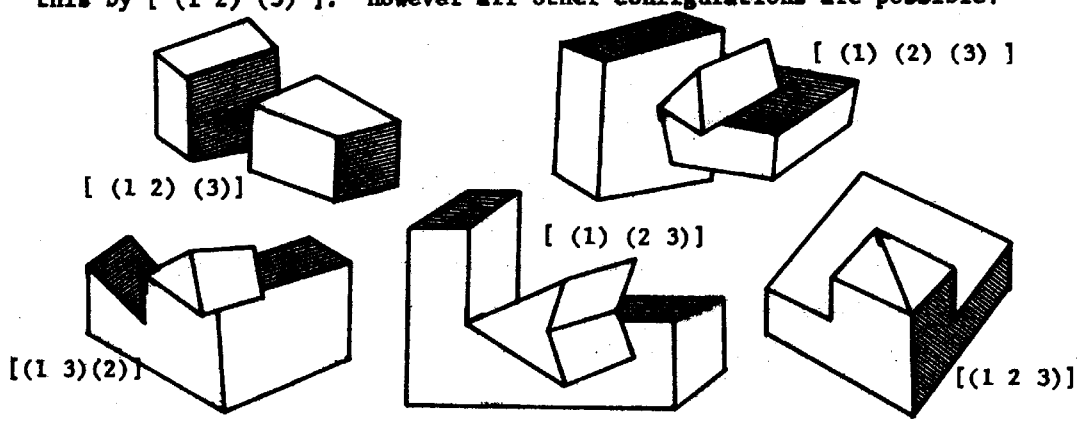
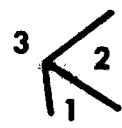
In brief, difficulties are of two kinds:

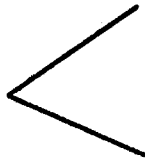
- Genuine and false vertices can not be distinguished locally (see Theorem below).
- Even when they are completely classified, problem of fig. 'CONTINUATION' remains.

The solution of these problems will have to make use of more global information.

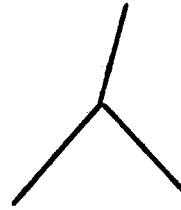
Classification of Vertices The table 'VERTICES' in next page classifies vertices according to their form, number of lines and angles among the lines. It contains the most common types; vertices having more edges could have been included.

Let us consider one of these types, ARROW. Three regions called 1, 2, and 3, form it. The standard, most common ARROW configuration is a body with faces 1 and 2 seen against some other object 3. We indicate this by [ (1 2) (3) ]. However all other configurations are possible:

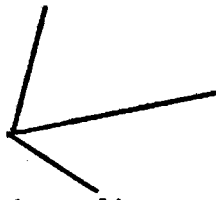




'L'.- Vertex where two lines meet.



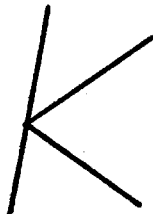
'FORK'.- Three lines forming angles smaller than 180 degrees.



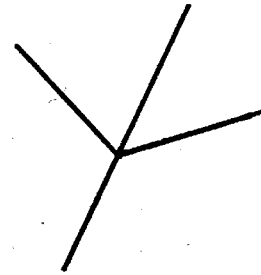
'ARROW'.- Three lines meeting at a point, with one of the angles bigger than 180 degrees.



'T'.- Three concurrent lines, two of them collinear.



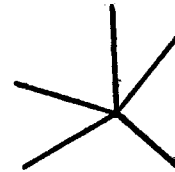
'K'.- Two of the lines are collinear, and the other two fall on the same side of such lines.



'X'.- Two of the lines are collinear, and the other two fall on opposite sides of such lines.



'PEAK'.- Formed by four or more lines, when there is an angle bigger than  $180^\circ$ .



'MULTI'.- Vertices formed by four or more lines, and not falling in any of the preceding types.

TABLE 'VERTICES'  
Classification of rectilinear vertices.

Thus, for an ARROW, all the groupings of its faces are possible; any procedure that, by looking at an Arrow tries to decide how its faces are grouped into bodies, will always make mistakes.

The generalization of the above analysis to all other types of vertices proves the following

**"Theorem"**. There does not exist a set of local decision procedures  $[\mu_i]$ , each one looking or getting information from one vertex and establishing b-equivalences among some of their faces (two faces  $a$  and  $b$  are b-equivalent, indicated  $a \equiv b$ , if the  $\mu_i$  decides that they belong to the same body; this is an equivalence relation), using information only from that vertex (it does not look at the other vertices or at the values of the  $\mu$ 's at the other vertices), which will partition all scenes correctly.

That is, the following machine will not work for all scenes:

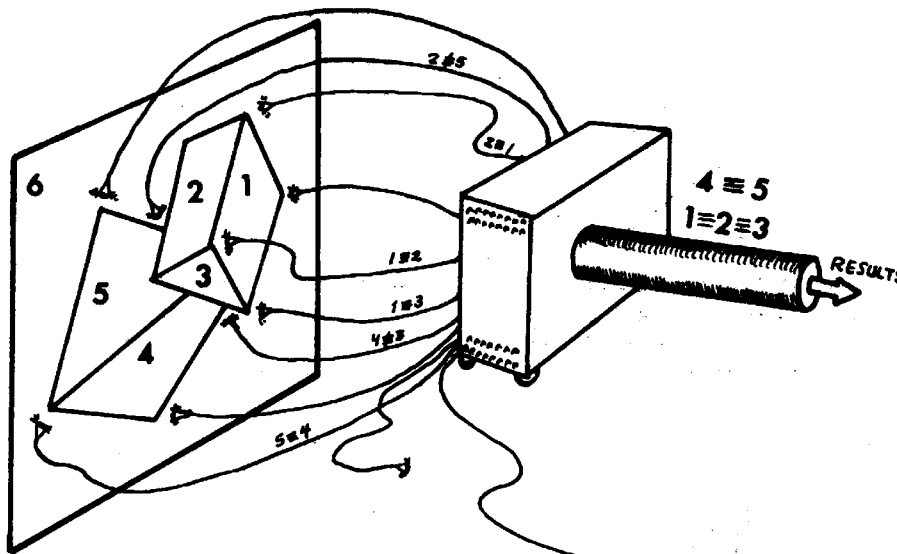
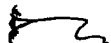


Figure 'MACHINE'

The decision procedures  $\mu_i$ , represented as 'eyes' here, decide by processing information at exactly one vertex; the box in the right accepts all these decisions and passes them as results. No matter what set of  $\mu_i$  we choose, there exists a scene that induces an incorrect partition by our machine.

A stronger assertion is that, in view of inherent ambiguity, there is not even any global procedure! 

All the different groupings of regions of a vertex into bodies are possible; this is illustrated by the following complete set of scenes, each one of them showing a different partitioning of a type of vertex. These examples are useful also in giving an idea of unusual, as well as familiar scenes; we will have later occasion to use them, when searching for heuristics to form bodies.

Generation of partitions

```

1  compo ( (1 2) )
   ((1) (2))
2  ((1 2))
   2

```

There are only two partitions of a set of two elements. **2**

Partitions of a set of **3** elements

```

1  compo ( (1 2 3) )
   ((1) (2) (3))
2  ((1 2) (3))
3  ((1 3) (2))
4  ((1) (2 3))
5  ((1 2 3))
   5

```

Partitions of a set of **4** elements

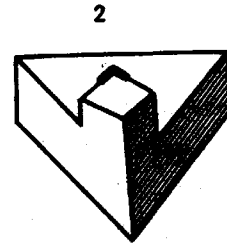
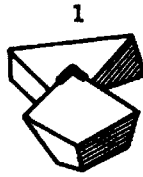
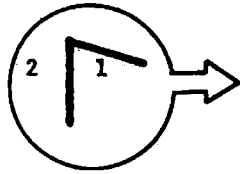
```

1  compo ( (1 2 3 4) )
   ((1) (2) (3) (4))
2  ((1 2) (3) (4))
3  ((1 3) (2) (4))
4  ((1 4) (2) (3))
5  ((1) (2 3) (4))
6  ((1 2 3) (4))
7  ((1 4) (2 3))
8  ((1) (2 4) (3))
9  ((1 2 4) (3))
10 ((1 3) (2 4))
11 ((1) (2) (3 4))
12 ((1 2) (3 4))
13 ((1 3 4) (2))
14 ((1) (2 3 4))
15 ((1 2 3 4))
   15

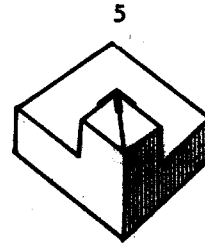
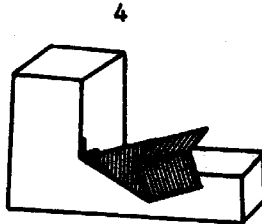
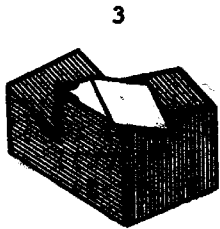
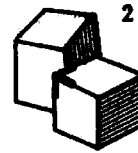
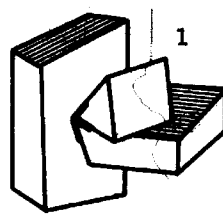
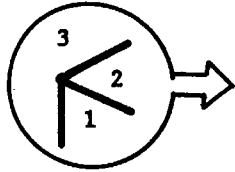
```

↑  
 Figures in the next few pages are numbered according to the numbers in the leftmost column in these tables.

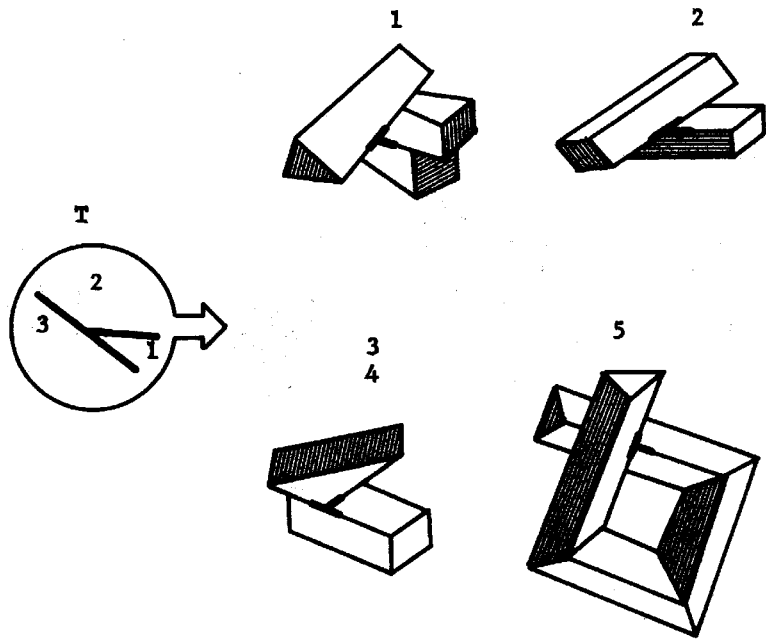
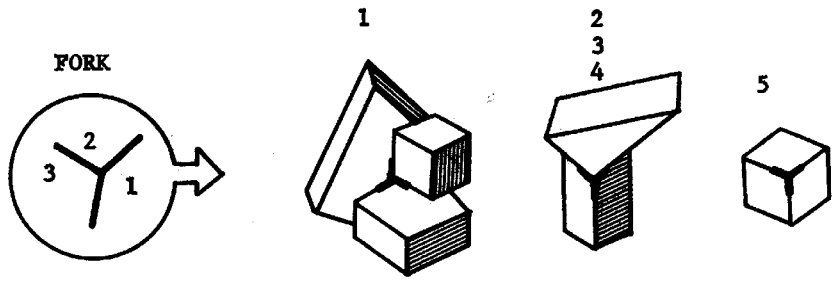
CORNER

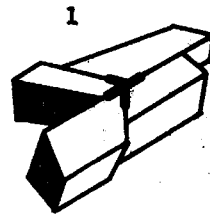
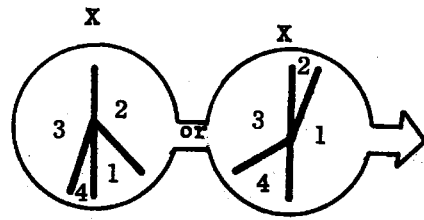


ARROW

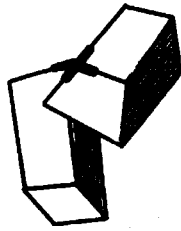




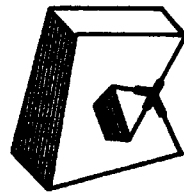




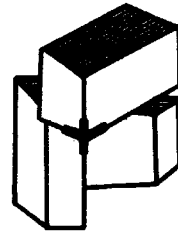
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11



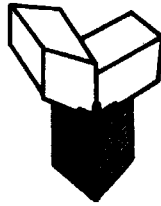
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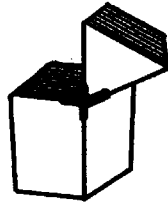
4



5



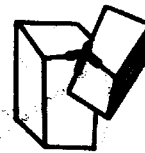
6  
14



7

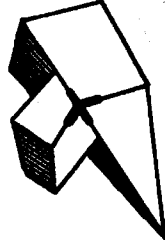


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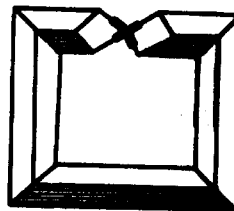


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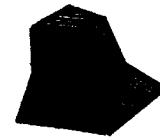
13

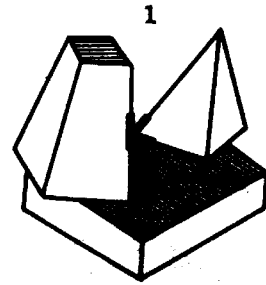
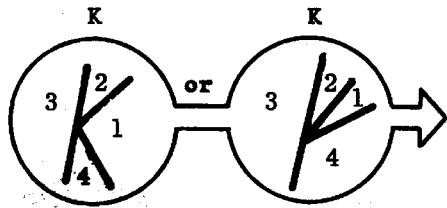


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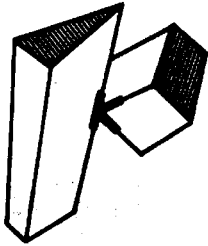


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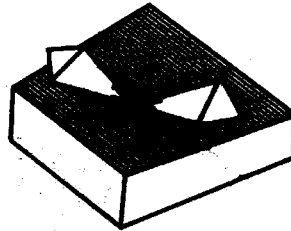




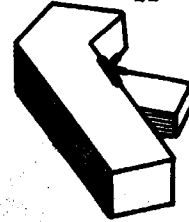
2  
4  
7



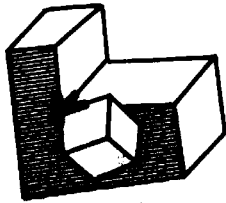
3



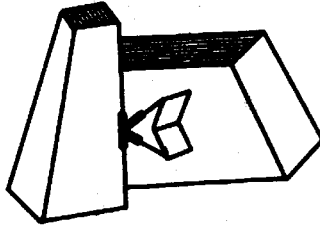
5  
11



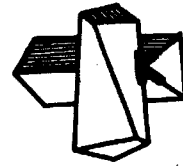
6  
13



8



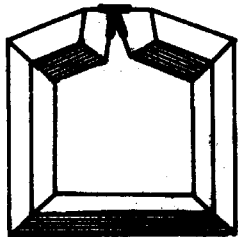
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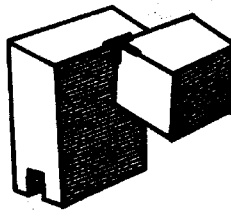
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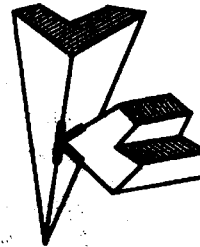
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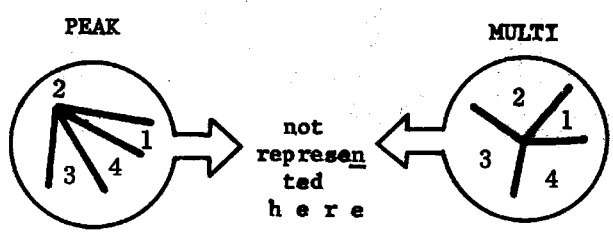
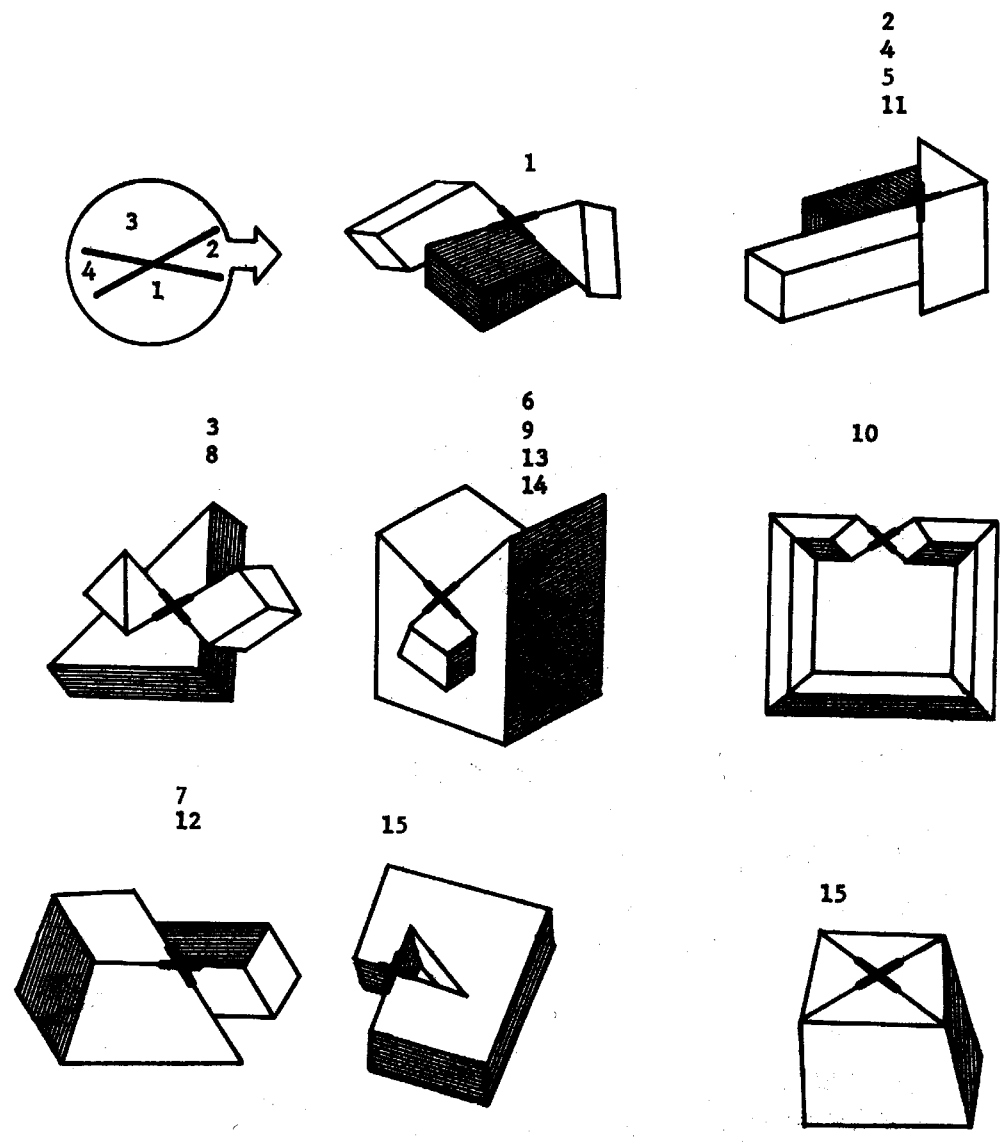


12



14





Digression 1. An alternate approach

Suggestion

As an alternate approach, one could try to use the faces as a basis for identification. For instance, use two scenes (left image, right image) or pictures, localize a sharp feature in one of them (vertex, crack in the face, peculiar texture, etc.) and by correlation or some other method, find it also in the other picture. Having found a few points in both images in this manner, determine the plane of the face, in 3-dim space. When several faces are thus identified, we can compute, if desired, their intersection and obtain the edges (lines). It will generally suffice to ignore the edges and rely on the faces. Since it is reasonable to expect considerable difficulty in finding lines and in differentiating lines caused by edges from those caused by shadows, an approach which avoids the lines altogether looks promising. But in this case, in addition to requiring two images, several correlations are needed (if we choose this method), a generally time-consuming and error-prone task.

## S E E, A PROGRAM THAT FINDS BODIES IN A SCENE

### Synopsis

#### How SEE works.

Algorithms and heuristics are presented, implemented in a program, that analyze a scene into a composition of three-dimensional objects. Only the two-dimensional representation of the three-dimensional scene is available as input, and is described by a collection of surfaces, lines and vertices.

SEE looks for three-dimensional objects in two-dimensional scenes. The program does not require a pre-conceived idea of the form of the objects which could appear in the scenes. It is only assumed that they will be solid objects formed by plane surfaces. Thus, SEE can not find "pentagonal prisms" or "houses" in a scene, since it does not know what a "pentagonal prism" is; but it will usually isolate the pentagonal prisms (or any other regular or irregular solid) in a scene, even if some of them are partially occluded, without having a description of such objects. It does this by paying attention to configuration of surfaces and lines which would make plausible three-dimensional solids, and in this way 'bodies' are identified.

The analysis that SEE makes of the different scenes generally agrees with human opinion, although in some ambiguous cases they tend to be conservative. The most interesting thing about the program is how well it deals with occlusions. Many examples in the next section 'Analysis of many scenes' illustrate the features and peculiarities of the program, and also illustrate the effects of inaccuracies introduced in the data.

L 10

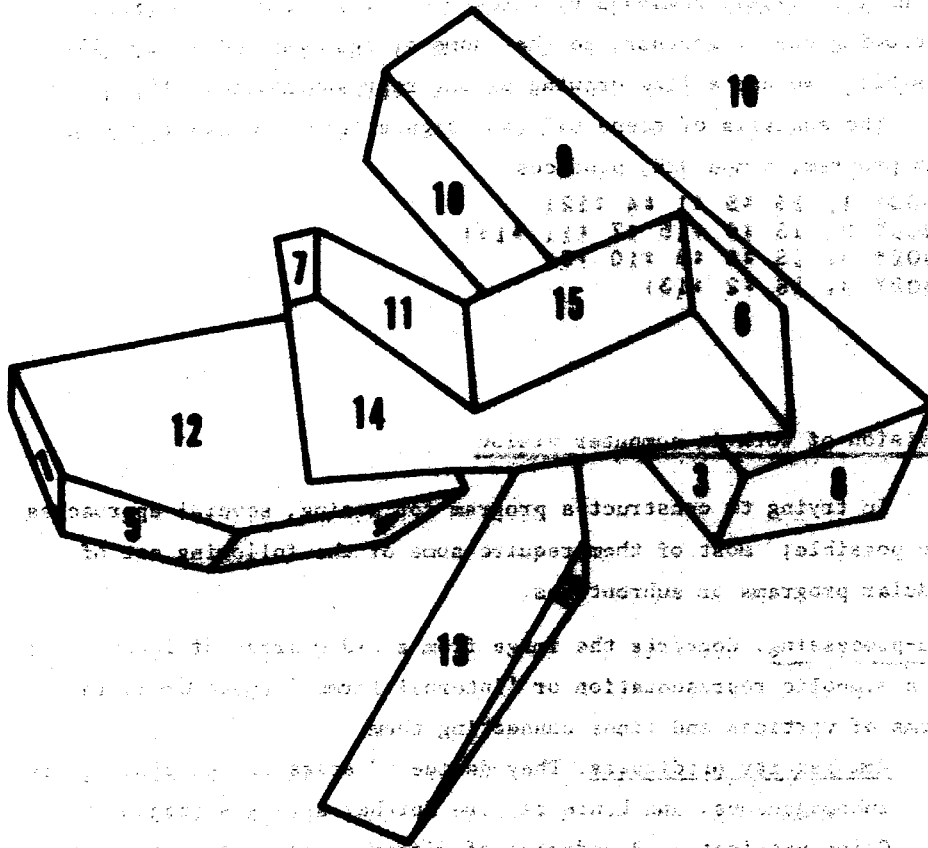


FIGURE 'L-10'

A scene analyzed by SEE.

## INTRODUCTION

Here is a program that locates objects in an optical image of a scene most likely composed by three-dimensional solids, perhaps occluding one to another, so that some of them may not be totally visible. We use a line drawing as our representation of the scene.

The analysis of scene L10 (see figure 'L10' in next page) by our program, named SEE, produces

```
(BODY 1. IS :5 :1 :4 :12)
(BODY 2. IS :6 :15 :7 :11 :14)
(BODY 3. IS :8 :9 :10 :3)
(BODY 4. IS :2 :13)
```

### Division of work in computer vision

In trying to construct a program for seeing, several approaches are possible; most of them require some of the following set of modular programs or subroutines.

Pre-processing. Converts the image from a 2-dim array of intensities to a symbolic representation or 'internal format' (page 66), in terms of vertices and lines connecting them.

Homogeneity predicates. They decide if areas of the picture are inhomogeneous, and hence require further analysis (page 16).

Color predicates. Boundaries of different color suggest lines.

Line finder. Locates lines of points having certain property (such as being inhomogeneous, or having a large light intensity gradient).

Vertex finder. Concurrent lines are merged, or a vertex is created at their meeting point.

Consolidator. Eliminates the false lines and finds more lines, incrementing in this way as much as possible the reliability of the system.



Illumination program. Discovers where the main light sources are.

Shadows program. Detects shadows so as to eliminate them.

Missing lines program. General shape considerations suggest places where faint lines can remain undetected.

Body recognition. Partitions the scene into appropriate subsets, each one being a body or object. Thus, SEE is a body-recognition program.

Object identification. These objects are compared against abstract descriptions (models) of cubes, pyramids, etc., so that a classification is done, and a name is attached to each one. In the process, certain parameters may acquire values: the height of the pyramid is observed.

Positioning. Having analyzed the scene, the relevant objects are positioned in three-dimensional space, and additional relations among them are discovered (support, obstruction, etc.). Enough information is obtained to allow the mechanical arm to manipulate the objects and achieve its goals.

Stereo. More than one view are analyzed (page 233) and from them, 3-dim spatial positions are found.

Focussing. The computer, by adjusting the focus of its lens, acquires knowledge of how far the objects are.

Feedback among these parts is more necessary as the complexity of the scene and of the desired goals increases.

Recognizer. The task of body recognition and body identification was formerly accomplished by a single program (for instance, DT or TD {my MS Thesis}) that compares the symbolic description of the scene against the symbolic or abstract description of the model of the desired object, in a kind of two-dimensional matching, to isolate instances of that object in the scene.

#### Technical descriptions of SEE

1. Annotated listings. Above all, the primary source of information is the listing of the programs, that appears complete in this thesis. They are written in Lisp. If, despite my efforts, some of my explanations are not clear, consult it: it is annotated. The programs themselves,

examples, test data, results, instructions, etc., are in the DEC-magnetic tape "GUZMAN F" at Project MAC (AI group). Instructions are given in page 78.

2. This section of the thesis contains a description and discussion of the different algorithms and procedures used.

3. Published papers that cover part of the material at somewhat less depth, and therefore are more readable, are also available [FJCC 68] [Pisa 68]. Except that they contain some examples not included here, they contain no other information not covered here.

4. An internal report [MAC M 357] described an earlier version of SEE.

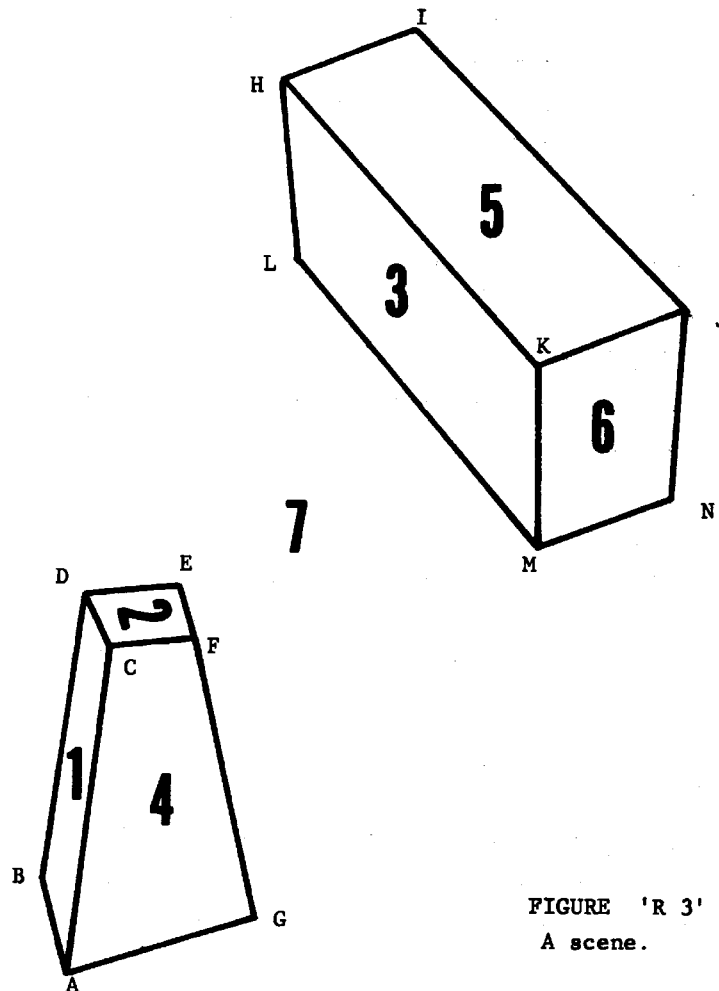


FIGURE 'R 3'  
A scene.

## INPUT FORMAT

Eventually, several preprocessors will be able to receive data through an input camera and reduce it to the "internal format" of a scene, in the form required by SEE. For testing purposes, the scenes are entered by hand in a simplified format, called 'input format', to be described now. All the scenes analyzed by SEE have been written in input format.

Example. R3 . The input format of scene R3 is  
(DEFPROP R3 (:7) BACKGROUND)

```
(NOT (SETQ R3 (QUOTE (
XA 4.3 4.5 (X:7 XG X:4 XC X:1 XB)
XB 4.0 5.7 (X:7 XA X:1 XD)
XC 4.8 8.5 (X:4 XF X:2 XD X:1 XA)
XD 4.5 9.15 (X:7 XB X:1 XC X:2 XE)
XE 5.65 9.25 (X:7 XD X:2 XF)
XF 5.85 8.6 (X:7 XE X:2 XC X:4 XG)
XG 6.6 5.2 (X:7 XF X:4 XA)
XH 6.9 15.4 (X:7 XL X:3 XK X:5 XI)
XI 8.5 16.0 (X:7 XH X:5 XJ)
XJ 11.8 12.6 (X:7 XI X:5 XK X:6 XN)
XK 10.0 11.9 (X:6 XJ X:5 XH X:3 XM)
XL 7.1 13.2 (X:7 XM X:3 XH)
XM 10.0 9.7 (X:7 XN X:6 XK X:3 XL)
XN 11.65 10.3 (X:7 XJ X:6 XM)
))))
R3 IN INPUT FORMAT
```

The first line declares :7 to be the background.\* We have to tell SEE which regions belong to the background. If this information is missing, a program is called that will compute the regions that belong to the background (see section 'Background discrimination by computer') prior to other calculations.

After that, the lines associate with each vertex its 2-dim coordinates and a list (which will later be called 'KIND'), in counterclockwise order, of regions and vertices radiating from that vertex.

The function PREPARA (see listing) converts the scene as just given to the "internal format" form which SEE expects. It does this by putting many properties in the property lists of the atoms representing vertices and regions (property lists in Lisp get explained in next page).

---

\*For the moment, ignore the % signs. They are used to distinguish right from left scenes.

Property lists in Lisp \* Each atomic expression in Lisp has a property list, which is a place where facts can be stored.

If it is desired to represent the fact that John is a 69 years old male, has a wife called Jacqueline, and a height of value 1.77 m, we could proceed in Lisp as follows:

- (1) We will agree that the atom 'JOHN' will represent our man.
- (2) In the property list of 'JOHN' we will store several properties or indicators and their values, using the function PUTPROP, that stores information in the property list; thus  
(Putprop (quote John) (quote Jacqueline) (quote Wife))  
will add, under the indicator or property 'Wife', the value 'Jacqueline':

```
      JOHN  
      |  
      WIFE ----- JACQUELINE
```

- (3) Hence, the representation of our facts in Lisp is

```
      JOHN  
      |  
      SEX    --  MALE  
      |  
      AGE    --  69.0  
      |  
      WIFE   --  JACQUELINE  
      |  
      HEIGHT --  (1.77 m)
```

- (4) In fact, the property list of 'JOHN', which is the CDR of 'JOHN' in Lisp 1.6 {MAC M 313}, is  
(SEX MALE AGE 69.0 WIFE JACQUELINE HEIGHT (1.77 m) ...)
- (5) If later we want to know the age of John, we will ask  
(Get (quote John) (quote Age))  
and the value will be 69.0

---

\* This paragraph, which can be skipped if it is known what a property list is, will make the next section clearer.

FORMAT OF SCENE R3

R3  
 REGIONS (X16 X15 X13 X12 X11 X14 X17)  
 VERTICES (XN XM XL XK XJ XI XM XG XF XE XD XC XB  
 XA)  
 BACKGROUND (X17)  
 X16  
 NEIGHBORS (X15 X13 X17 X17)  
 VERTICES (XK XM XN XJ)  
 FOOP (X115 XK X13 XM X17 XN X17 XJ))  
 X15  
 NEIGHBORS (X13 X16 X17 X17)  
 VERTICES (XK XJ XI XM)  
 FOOP (X113 XK X16 XJ X17 XI X17 XM))  
 X13  
 NEIGHBORS (X17 X17 X16 X15)  
 VERTICES (XL XM XK XM)  
 FOOP (X117 XL X17 XM X16 XK X15 XM))  
 X12  
 NEIGHBORS (X14 X17 X17 X11)  
 VERTICES (XJ XE XD XC)  
 FOOP (X114 XF X17 XE X17 XD X11 XC))  
 X11  
 NEIGHBORS (X14 X12 X17 X17)  
 VERTICES (XC XD XB XA)  
 FOOP (X114 XC X12 XD X17 XD X17 XA))  
 X14  
 NEIGHBORS (X12 X11 X17 X17)  
 VERTICES (XC XA XG XF)  
 FOOP (X112 XC X11 XA X17 XG X17 XF))  
 X17  
 NEIGHBORS (X16 X16 X13 X13 X15 X15 X12 X12 X14 X14  
 X11 X11)  
 VERTICES (XM XN XL XM XI XJ XE XF XG XA XM XD)  
 FOOP (X116 XM X16 XM X13 XL X13 XM X15 XI X15  
 X1 X1))  
 XJ  
 XCOR 11.649999  
 YCOR 10.200000  
 NVERTICES (XJ XM)  
 NREGIONS (X17 X16)  
 KIND (X17 XJ X16 XM)  
 TYPE (L (X16 X17))  
 XM  
 XCOR 10.8  
 YCOR 9.700000  
 NVERTICES (XM XK XL)  
 NREGIONS (X17 X16 X13)  
 KIND (X17 XM X16 XK X13 XL)  
 TYPE (ARROW (XK XM XN XL X16 X13 X17))  
 XL  
 XCOR 7.100000  
 YCOR 13.300000  
 NVERTICES (XM XM)  
 NREGIONS (X17 X13)  
 KIND (X17 XM X13 XM)  
 TYPE (L (X13 X17))  
 XA  
 XCOR 10.8  
 YCOR 11.000000  
 NVERTICES (XJ XM XM)  
 NREGIONS (X16 X15 X13)  
 KIND (X16 XJ X15 XM X13 XM)  
 TYPE (FORK XK)

XJ  
 XCOR 11.700000  
 YCOR 12.000000  
 NVERTICES (XI XK XM)  
 NREGIONS (X17 X15 X16)  
 KIND (X17 XI X15 XK X16 XM)  
 TYPE (ARROW (XK XJ XI XM X15 X16 X17))  
 XI  
 XCOR 0.5  
 YCOR 10.0  
 NVERTICES (XM XJ)  
 NREGIONS (X17 X16)  
 KIND (X17 XM X16 XJ)  
 TYPE (L (X16 X17))  
 XM  
 XCOR 6.000000  
 YCOR 15.300000  
 NVERTICES (XL XK XI)  
 NREGIONS (X17 X13 X16)  
 KIND (X17 XL X13 XK X15 XI)  
 TYPE (ARROW (XK XM XL XI X13 X15 X17))  
 XG  
 XCOR 6.000000  
 YCOR 5.100000  
 NVERTICES (XF XA)  
 NREGIONS (X17 X14)  
 KIND (X17 XF X14 XA)  
 TYPE (L (X14 X17))  
 XF  
 XCOR 5.800000  
 YCOR 6.000000  
 NVERTICES (XE XC XG)  
 NREGIONS (X17 X12 X14)  
 KIND (X17 XE X12 XC X14 XG)  
 TYPE (T (XC XF XG XE X12 X14 X17))  
 XE  
 XCOR 5.640000  
 YCOR 9.25  
 NVERTICES (XD XF)  
 NREGIONS (X17 X12)  
 KIND (X17 XD X12 XF)  
 TYPE (L (X12 X17))  
 XD  
 XCOR 4.5  
 YCOR 9.140000  
 NVERTICES (XD XC XE)  
 NREGIONS (X17 X11 X12)  
 KIND (X17 XD X11 XC X12 XE)  
 TYPE (ARROW (XC XD XE X11 X12 X17))  
 XC  
 XCOR 4.000000  
 YCOR 0.5  
 NVERTICES (XF XD XA)  
 NREGIONS (X14 X12 X11)  
 KIND (X14 XF X12 XD X11 XA)  
 TYPE (FORK XC)  
 XG  
 XCOR 4.8  
 YCOR 9.000000  
 NVERTICES (XA XD)  
 NREGIONS (X17 X11)  
 KIND (X17 XA X11 XD)  
 TYPE (L (X11 X17))  
 XA  
 XCOR 4.300000  
 YCOR 4.5  
 NVERTICES (XD XC XE)  
 NREGIONS (X17 X14 X11)  
 KIND (X17 XD X14 XC X11 XE)  
 TYPE (ARROW (XC XA XE X14 X11 X17))

TABLE

R 3 IN INTERNAL FORMAT

## INTERNAL FORMAT

The program assumes the scene in a special symbolic format, which basically, is an arrangement of relations between vertices and regions, which are represented by atoms having adequate properties in their property-lists.

A scene has a name which identifies it; this name is an atom whose property list contains the properties 'REGIONS', 'VERTICES', and 'BACKGROUND'. For example, the scene R3 (see figure R3) has the name 'R3'. In the property list of R3 we find (see also table "R3 IN INTERNAL FORMAT")

```

REGIONS      (:6 :5 :3 :2 :1 :4 :7)
              Unordered list of regions
              composing the scene R3. Order is immaterial.

VERTICES     (XN XM XL XK XJ XI XH XG XF XE XD XC XB XA)
              Unordered list of vertices
              composing the scene R3.

BACKGROUND  (:7)
              Unordered list of regions
              composing the background of
              scene R3.
    
```

Region A region corresponds to a surface limited by simple closed curves. Regions are represented by atoms that start with a colon (:). For instance, in R3, the surface delimited by the vertices K J N M is a region, called :6, but D E F G A C is not.

Each region has as name an atom which possess additional properties describing different attributes of the region in question. These are 'NEIGHBORS', 'KVERTICES', and 'FOOP'. For example, the region in scene R3 formed by the lines DE, EF, FC, CD has ':2' as its name. In the property list of :2 we find:

```

NEIGHBORS    (:4 :7 :7 :1)
              Counterclockwise ordered list of
              all regions which are neighbors to
              :2. For each region, this list is
              unique up to cyclic permutation.
    
```

KVERTICES (XF XE XD XC)

Counterclockwise ordered list of all vertices which belong to region :2. This list is unique up to cyclic permutation.

FOOP ((X:4 XF X:7 XE X:7 XD X:1 XC))

Each sublist is a counterclockwise ordered list of alternating neighbors and kvertices of :2. Each sublist is unique up to cyclic permutation, and indicates a simple boundary.

Each sublist of the FOOP property of a region is formed by a man who walks on its boundary always having this region to his left, and takes note of the regions to his right and of the vertices which he finds in his way.

As other example, in the property list of :7 we find:

```
NEIGHBORS (X:6 X:6 X:3 X:3 X:5 X:5 X:2 X:2 X:4 X:4
X:1 X:1)
KVERTICES (XN XM XL XH XI XJ XE XF XG XA XB XD)
FOOP ((X:6 XN X:6 XM X:3 XL X:3 XH X:5 XI X:5
XJ) (X:2 XE X:2 XF X:4 XG X:4 XA X:1 XB X:1 XD))
```

Vertex A vertex is the point where two or more lines of the scene meet; for instance, A, G, and K are vertices of the scene R3. Each vertex has as name an atom which possess additional properties describing different attributes of the vertex in question. These are 'XCOR', 'YCOR', 'NVERTICES', 'NREGIONS', 'KIND', 'TYPE', and 'NEXT'. For example, vertex J (see scene R3) has in its property list:

```
XCOR      11.799999      x-coordinate
YCOR      12.600000      y-coordinate
NVERTICES (XI XK XN)
```

Counterclockwise ordered list of vertices to which J is connected. Unique up to cyclic permutation.

NREGIONS (X:7 X:5 X:6)

Counterclockwise ordered list of regions to which J is connected. Unique up to cyclic permutation.

KIND (X:7 X:1 X:5 X:K X:6 X:N)

Counterclockwise ordered list of alternating nregions and nvertices of J. This list is unique up to cyclic permutation.

TYPE (ARROW (X:K X:J X:1 X:N X:5 X:6 X:7))

List of two elements; the first is an atom indicating the type-name of J; the second is the datum of J. To be explained in next section.

(NEXTE)

Vertex J does not have the indicator NEXTE in its property list.

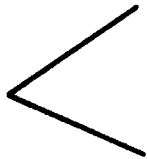
The KIND property of a vertex is formed by a man who stands at the vertex and, while rotating counterclockwise, takes note of the regions and vertices which he sees. NREGIONS and NVERTICES are then easily derived from KIND, by taking its odd positioned elements, and its even positioned elements, respectively.

NEXTE is a property that appears in certain vertices (none in scene R3); it will be explained in next section.

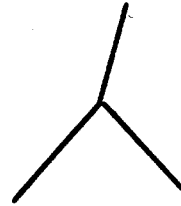
The property TYPE is also put by the function PREPARA; it classifies each vertex into one of several types, as described in table

'VERTICES' (next page).





'L'.- Vertex where two lines meet.



'FORK'.- Three lines forming angles smaller than 180 degrees.



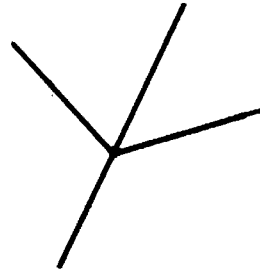
'ARROW'.- Three lines meeting at a point, with one of the angles bigger than 180 degrees.



'T'.- Three concurrent lines, two of them collinear.



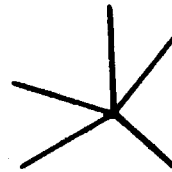
'K'.- Two of the lines are collinear, and the other two fall on the same side of such lines.



'X'.- Two of the lines are collinear, and the other two fall on opposite sides of such lines.



'PEAK'.- Formed by four or more lines, when there is an angle bigger than  $180^\circ$ .



'MULTI'.- Vertices formed by four or more lines, and not falling in any of the preceding types.

TABLE 'VERTICES'  
Classification of rectilinear vertices.

## TYPES OF VERTICES

The disposition, slope and number of lines which form a vertex are used to classify it, task performed by the function (TYPEGENERATOR L) by storing in its property list its corresponding type.

The TYPE of a vertex is always a list of two elements; the first is the type-name: one of 'L', 'FORK', 'ARROW', 'T', 'K', 'X', 'PEAK', 'MULTI'; the second element is the datum, which generally is a list, whose form varies with the type-name and contains information in a determined order about the vertex in question (see table 'VERTICES').

### Vertices where two lines meet.

L. - A vertex formed by only two lines is always classified as of type 'L'. Two angles exist at it, one bigger and other smaller than  $180^\circ$ . The datum is a list of the form

(E<sub>1</sub> E<sub>2</sub>), where E<sub>1</sub> is the region which contains the angle smaller than  $180^\circ$ .

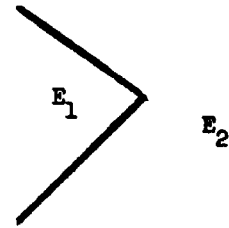
E<sub>2</sub> is the region which contains the angle greater than  $180^\circ$ .

For instance, in scene R3 (see fig. 'R3').

G has in its property list:

```
TYPE      (L (%:4 %:7) )
```

The vertices of type L present in R3 are B, E, G, I, L, N.



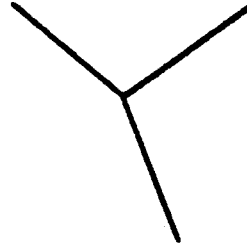
### Vertices where three lines meet.

FORK. - Three lines meeting at a point and forming angles smaller than  $180^\circ$  form a FORK.

Its datum is the vertex itself at which the fork occurs. For instance, vertex K has in its property list

TYPE (FORK %K)

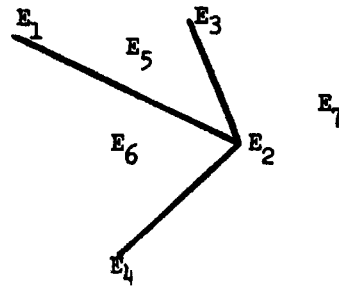
The vertices of type FORK present in R3 are C, K.



ARROW. - Three lines meeting at a point, with one of the angles bigger than  $180^\circ$ .

The datum of an ARROW is a list like  $(E_1 E_2 E_3 E_4 E_5 E_6 E_7)$  where

- $E_1$  is the vertex at the 'tail',
- $E_2$  is the vertex at the center.
- $E_3$  is the vertex at the left of  $E_1 \rightarrow E_2$
- $E_4$  is the vertex at the right.
- $E_5$  is the region at the left.
- $E_6$  is the region at the right.
- $E_7$  is the region which contains the angle bigger than  $180^\circ$ .



For instance, vertex H has in its property list

TYPE (ARROW (%K %H %L %I %:3 %:5 %:7))

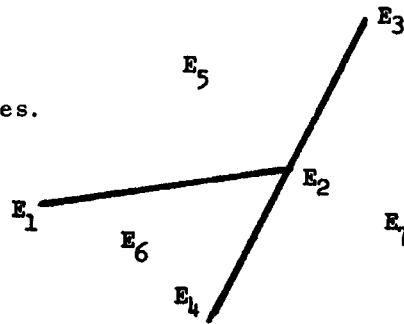
--fig R3

The vertices of type ARROW present in R3 are A, D, H, J, M.

T. - Three concurrent lines, of which two are collinear.

The datum for a T is a list of the form  $(E_1 E_2 E_3 E_4 E_5 E_6 E_7)$ , where

- $E_1$  is the vertex at the 'tail' of the T.
- $E_2$  is the central vertex.
- $E_3$  is a vertex such that  $E_1 E_2 E_3$  is an angle between 90 and 180 degrees.
- $E_4$  is a vertex such that  $E_1 E_2 E_4$  is an angle smaller than 90 degrees. That is,  $E_3 E_2 E_4$  are collinear.
- $E_5$  is the region which contains the angle between 90 and 180 degrees.



$E_6$  is the region which contains the angle smaller than 90 degrees.

$E_7$  is the "central" region (where the  $180^\circ$  angle is).

For instance, vertex F (fig. R3) has in its property list

TYPE (T (%C %F %G %E %:2 %:4 %:7))

The vertices of type T present in R3 are F only.

See also "Matching T's or Nextes" below.

Vertices where four lines meet.

K.- When two of the lines are collinear, and the other two fall in the same side of such lines, The datum is a list of the form

( $E_1 E_2 E_3 E_4 E_5 E_6 E_7 E_8$ ) where

$E_1$  is the central region.

$E_2$  is the region having the  $180^\circ$  angle.

$E_3$  is the collinear vertex which falls to the left of  $E_1 E_2$ .

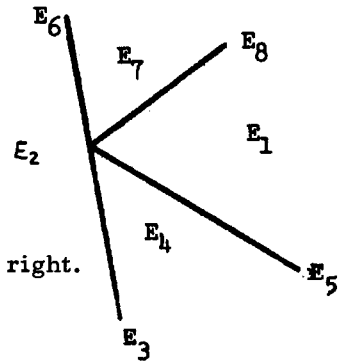
$E_4$  is the region to the left of  $E_1 \rightarrow E_2$

$E_5$  is the vertex to the left of  $E_1 \rightarrow E_2$

$E_6$  is the collinear vertex which falls to the right.

$E_7$  is the region to the right of  $E_1 \rightarrow E_2$ .

$E_8$  is the other vertex to the right (of  $E_1$ ).



R3 contains no vertices of type K. PA of figure BRIDGE is of type 'K'.

X. - When two of the lines are collinear, and the other two fall in opposite sides of such lines. The datum is a list of the form

( $E_1 E_2 E_3 E_4 E_5 E_6$ ), where

$E_1$  is one of the collinear vertices.

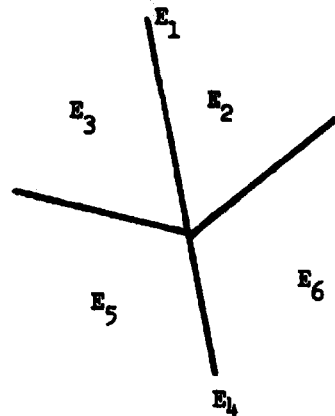
$E_2$  is the region to the left of  $E_1 C$ , where C is the vertex at the center.

$E_3$  is the region to the right of  $E_1 C$ ,

$E_4$  is the other collinear vertex.

$E_5$  is the region to the left of  $E_4 C$ .

$E_6$  is the region to the right of  $E_4 C$ .



For instance, we find in the property list of F  
(figure BRIDGE):

TYPE (X (QA:26 :22 G :21 :30) )

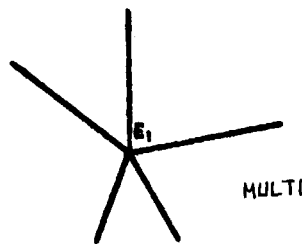
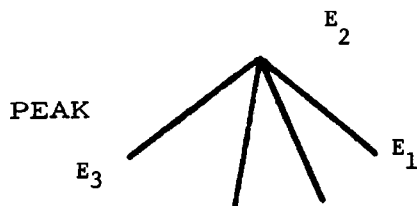
The vertices of type X present in BRIDGE are F, only.

The datum for an X may also be in the form  $(E_4 E_5 E_6 E_1 E_2 E_3)$ .

Vertices of four lines which are not of type K or X are either of type PEAK or MULTI.

Other types of vertices.

PEAK. - Formed by four or more lines, when there is an angle bigger than  $180^\circ$ .



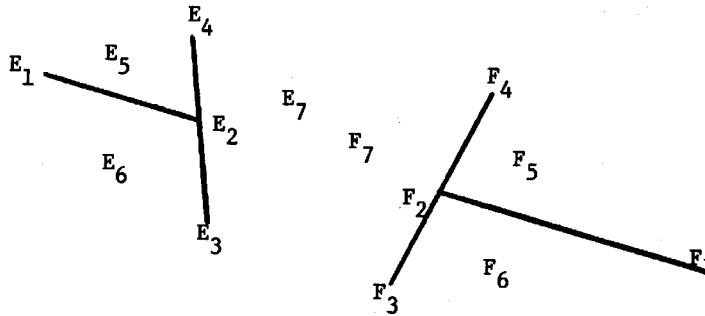
MULTI. - Vertices formed by four or more lines, and not falling in any of the preceding types, belong to the type MULTI. R3 contains no PEAKS or MULTIS.

The datum for vertices of type PEAK is of the form  $(E_1 E_2 E_3)$ , where  $E_2$  is the region that contains the angle bigger than 180 degrees;  $E_1$  is the vertex before  $E_2$ , and  $E_3$  is after (in the  $\oint$  sense).

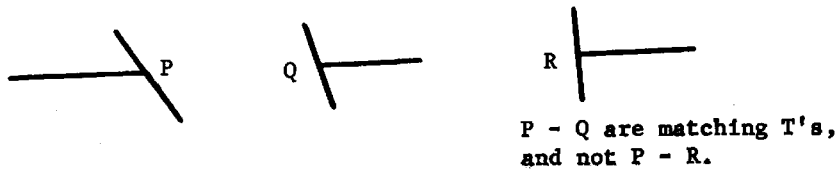
The datum for vertices of type MULTI is of the form  $E_1$ , where  $E_1$  is the vertex itself.

NEXTEs or Matching T's. Two T's which are collinear and facing each other (see figure) are called "matching T's", and each one is the "nexte" of the other. The indicator "NEXTE" is placed in such vertices.

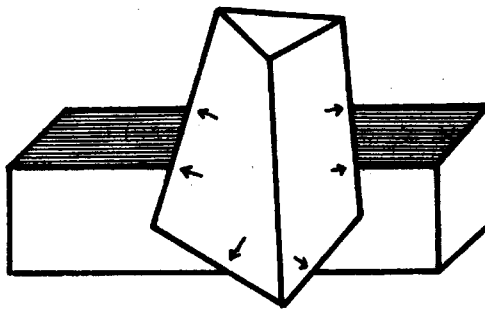
If the region  $E_7$  of a T (see figure) is the background, that T can not be a matching T.



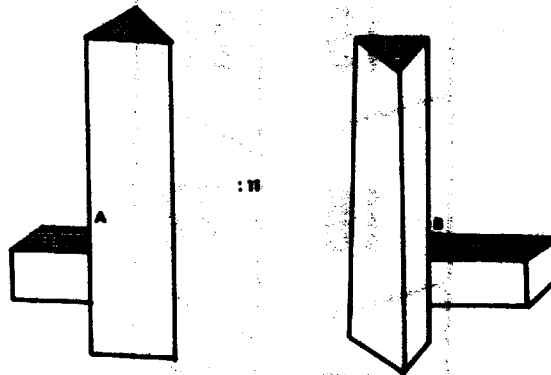
In the figure,  $E_2$  and  $F_2$  are matching T's because  $E_1-E_2$  is colinear with  $F_2-F_1$ . It is not required of  $E_3-E_4$  to be parallel to  $F_3-F_4$ . If several pairs of T's are possible, the closest is chosen:



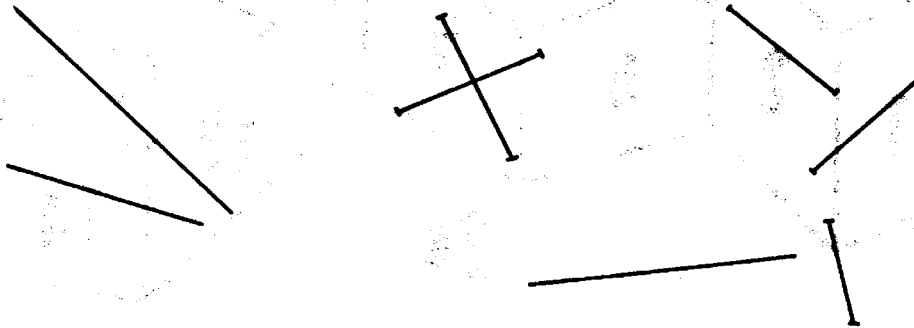
The matching T's will get involved in the determination of places where a body is occluded by another object and later emerges visible again.



For two T's to be NEXTEs or matching T's, it is required that neither  $E_7$  nor  $F_7$  be background. This requirement should be extended to all regions between  $E_7$  and  $F_7$ , since a line can not go "under" the background region:



A and B can not be NEXTEs, since :H is the background. Two straight lines always intersect (possibly at infinity); a way to detect these background regions **SUGGESTION** is to write functions (subroutines) that find out if two segments of line intersect, or if one segment intersects with a line.



#### LINES AND SEGMENTS

In the plane, two straight lines always meet. Two segments, or a line and a segment, may or may not meet. (a segment is a finite portion of a line).

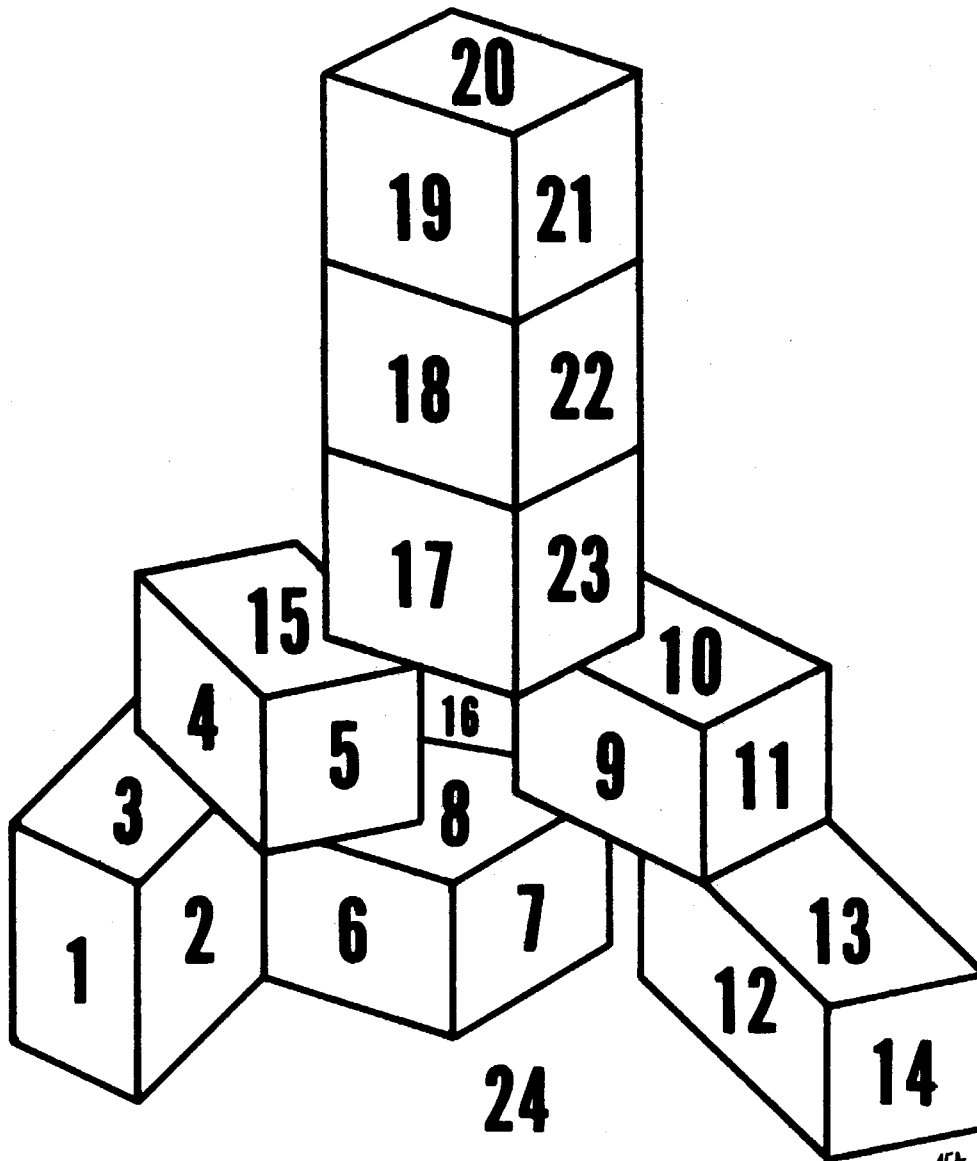


FIGURE 'TOWER'

AGA  
1968





## THE PROGRAM

We now describe SEE, and how it achieves its goals, by discussing the procedures, heuristics, etc., employed and the way they work. We begin with several examples.

Example A. Scene 'TOWER'. This scene (see figure 'TOWER') is analyzed by SEE, with the following results:

### RESULTS

(BODY 1. IS :2 :3 :1)  
(BODY 2. IS :15 :5 :4)  
(BODY 3. IS :23 :17)  
(BODY 4. IS :6 :7 :8)  
(BODY 5. IS :10 :11 :9)  
(BODY 6. IS :13 :14 :12)  
(BODY 7. IS :18 :22)  
(BODY 8. IS :20 :19 :21)

Results for scene TOWER

Example B. Scene 'MOMO'. Details of the program's operation are given. (skip to next page, if you wish).

↑Z \$L SEE 1 ↵

Go to DDT and load file SEE 1 (in tape GUZMAN F), a binary dump of the program SEE.

\$G

Start.

(UREAD MOMO S1 3) ↑Q

Read the file MOMO S1 (in tape GUZMAN C) from tape drive 3.

(PREPARA MOMO)

Convert MOMO from its Input Format form to Internal Format, the proper form that SEE expects.

(SEE (QUOTE MOMO))

Call SEE to work on MOMO.

Results appear in next page.

Notes: ↑Z (control Z) is keyed by striking the Z key while holding down simultaneously the CONTROL key. (Memos <sup>A.2</sup> 161, 59, 119)

↵ denotes carriage return.

\$ denotes the character "alt. mode". (See also instructions in listing)

SEE 58 ANALYZES MOMO  
 EVIDENCE  
 LOCALEVIDENCE  
 TRIANG  
 GLOBAL  
 ((NIL) (:38) G0044 G0043 G0041 G0040) (:19) G0046 G0045 G0 etc.  
 LOCAL  
 (LOCAL ASSUMES (:17) (:9) SAME BODY)  
 (LOCAL ASSUMES (:9 :17) (:18) SAME BODY)  
 LOCAL  
 ((NIL) (NIL) (:36)) (NIL) (NIL) (NIL) (:38 :37 :39) G0043 etc.  
 LOCAL  
 ((:3 :2 :1) G0081 G0029 G0030 G0028) (:32 :33 :27 :26) G0 etc.  
 LOCAL  
 SMB  
 RESULTS  
 (BODY 1. IS :3 :2 :1)  
 (BODY 2. IS :32 :33 :27 :26)  
 (BODY 3. IS :28 :31)  
 (BODY 4. IS :20 :34 :19 :30 :29)  
 (BODY 5. IS :36 :35)  
 (BODY 6. IS :24 :5 :21 :4)  
 (BODY 7. IS :25 :23 :22)  
 (BODY 8. IS :14 :13 :15)  
 (BODY 9. IS :10 :16 :11 :12)  
 (BODY 10. IS :17 :18 :9)  
 (BODY 11. IS :7 :8)  
 (BODY 12. IS :38 :37 :39)  
 NIL

RESULTS FOR MOMO

Most of the scenes contain several "nasty" coincidences: a vertex of an object lies precisely on the edge of another object; two nearly parallel lines are merged into a single one, etc. This has been done on purpose, since a non-sophisticated pre-processor will tend to make this kind of error.

Example C. R3. Analysis by SEE gives

(BODY 1. IS X:2 X:1 X:4)  
 (BODY 2. IS X:6 X:5 X:3)

RESULTS FOR 'R3'

The % sign indicates the dextral scenes (cf. page 233). The signs may be ignored.

The Parts of SEE The program is straightforward; it does not call itself recursively; it does not do "pattern matching"; it does not do tree search. It is formed by several main parts, sequentially executed. They are

LINKS FORMATION. An analysis is made of vertices, regions and associated information, in search of clues that indicate that two regions form part of the same body. If evidence exists that two regions in fact belong to the same body, they are linked or marked with a "gensym" (both receive the same new label).\* There are two kinds of links, called strong (global) or weak (local).

Some features of the scene will weakly suggest that a group of regions should be considered together, as part of the same body. This part of the program is that which produces the 'local' links or evidences.

NUCLEI CONSOLIDATION. The 'strong' links gathered so far are analyzed; regions are grouped into "nuclei" of bodies, which grow until some conditions fail to be satisfied (a detailed explanation follows later).

Weak evidence is taken into account for deciding which of the unsatisfactory global links should be considered satisfactory, and the corresponding nuclei of bodies are then joined to form a single and bigger nucleus.

BODY RETOUCHING. If a single region does not belong to a larger nucleus, but is linked by one strong evidence to another region, it is incorporated into the nucleus of that other region. If necessary, more nuclei consolidation could be done after this step.

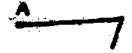
A last attempt is done to associate the remaining single regions to other bodies.

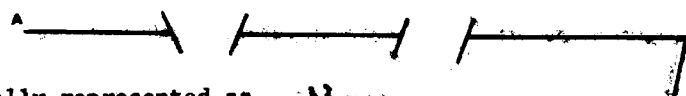
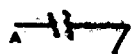
The regions belonging to the background are screened out, and the results are printed.

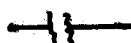
\* In LISP, a "gensym" (generated symbol) is a new Atomic symbol, previously unused.


Auxiliary Routines

Three functions are used constantly, and will be described now.

THROUGHTES "Through a chain of T's." Allows properties or configurations to extend along straight lines; for instance, the property <<'A' has as neighbor an L>>  can be extended so as to say <<throughtes, 'A' has as neighbor an L>>.

 schematically represented as 

Strict definition.  is defined as one of

(1) • (meaning the two vertices in both sides of  are in fact the same).

(2)   
matching T's

(3) 

(4) 

Example of  See also annotations on listing.

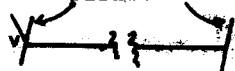
GOODT If a vertex  $V$  is considered a "good T", (GOODT  $V$ ) is TRUE; false otherwise.

(GOODT  $V$ ) = F if  $V$  is not a "T"

F if  background.

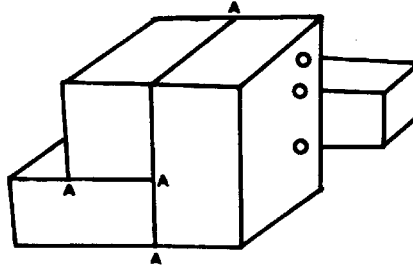
T if  $V$  has a NEKTE.

F if 

F if 

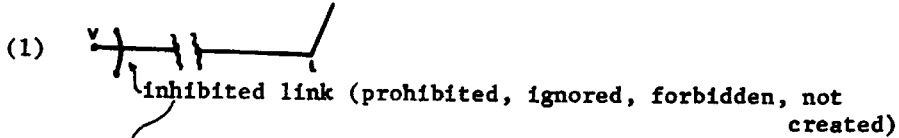

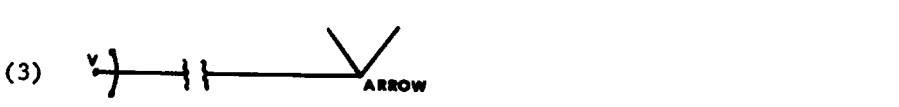


T otherwise.

As we see, this function tries to distinguish between T's originated by occlusion, such as O, and T's originated by accident (A).



NOSABO "Not same body." Acts as a link inhibitor.

If consulted, (NOSABO .. V ..) will inhibit, in the following conditions, the link that vertex V may have created:

- (1)  inhibited link (prohibited, ignored, forbidden, not created)
- (2)  GOODT
- (3)  ARROW
- (4)  PEAK
- (5)  K

Nosabo tries to find conditions indicating that two regions should not be considered as part of the same body; hence, if consulted, Nosabo may forbid a link among them. Some heuristics place links without asking Nosabo's approval and Nosabo can not "erase" a link placed without its authorization.

If none of conditions (1) to (5) is met, Nosabo will be False, indicating no inhibition was found, and it is up to the program that asked Nosabo's opinion to lay or fail to lay the link in question.


We proceed now to explain in considerable detail each of the parts of SEE. This will help the reader to understand the behavior of the program, its strengths and deficiencies.


## LINK FORMATION

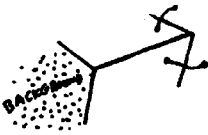

Several subroutines are devoted to creating weak and strong links. See also Listing.

CLEAN Removes several unwanted properties.

EVERTICES Each vertex is considered under the following rules:

L.-  No evidence is *created* directly by this type of vertex. Nevertheless, the "L" is used in many combinations with other vertices to account for evidence. As we saw, Nosabo uses L's. "Legs" will use them, too.

FORK.-  == No link is *created* if any of the three regions is background (but see below).  
Example (unless otherwise indicated, all examples are from figure 'BRIDGE' page 94): Vertex J does not generate links.  
== Otherwise, three links are *created* as shown, except that each one may be inhibited by Nosabo.  
Example. Vertex JB only produces link :5-:8. Link :5-:9 is inhibited because S is a 'T'; Nosabo also forbids link :8-:9 because KB is an 'arrow'. This last rule is the most powerful of the heuristics.

 == Two links are *created* as shown, without asking Nosabo, if the fork is connected to the central line of an arrow. (No link is put here )  
Example: In fig. R19, PA generates links :29-:17 and :35-:17.

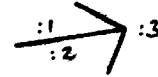
This last heuristic is of help where there are concave objects (Fig. R19).

ARROW.-



== Link if an L is connected to its central line, and the region shaded contains only that arrow as a "proper-arrow," and no Forks.

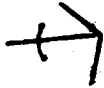
Region :1 contains arrow A as a "proper-arrow"; also



region :2, but not region :3. Capisce?

Example. BB links:10 with :4.

Allows "lateral faces" of legs to be properly identified and agglutinated.



== Otherwise, link except if inhibited by Nosabo.

Example. D lays a link between :26 and :23.

Powerful and general heuristic,

X.-



== No link if the X comes from the intersection of two lines.



== Otherwise, link as shown except if Nosabo disagrees.

Example. G originates links :26-:22 and :21-:30; this last one will later be erased or disregarded, since :30 is the background.

K.-



== No link.

PEAK.-



== Links are established between contiguous regions, except those to the region containing the angle bigger than 180°. These links are subject to Nosabo inhibition.

Example. In fig. 'CORN', JJ generates links :8-:9 and :9-:10.

Of certain use, specially with pyramids and "pointy" objects.

MULTI.-



== No link.

The reason is:

(1) if the vertex is "genuine" (cf. page 44),



although it *generates* no links, the object having it will probably possess many other vertices, through which links will get established, and

(2) if the vertex is "false" because is the result of the casual coincidence of two or more genuine vertices, mistakes are avoided by abstaining of *generating* links. This is generally the case.

An improvement is possible, by allowing MULTI vertices to place links.

**SUGGESTION**

T.-

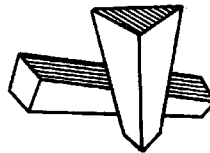


== If matching T's, link as shown, without consulting Nosabo, Avoid linking to the background. Each pair of matching T's produces these links only once; that is, we do not produce two links while analyzing A and another two at B.

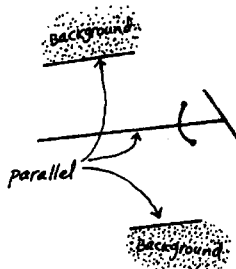


== Do not link if the middle region of a 'T' is the background.

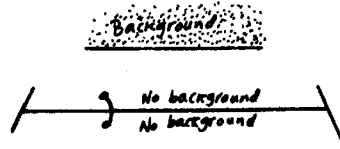
What we are trying to do here is to find places where a body appears as two disconnected parts.



== Link (without Nosabo's consent) as shown if the central segment of the 'T' separates two non-background regions, and these have the background as neighbor, and part of the separations between background and no-background are parallel to the central segment of the 'T'.



Avoid double links in the following case (link just once):



Example. TA links :21 with :27 (F-G, RA-TA and JA-IA are parallel).

Favors occluded bodies with parallel faces.

== Also, see "STUDY" in listing, still an experimental feature.

== Two links are placed as shown (without asking Nosabo) if the central line of the T is connected to the central line of an arrow. It is of help where there are concave objects.

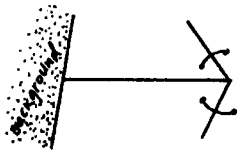


Table 'Global Evidence' shows compactly the main rules just discussed.

LOCALEVIDENCE

Weak or local links are laid here; they are used to indicate, in a feebler way, that two faces or regions may be part of the same object.

Nosabo can not inhibit local links.



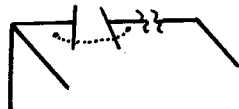
== A weak link is placed as shown (dotted) if, through a vertex, an L is connected to an Arrow, and the two indicated edges are parallel.

We call this configuration 'Leg'.

Example (all examples from figure 'BRIDGE', except if counterindicated). Vertex FA is a Leg (FA - QB is parallel to EA - DA) that links weakly :18 with :19.

== In a Leg, if there are two matching T's as shown, a weak link is placed correspondingly.

Example. In fig. 'TRIAL' (page 88), a weak link or evidence is placed between :7 and :4, because EE is a Leg, and L and E are matching T's.



The heuristics described will sometimes produce a "wrong linkage," linking two regions that do not belong to the same body. These mistakes are not likely to confuse SEE, since the handling of these links (and all of SEE, in general) is done under the assumption or knowledge that the information is noisy and somewhat unreliable.

Strong links are shown dotted; weak links are not shown.

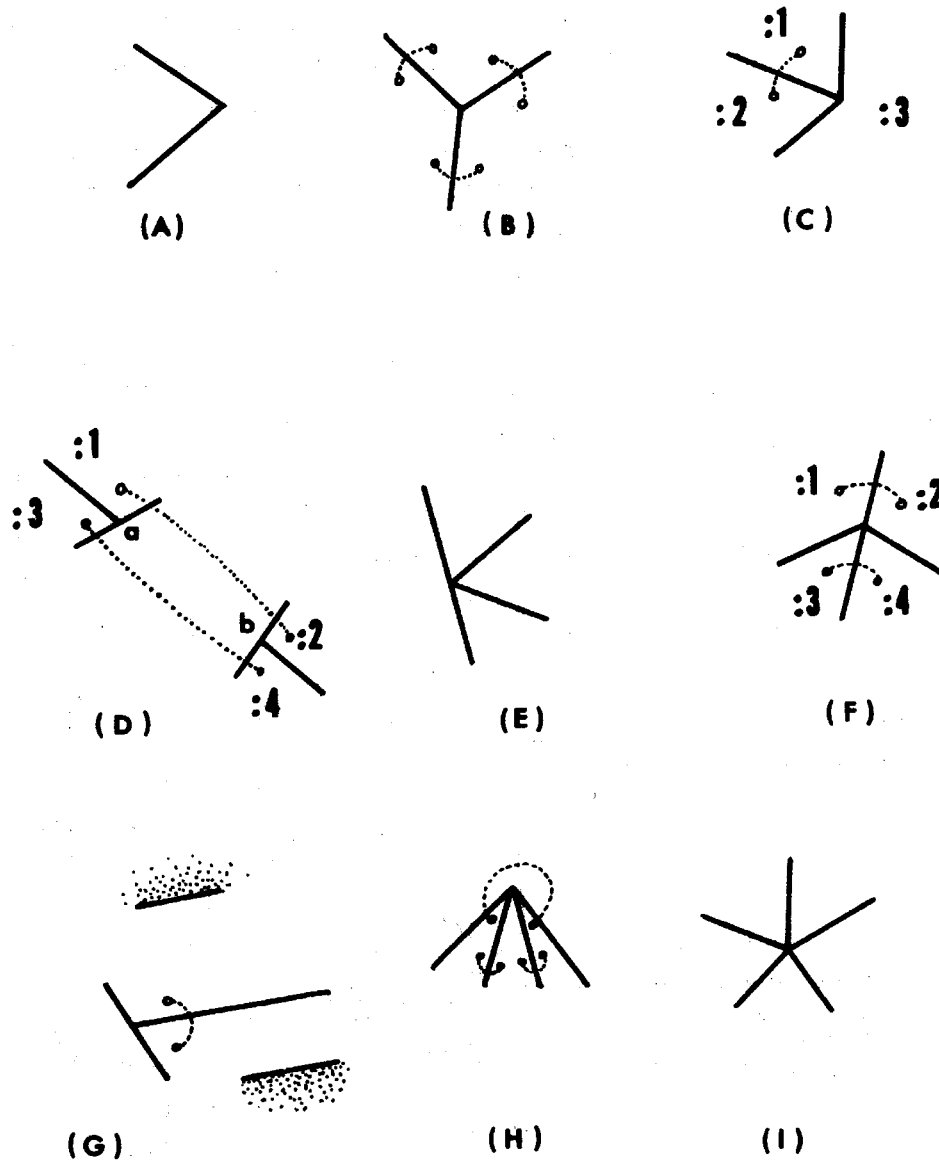
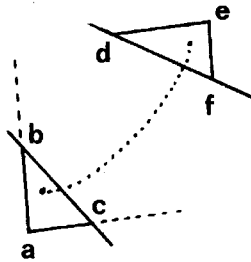


TABLE 'GLOBAL EVIDENCE'

TRIANGLE.-



== A Triangle is a 3-vertex region, of which two are interconnected T's, the type of the other vertex being irrelevant.  
 Two triangles are weakly linked if they are  
 (1) "facing each other", and  
 (2) "properly contained", meaning that D has to fall on the same side of AB as C does, and similarly for the other vertices, and  
 (3) AB is parallel to EF, and AC to DE.

The heuristic helps with faces of a prism that is badly obscured. It does not help much, since it gives only a weak link. On the other hand, this weakness prevents mistakes when the two triangles are not from the same body.

**SUGGESTION**

A possible improvement consists of choosing the closest of two triangles, if several candidates are possible.  
 Example. In figure 'WRIST' (page 136), weak links are placed between triangles 5 and 6, and between 1 and 2.

Example. Figure 'TRIAL' receives the following strong links (full lines) and weak links (dotted lines)

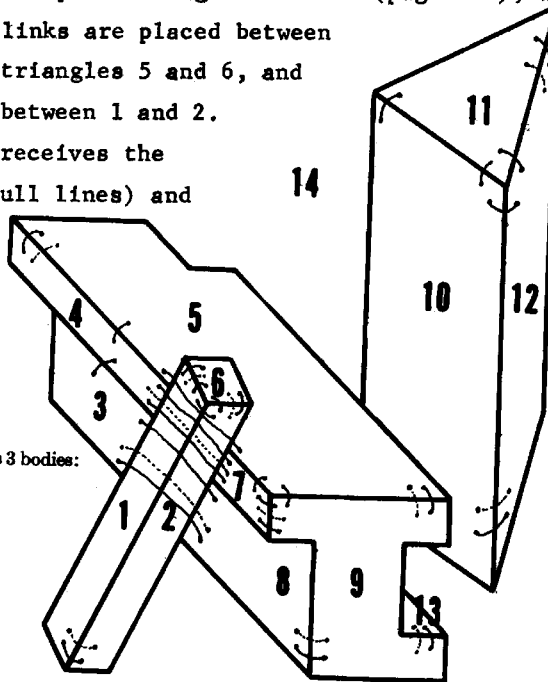


FIGURE TRIAL

The program analyzes this scene and finds 3 bodies:

- (BODY 1 IS :6 :2 :1)
- (BODY 2 IS :11 :12 :10)
- (BODY 3 IS :4 :9 :5 :7 :3 :8 :13)

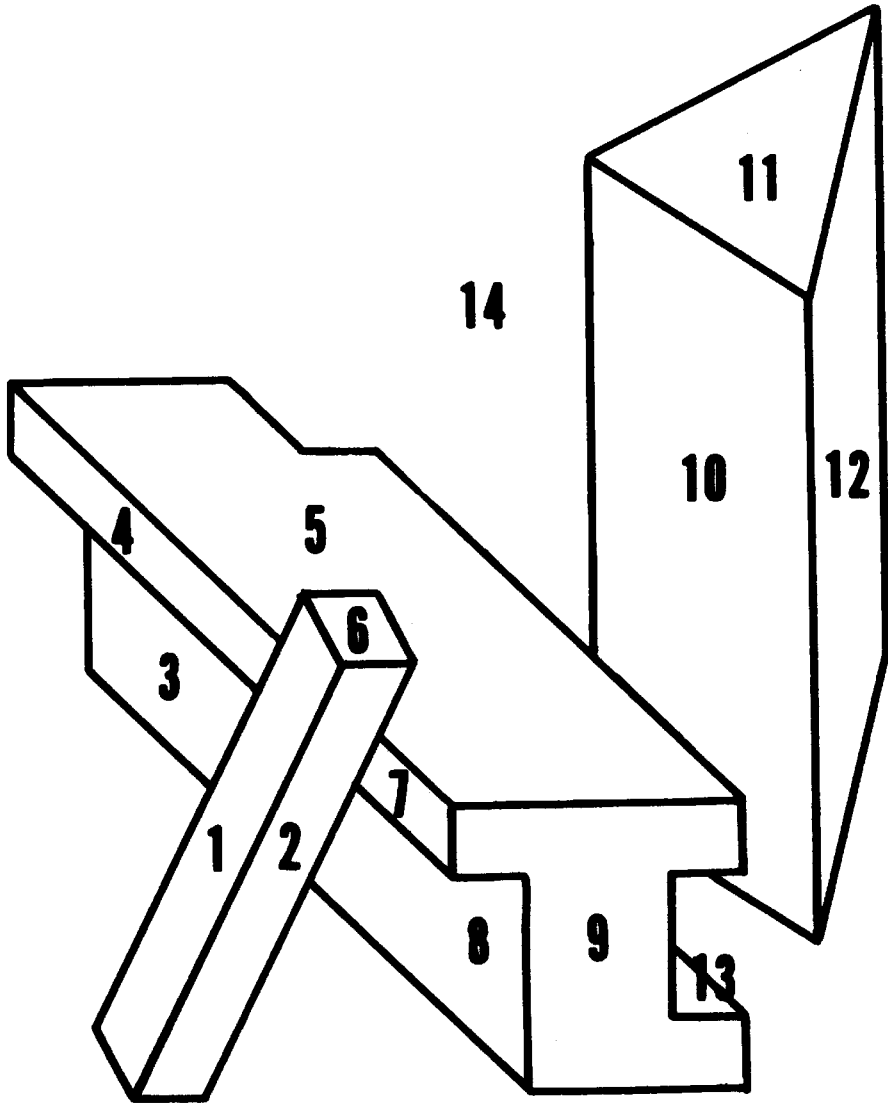


FIGURE 'TRIAL'

The links could be represented as

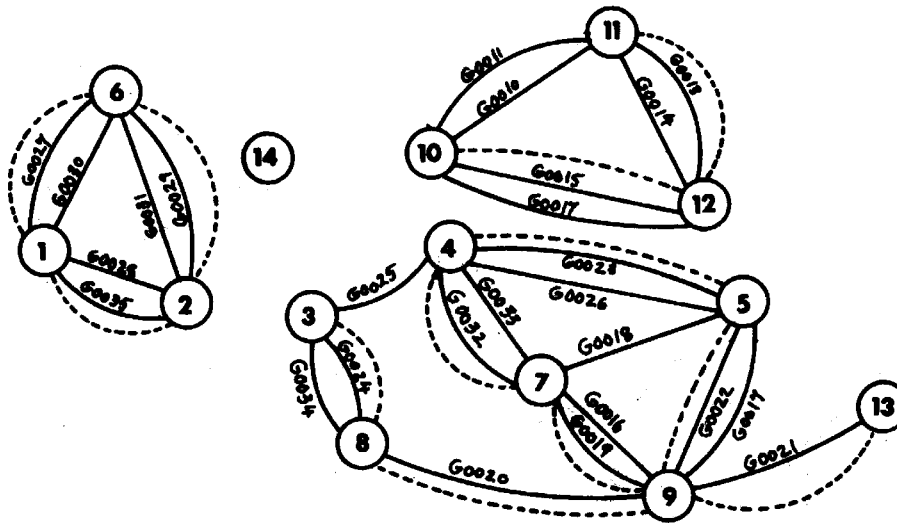


Figure 'TRIAL - LINKS'

Strong (solid) and weak (broken lines) links of figure 'TRIAL'.

SEE prints these links in the following way: (cf. also p. 110):

:11 has four <sup>strong</sup> links emanating from itself.

```
((NIL) ((:11) G0014 G0013 G0011 G0010) (
(:12) G0015 G0014 G0013 G0012) ((:13) G0
021) ((:9) G0022 G0021 G0020 G0019 G0017
G0016) ((:10) G0015 G0012 G0011 G0010)
(:3) G0034 G0025 G0024) ((:4) G0033 G00
32 G0026 G0025 G0023) ((:6) G0031 G0030
G0029 G0027) ((:5) G0026 G0023 G0022 G00
18 G0017) ((:7) G0033 G0032 G0019 G0018
G0016) ((:8) G0034 G0024 G0020) ((:2) G0
035 G0031 G0029 G0028) ((:14)) ((:1) G00
35 G0030 G0028 G0027))
```

Strong Links of 'TRIAL'

Weak links of scene 'TRIAL' are

```
((:2 :1) (:6 :2) (:6 :1) (:4 :5) (:9 :5)
(:13 :9) (:3 :8) (:9 :8) (:4 :7) (:9 :7)
) (:12 :10) (:11 :12))
```

Weak links of 'TRIAL'.

There is a weak link between :12 and :10

The next step is to gather all this evidence and to form tentative hypotheses of objects as assemblages of faces with many links among them.

#### NUCLEI CONSOLIDATION

All the links to the background are deleted, since it can not be part of any body.

Strong and weak links exist among the different regions of a scene. They are consolidated in that order by two subroutines, Global and Local.

GLOBAL Groups of faces with an abundance of strong links among them are first found; these "nuclei" will later compete for other faces more loosely linked.

Definition: a nucleus (of a body) is either a region or a set of regions that has been formed by the following rule.

Rule: If two nuclei are connected by two or more strong links, they are merged into a larger nucleus.

More detailed rules appear in page 25 , in section 'Simplified view of Scene Analysis'.

For instance, in the figure below, regions :1 and :2 are put

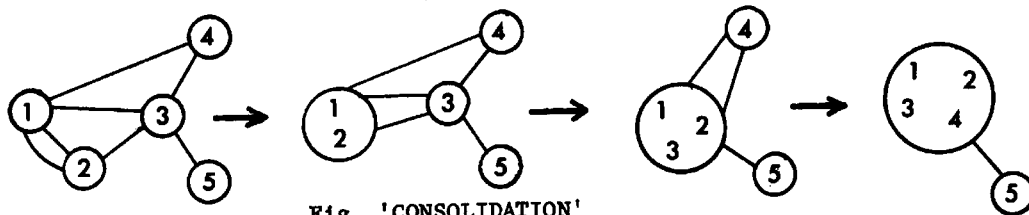


Fig. 'CONSOLIDATION'  
Two links between two nuclei merge them.

together, because there exist two links among them, to form nucleus :1-2. Now we see that region :3 has two links with this nucleus :1-2, and therefore the new nucleus :1-2-3 is formed.

We let the nuclei grow and merge under the former rule, until no new nuclei can be formed.

When this is the case, the scene has been partitioned into several "maximal" nuclei; between any two of these there is at most one link. For example, figure 'TRIAL-LINKS' will be transformed into figure 'TRIAL-NUCLEI'.

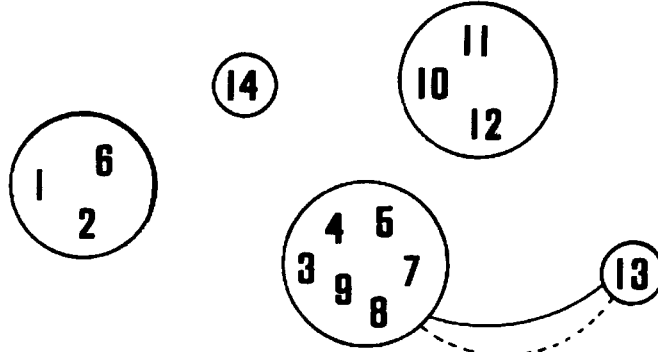


Figure 'TRIAL - NUCLEI'  
Maximal nuclei of scene TRIAL.

LOCAL If some strong link joining two "maximal" nuclei is also reinforced by a weak link, these nuclei are merged.

The weak links of figure TRIAL are shown as dotted lines in figure 'TRIAL-LINKS' (page 90); they transform figure 'TRIAL-NUCLEI' into figure 'TRIAL-FINAL'.

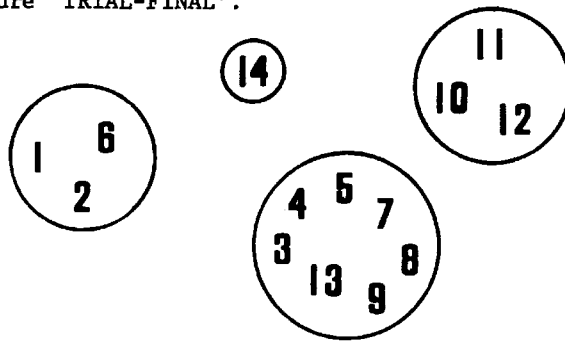


Figure 'TRIAL - FINAL'  
Nuclei of scene TRIAL after merging  
suggested by local links.

#### BODY RETOUCHING

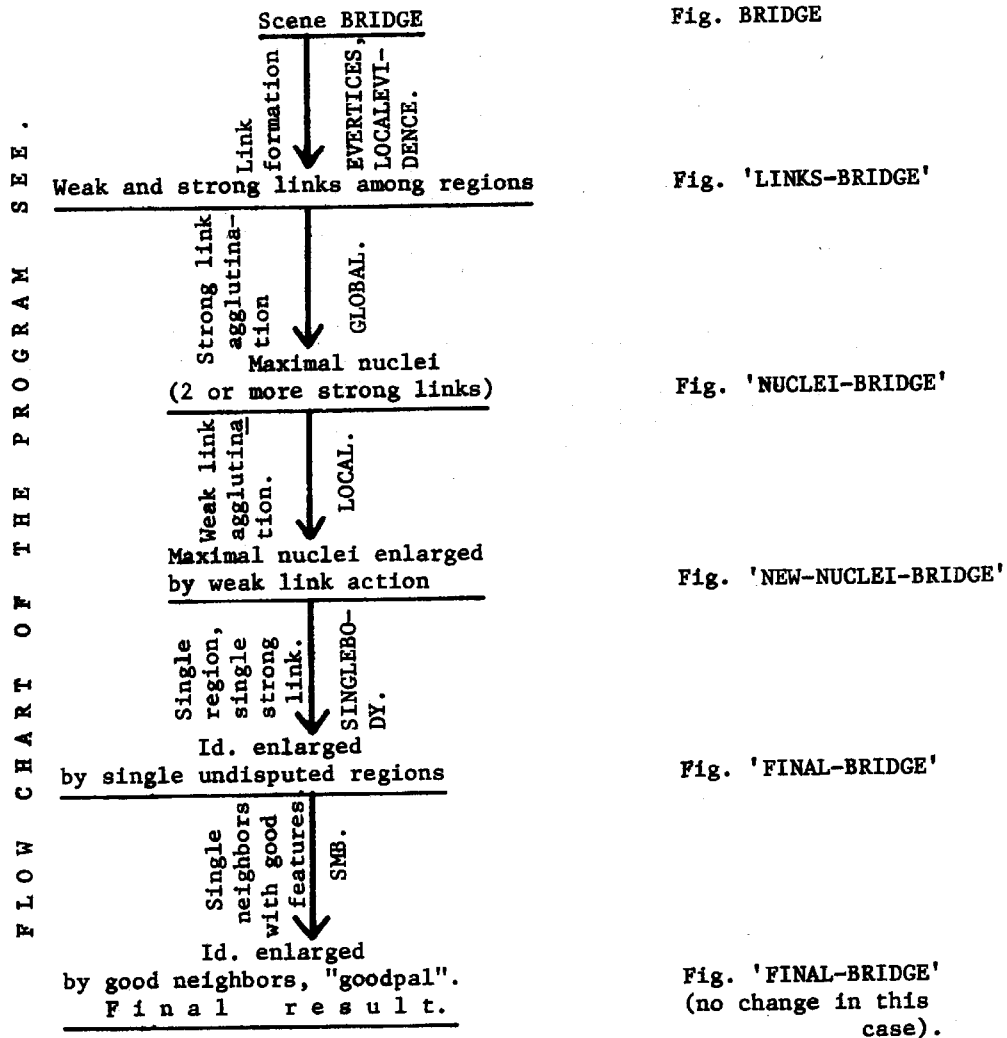
Additional heuristics assign unsatisfactory faces to existing nuclei, or isolate them. SINGLEBODY and SMB are used for this task.



SINGLEBODY A strong link joining a nucleus and another nucleus composed by a single region is considered enough evidence to merge the nuclei in question if there is no other link emanating from the single region. A message is printed indicating these merges.

Such rules produce no change in fig. 'TRIAL-FINAL', and therefore its nuclei will be reported as bodies.

A more complex example shows the retouching operation. Figure 'BRIDGE' undergoes these transformations:



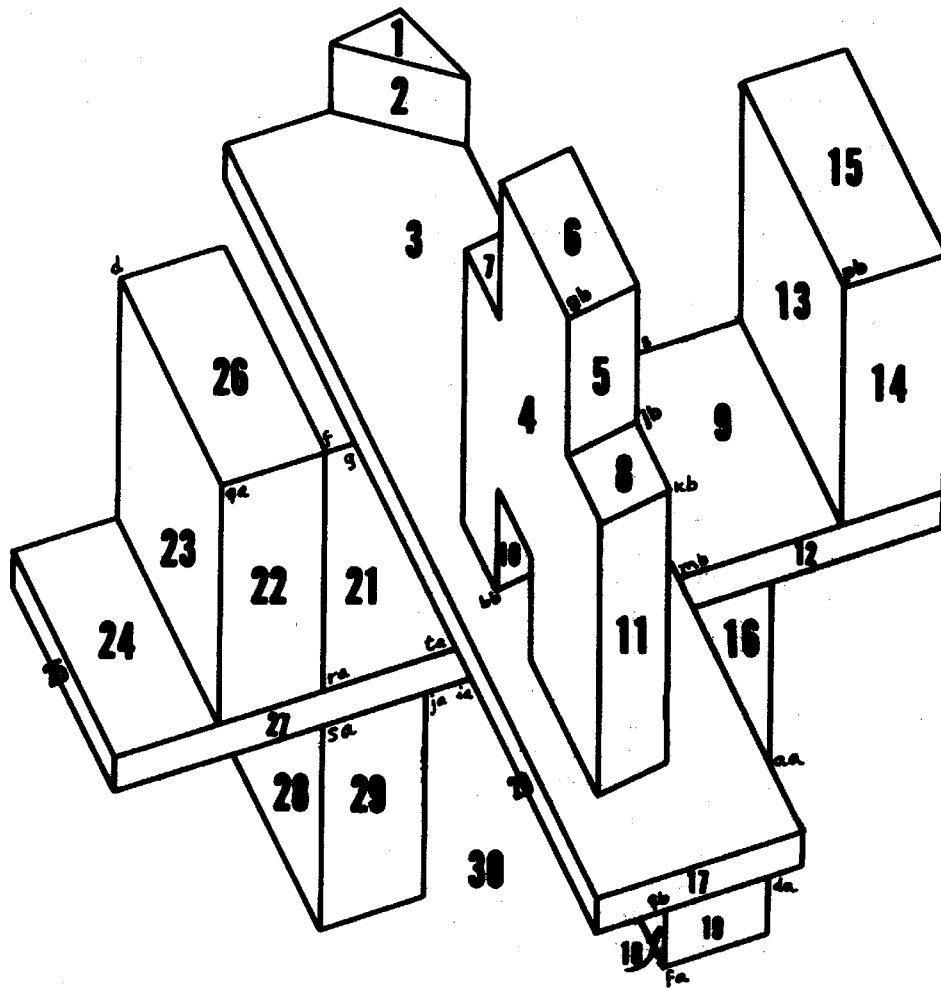


FIGURE 'BRIDGE'

FIGURE 'LINKS-BRIDGE'

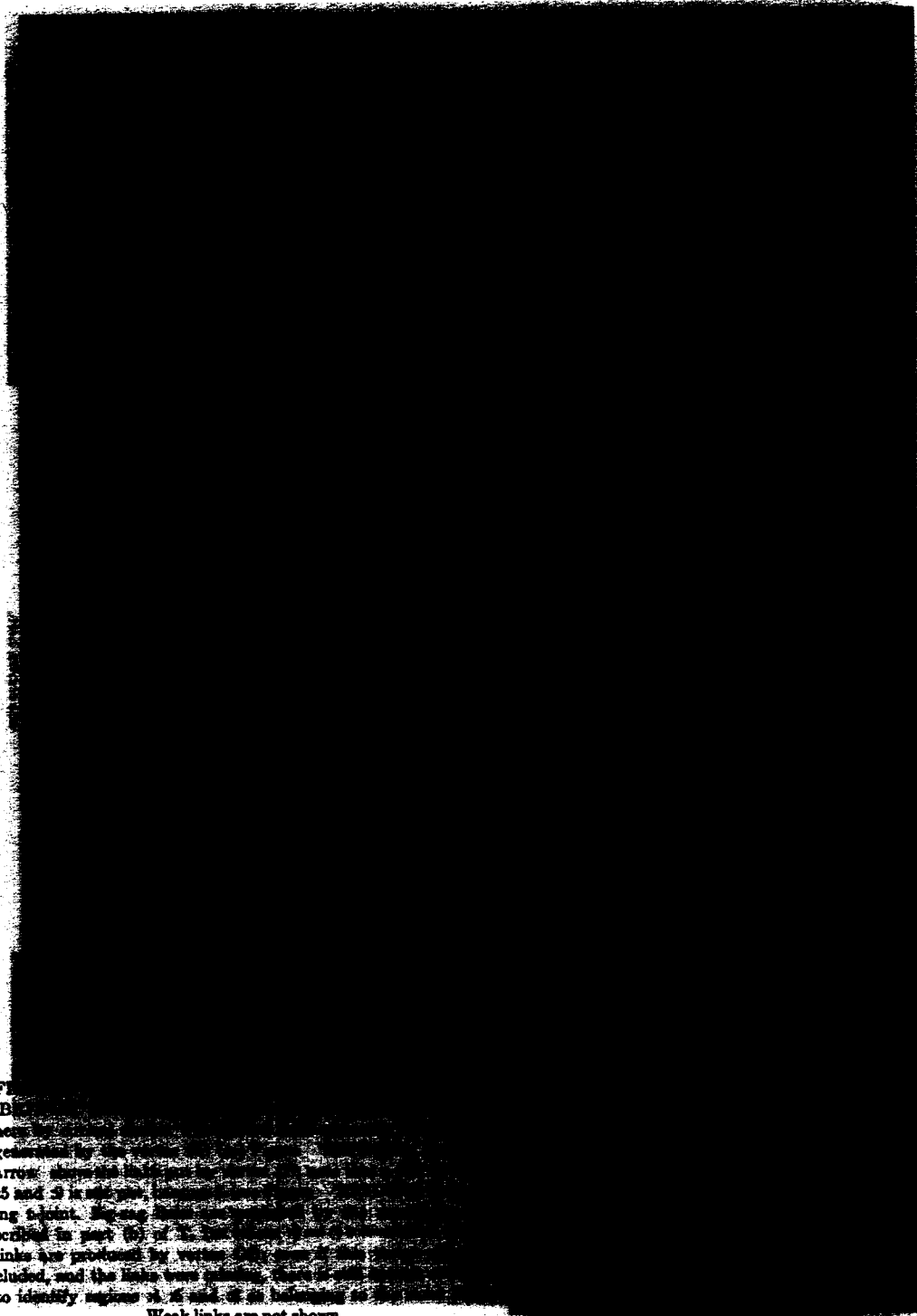
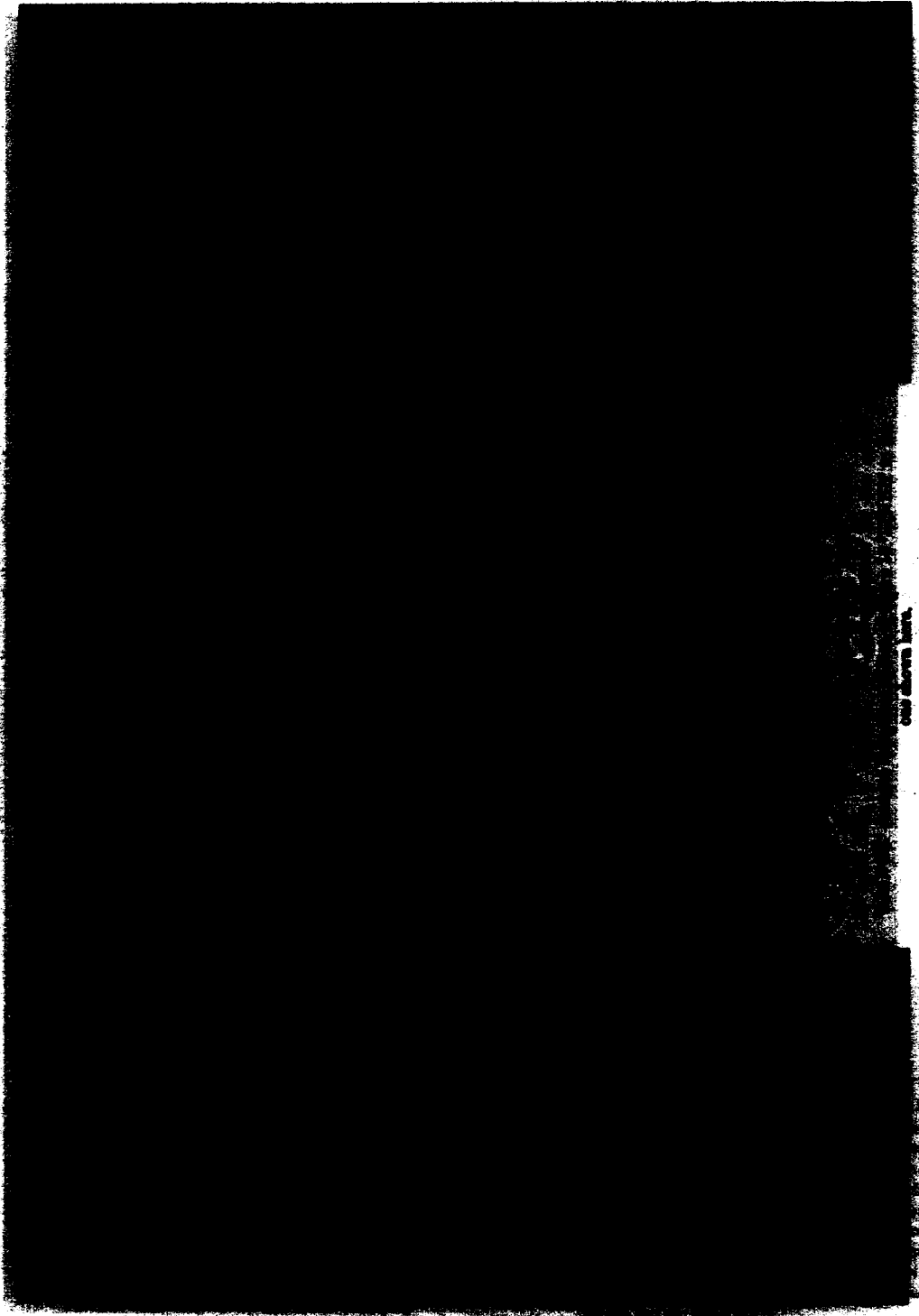
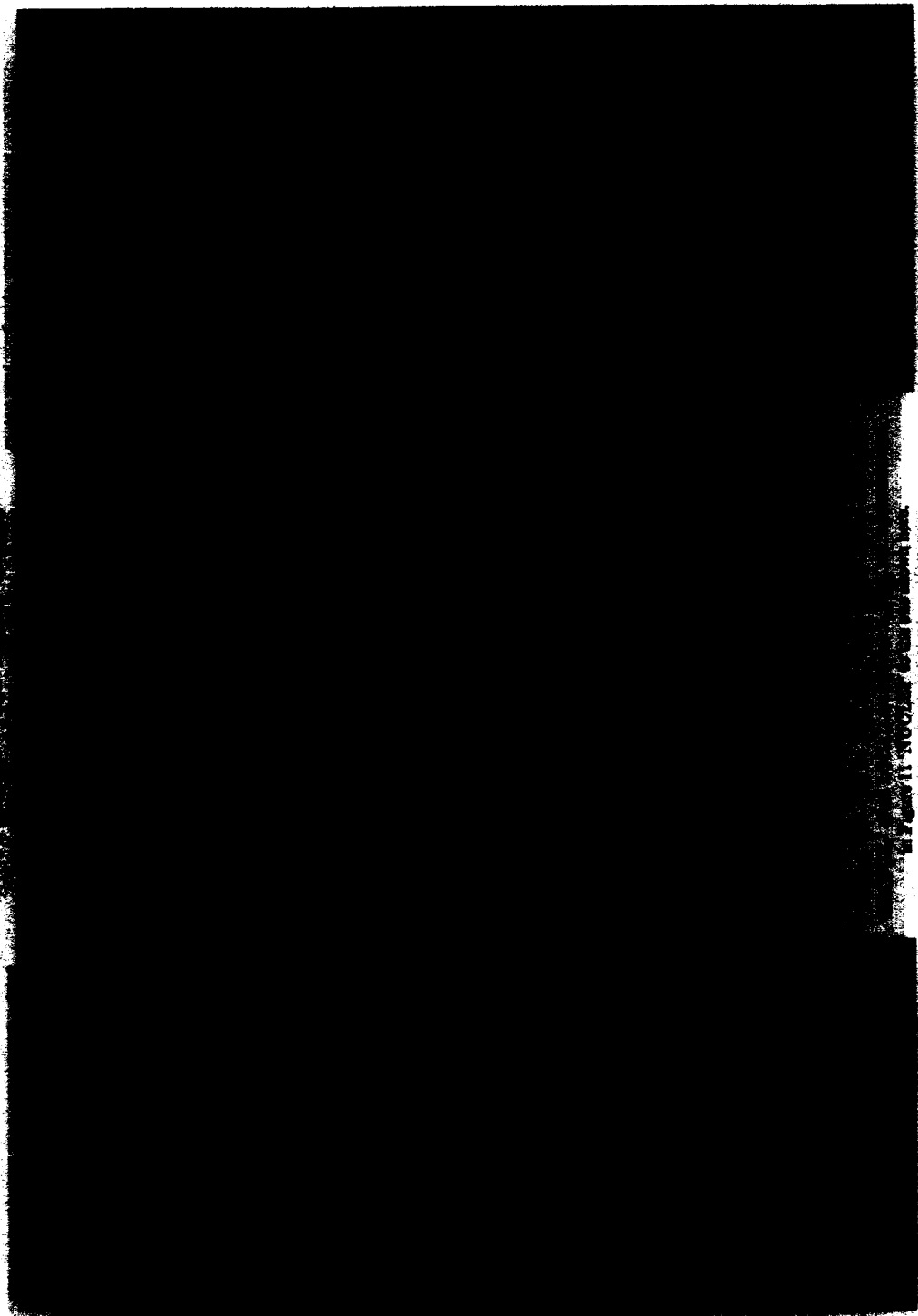
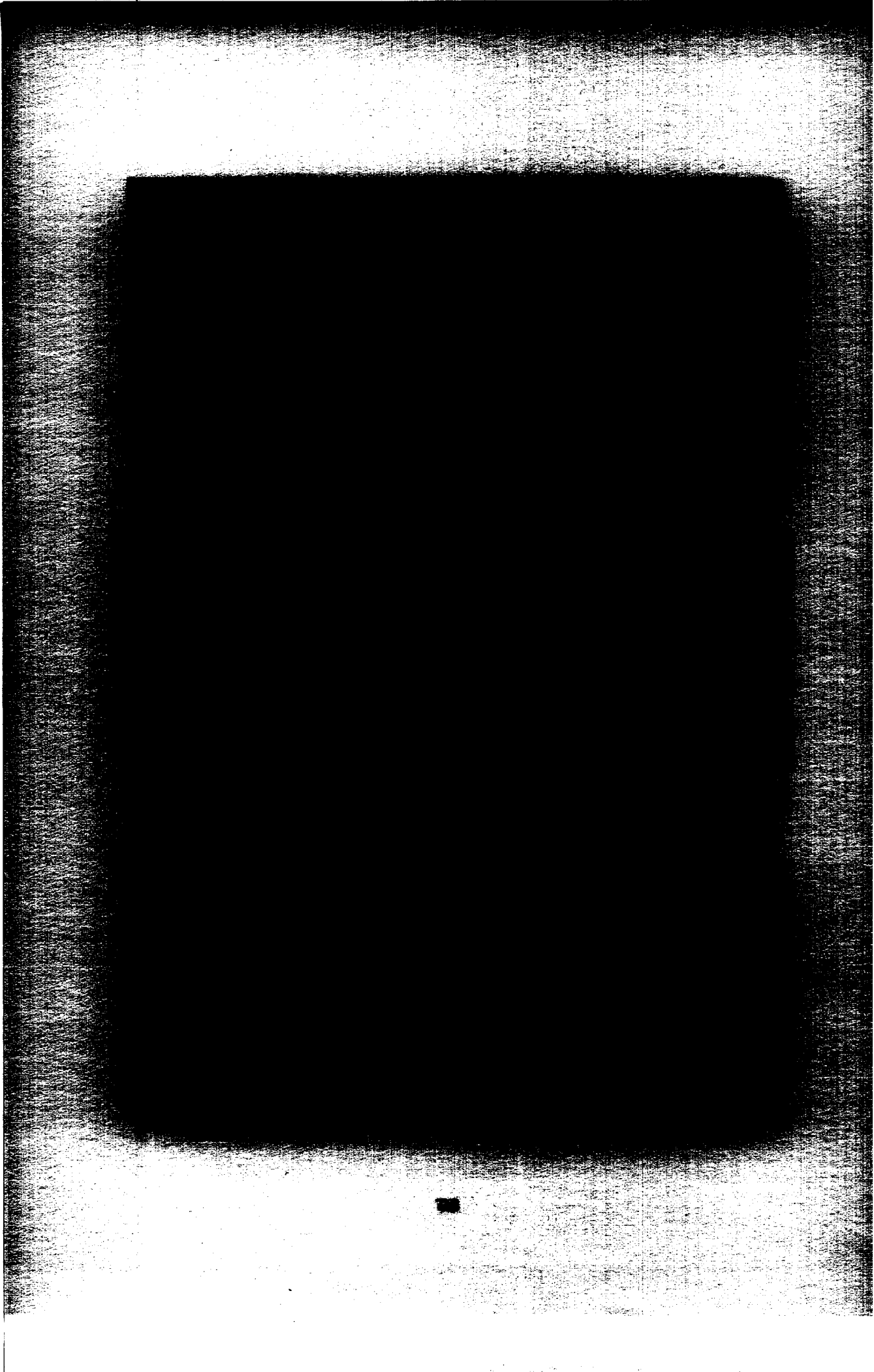


FIGURE 'NUCLEI - BRIDGE'







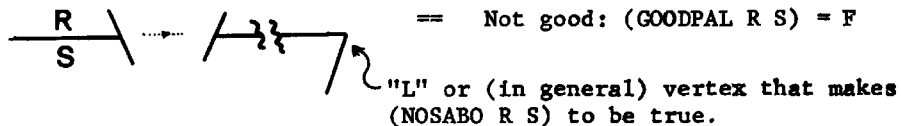
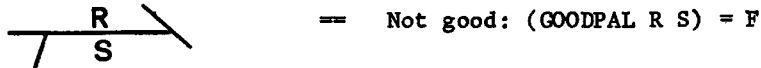
We see that in figure 'NEW-NUCLEI-BRIDGE', nucleus :16 is merged by SINGLEBODY with nucleus :18-19 (see figure 'FINAL-BRIDGE'). Nucleus :28-29 is not joined with :26-22-23 or with :24-25-27-12-21-9. Even if nucleus :28-29 were composed by a single region, still will not be merged, since two links emerge from it: two nuclei claim its possession.

This rule joins single regions having only one possible "owner" nucleus.

SMB Two systems of links are used by SEE. One consists of weak and strong links, produced by examining each vertex, and culminates forming nuclei under GLOBAL, LOCAL, etc.

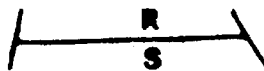
The second system constitutes a different network of links; SMB works in the second system. It is motivated by the desire to collect evidence not directly available through the vertices. It gathers evidence from the lines or boundaries separating two regions, in an effort to answer the question: Are two given neighboring regions part of the same object, or are not they? That is, are two contiguous regions "good neighbors" ("good'pals")? If they are, a special link, s-link, is placed, eventually forming a network independent of weak and strong links, that will collapse in a somewhat peculiar way. Thus, a great amount of unnecessary duplication could be possible in the information carried by both systems of links. To reduce it, the s-links are designed to complement and extend, rather than to re-do, the agglutination produced by weak+strong links. They (the s-links) will, therefore, mainly study single faces not satisfactorily accounted for.

SMB uses the predicate (GOODPAL R S), which acquires the value T (true) if R and S are two contiguous "good neighbors" regions. To satisfy this, their common boundary must not be empty, and must lack L's, FORKS, ARROWS, K's, X's, PEAKs, MULTIs. In addition:



== O. K. otherwise: (GOODPAL R S) = T.

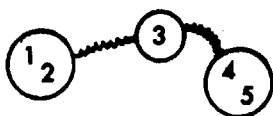
In particular,



is O. K. if (NOSABO R S) = F.

SMB analyzes the nuclei formed under weak+strong links that, after SINGLEBODY actuation, still remain formed by a single face or region. The steps are:

1. A network of s-links is formed by putting a s-link between regions forming a nucleus all by themselves, and their goodpal neighbors.
2. If exactly one nucleus is s-linked to one of those regions (that is to say, if such single-region single-nucleus has precisely one good-pal), the region gets absorbed by the nucleus; otherwise the region is reported as a body in itself (consisting of a single region)



does not change because :3 has two s-links.

Note that

- a. The s-links are not used to form nuclei as the weak+strong links were; they only help certain isolated faces to join bigger structures.
- b. Two s-links between two regions have the effect of one.

Example. In figure 'HARD', regions :6 and :7 get joined by SMB.



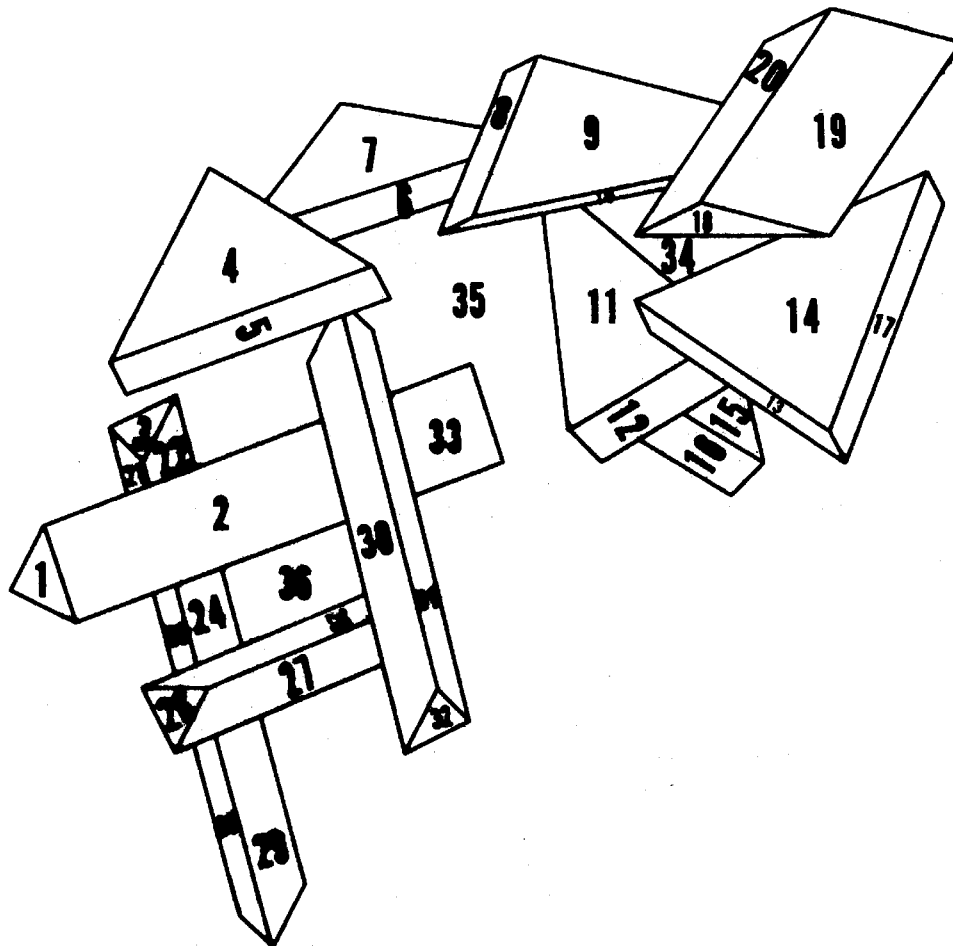


FIGURE 'H A R D'  
This scene shows the use of SPB.

SEE 58 ANALYZES HARD

EVIDENCE

LOCALEVIDENCE

TRIANG

GLOBAL

((NIL) ((:34)) ((:6)) ((:36)) ((:24) G0026 G0025 G0023 G0 etc.  
0044 G0043 G0042) ((:17) G0047 G0046 G0045 G0044) ((:17)) etc..  
0041 G0039) ((:21) G0050 G0040 G0039 G0029 G0028 G0027) (...  
0038 G0036 G0019) ((:26) G0054 G0053 G0037 G0036) ((:27) ...  
G0055 G0023 G0020 G0015) ((:32) G0057 G0056 G0034 G0033)  
8 G0048) ((:4) G0058 G0048) ((:10) G0059 G0032 G0031) ((:  
:19) G0064 G0063 G0062 G0061) ((:20) G0064 G0062 G0060 G0  
:30) G0056 G0035 G0033 G0016) ((:15) G0066) ((:16) G0066)  
((NIL) ((:34)) ((:6)) ((:36)) (NIL) (NIL) (NIL) (NIL) ((:  
019 G0053 G0036 G0054 G0038 G0037 G0019) (NIL) ((:24 :22  
0040 G0039 G0029 G0028 G0027 G0024 G0022 G0055 G0023 G002  
) (NIL) ((:5 :4) G0048 G0058 G0048) (NIL) ((:13 :17 :14) :  
:18 :19 :20) G0060 G0064 G0063 G0061 G0064 G0062 G0060 G0  
:32 :31 :30) G0033 G0057 G0034 G0056 G0035 G0033 G0016) (

LOCAL

(LOCAL ASSUMES (:11) (:12) SAME BODY)

(LOCAL ASSUMES (:15) (:16) SAME BODY)

((NIL) ((:34)) ((:6)) ((:36)) (NIL) (NIL) ((:7)) (NIL) (N  
019) ((:24 :22 :3 :23 :21 :28 :29) G0020 G0026 G0025 G004  
0055 G0023 G0020 G0015) ((:1 :2 :33) G0052 G0051 G0017 G0  
43 G0047 G0046 G0044 G0047 G0045 G0043 G0042) (NIL) ((:18  
:10 :8) G0032 G0032 G0065 G0059 G0031 G0030) ((:32 :31 :  
) (NIL) ((:35)) ((:12 :11) G0067) (NIL))

LOCAL

((:12 :11) G0067) ((:16 :15) G0066) ((:32 :31 :30) G0033  
G0065 G0059 G0031 G0030) ((:18 :19 :20) G0060 G0064 G0063  
6 G0044 G0047 G0045 G0043 G0042) ((:5 :4) G0048 G0058 G00  
3 :21 :28 :29) G0020 G0026 G0025 G0049 G0041 G0021 G0050 ( :  
15) ((:25 :26 :27) G0019 G0053 G0036 G0054 G0038 G0037 G0

LOCAL

SMB

(SMB ASSUMES :7 :6 SAME BODY)

RESULTS

(BODY 1. IS :12 :11)

(BODY 2. IS :16 :15)

(BODY 3. IS :32 :31 :30)

(BODY 4. IS :9 :10 :8)

(BODY 5. IS :18 :19 :20)

(BODY 6. IS :13 :17 :14)

(BODY 7. IS :5 :4)

(BODY 8. IS :1 :2 :33)

(BODY 9. IS :24 :22 :3 :23 :21 :28 :29)

(BODY 10. IS :25 :26 :27)

(BODY 11. IS :7 :6)

NIL

RESULTS FOR HARD

RESULTS. After having screened out the regions that belong to the background, the nuclei are printed as "bodies".

In this process, the links which may be joining some of the nuclei are ignored: RESULTS considers the links of figure 'FINAL-BRIDGE', for instance, as non-existent. These links are the result of imperfections in the heuristics, mistakes in the placement of links, and may point out different parsings. An improvement to SEE will be to try to "explain" these residual links.

Summary SEE uses a variety of kinds of evidence to link together regions of a scene. The links in SEE are supposed to be general enough to make SEE an object-analysis system. Each link is a piece of evidence that suggests that two or more regions come from the same object, and regions that get tied together by enough evidence are considered as "nuclei" of possible objects.

Examples and discussion are in next section.

## ANALYSIS OF MANY SCENES

Until we have an adequate analytic theory, the behavior of a heuristic program is best understood with examples. There are several ways to go about this:

Simple In order to learn what a program does, simple examples, each one illustrating a single feature or group of features, are very appropriate.

Favorable A shiny impression of a set of routines is obtained by presenting 'favorable' cases, designed to enhance the characteristics of the program in front of the unsophisticated observer.

Of course, of all possible inputs, there is a subset that will produce outputs very pleasant in terms of speed, easiness of programming, generality, accuracy, or whatever other feature that system advertises. This subset tends to get the highlights in the descriptions.

Nasty Examples in which the program does particularly poorly are useful, if well chosen, to illustrate the weak points and pitfalls of the techniques used, the restrictions and constraints in the input, etc. They may point out improvements or extensions.

Silly Examples having very weak connection with the purpose or intention of the routines or algorithms discussed serve no useful end, except perhaps to point out that the maker of such examples did not understand the issues. For instance, one could take a box full of pins, drop them on the table, take their picture and ask SEE to work on it.

A collection of simple, favorable, and nasty examples follows. They are not in that order.

A discussion is found at the end of this section.

Stereo Scenes Analysis of stereographic pictures will be found in the section 'Stereo Perception'.

Finding the background Examples where the background is not known in advance and has to be deduced are given in the section 'Background Discrimination by Computer'.

LIST OF SCENES ANALYZED BY SEE IN THIS SECTION

P A G E

N a m e.	Comments. Scene (figure). Computer Results.		
R17	107	108	109
L3	110	111	112
R3	113	114	115
SPREAD	116	117	118
STACK	119	120	122
STACK*	119	121	122
L10	123	124	125
R10	126	127	128
TOWER	129	130	131
REWOT	132	133	134
WRIST*	135	136	137
L2	138	141	142
R2	138	139	140
L19	143	144	145
R19	146	147	148
CORN	149	150	151
L9	152	153	154, 155
R9	156	158	157
R9T	156	159	160
TRIAL	161	162	163
ARCH	164	165	166
HARD	167	168	169
L4	170	171	172
R4	173	174	175
MOMO	176	177	178
BRIDGE	179	180	181

Scene R17 The three prisms are found. In scenes like this, the position of one or two vertices may alter the analysis made by SEE, by changing radically the slope-direction of a small segment (such as KL and GH, figure 'R17'), killing several T-joints and separating regions :1-2 from :5-6.

Small errors in the coordinates of vertices K, L, G, H, and few others will drastically change the slope of segments of short length. This will transform G and K to be Arrows or Forks, so that G and K will no longer be matching T's (cf. also 'Conservatism and Tolerance' page 173). As a consequence, body :2-1 will be disconnected from body :5-6. This annoying problem is not difficult to correct, at preprocessor level, since there is good information about the slope of the (long) line BN: the slope of KL has to agree with the slope of BN, giving a good estimate of its true shape. The SUGGESTION rule seems to be that these short segments should be "re-oriented" if necessary, to agree with the longer ones, which are more reliable. Deeper analysis is found in section 'On Noisy Input'.

The preprocessor should consider the hypothesis SUGGESTION that BKLN are colinear -- or SEE should propose it for confirmation (see 'Division of Work in Computer Vision', p. 60).

The % signs In the printouts of some scenes, such as R17 (see 'RESULTS FOR R17' in page 109), a % sign appears as part of the name of every region and vertex; that is, %:3 instead of :3. This will be the case in all scenes having names starting with the letter R, differentiating the "right regions" from the "left regions". This will become clear in the section 'Stereo Perception', page 233; until then, disregard the %'s.

R 17

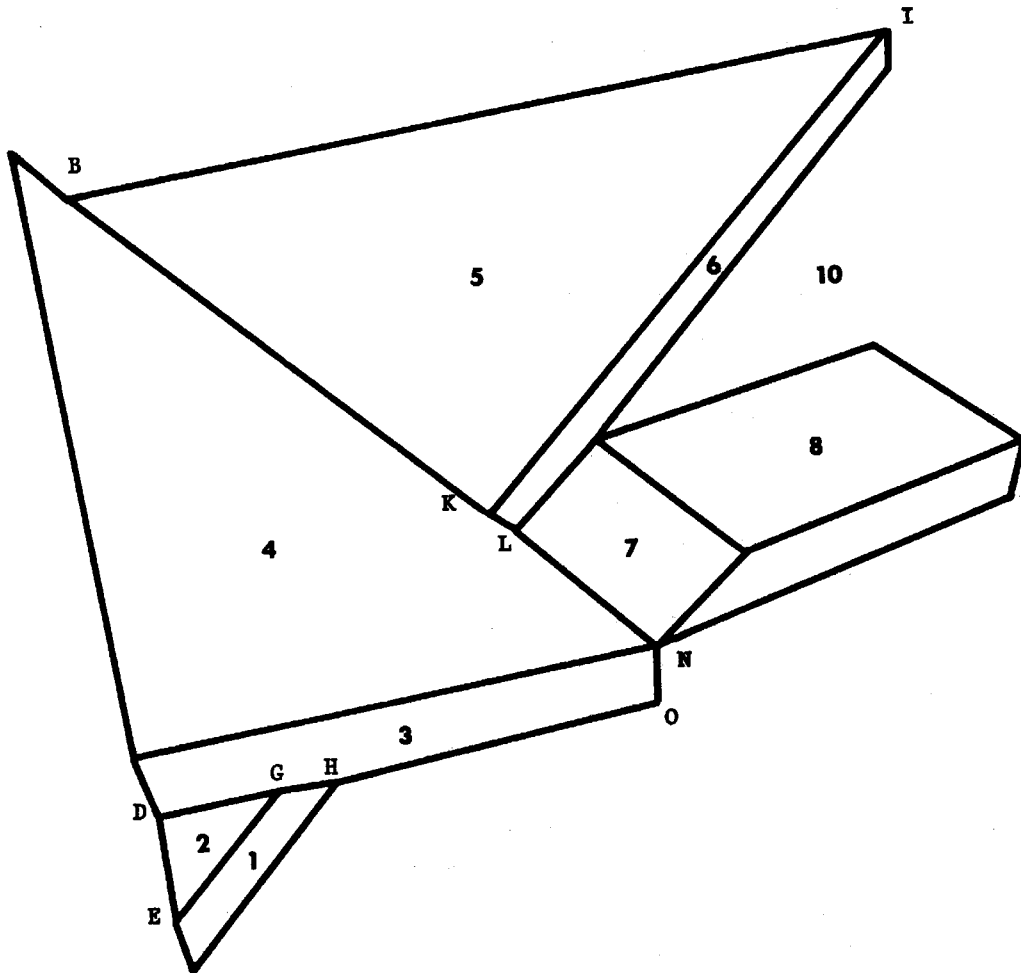


FIGURE 'R 1 7'

The three prisms were correctly found.  
There are several "nasty" coincidences  
in this scene, simulating the data  
that a not-too-satisfactory preprocessor  
will tend to provide.



SEE 98 ANALYZES R17  
 EVIDENCE  
 LOCALEVIDENCE  
 TRIANG  
 GLOBAL  
 (NIL) (X19) G0012 G0011 G0009 (X16) G0012 G0010 G0009 (X17) G0011 G0010 (X16) G0015 G0014 G0013 (X11) G0015 G0  
 013 (X12) G0016 (X13) G0017 (X15) G0016 G0014 (X14) G0017 (X19)  
 (NIL) (NIL) (NIL) (X19 X18 X17) G0012 G0009 G0011 G0010 (NIL) (X16 X11) G0014 G0015 G0013 (X12) G0016 (X13) G001  
 7 (X15) G0016 G0014 (X14) G0017 (X19)  
 LOCAL  
 (LOCAL ASSUMES (X16 X11) (X15) SAME BODY)  
 (NIL) (NIL) (X19 X18 X17) G0012 G0009 G0011 G0010 (X15 X16 X11) G0016 G0014 G0015 G0013 (X12) G0016 (X13) G0017)  
 (NIL) (X14) G0017 (X110))  
 LOCAL  
 (SINGLEBODY ASSUMES (X13) (X14) SAME BODY)  
 (SINGLEBODY ASSUMES (X15 X16 X11) (X12) SAME BODY)  
 (NIL) (X13 X14) G0017 (NIL) (X15 X16 X11 X12) G0016 G0014 G0015 G0013 (X19 X18 X17) G0012 G0009 G0011 G0010)  
 LOCAL  
 SMS  
 RESULTS  
 (BODY 1. 18 X13 X14)  
 (BODY 2. 18 X15 X16 X11 X12)  
 (BODY 3. 18 X19 X18 X17)  
 NIL

RESULTS FOR R 1 7

Scene L3 Without difficulty, two bodies are found. Each region contains four strong links relating it with other regions (see 'RESULTS FOR L3'). LOCAL is not needed to form nuclei; neither SINGLEBODY or SMB.

Explanation of the printout produced by the program In page 112, a printout of the results appears. The format is the same for every scene. It starts by saying

SEE 58 ANALYZES L3

which identifies the name of the program (SEE), its number (version number 58), and the scene to be analyzed (L3).

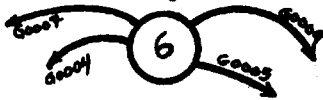
EVIDENCE  
 LOCALEVIDENCE  
 TRIANG  
 GLOBAL

The different sections of the program print their name, when they are entered.

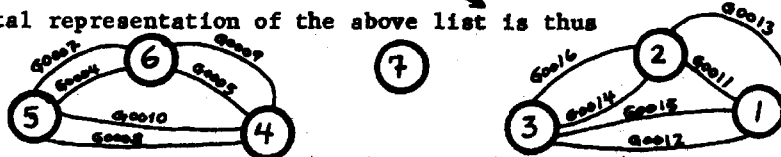
We then come to a list containing regions (such as :6) and 'gensyms' (such as G0009):

```
((NIL) ((:6) G0009 G0007 G0005 G0004) (:5) G0010 G0008
G0007 G0004) (:4) G0010 G0009 G0008 G0005) (:1) G0015
G0013 G0012 G0011) (:2) G0016 G0014 G0013 G0011)
(:3) G0016 G0015 G0014 G0012) (:7)))
```

This list contains the nuclei and the links (strong links); the first nucleus that we see is ((:6) G0009 G0007 G0005 G0004), meaning that from nucleus (or region) :6 emanate four links, namely G0009, G0007, G0005 and G0004. We can represent this graphically:



The total representation of the above list is thus



We then see "LOCAL" (when this function is entered, it prints its name), then the list of nuclei again, this time shrunk somewhat by LOCAL; finally, we see "RESULTS", and then 2 bodies, followed by NIL, meaning the end of the program. (See page 112).

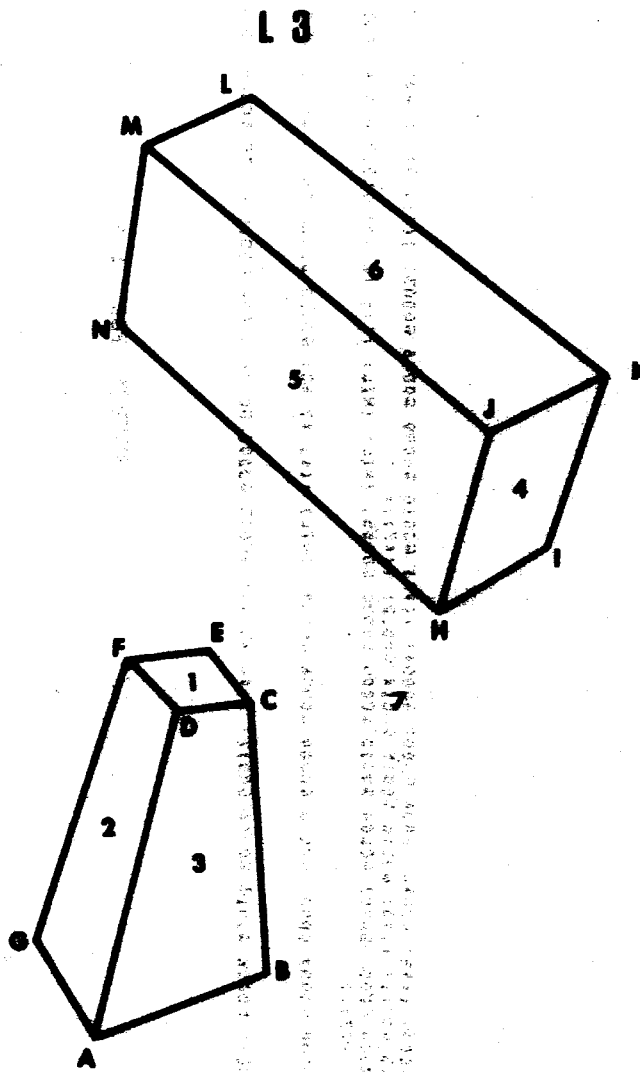


FIGURE 'L 3'

Two bodies are found in this scene by our programs.

In the input data it is indicated that region : 7 is the background.

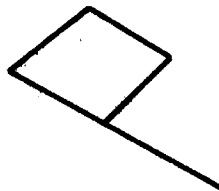
SEE 56 ANALYZES L3  
 EVIDENCE  
 LOCALEVIDENCE  
 TRIANG  
 GLOBAL  
 ((NIL)) ((18)) 50009 50007 50005 50004 ((15)) 50010 50006 50007 50004 ((14)) 50010 50009 50008 50005 ((11)) 50015 50013 50  
 012 50011 ((12)) 50016 50014 50013 50011 ((13)) 50016 50015 50014 50012 ((17))  
 ((NIL)) ((NIL)) ((NIL)) ((16 15 14)) 50005 50008 50007 50004 50010 50009 50008 50005 ((NIL)) ((11 12 13)) 50012 50014 5001  
 3 50011 50016 50015 50014 50012 ((17))  
 LOCAL  
 ((NIL)) ((NIL)) ((16 15 14)) 50005 50008 50007 50004 50010 50009 50008 50005 ((NIL)) ((11 12 13)) 50012 50014 50013 50011 5001  
 6 50015 50014 50012 ((17))  
 LOCAL  
 ((11 12 13)) 50012 50014 50013 50011 50016 50015 50014 50012 ((16 15 14)) 50005 50008 50007 50004 50010 50009 50008 5000  
 5))  
 LOCAL  
 SMB  
 RESULTS  
 (BODY 1. 16 11 12 13)  
 (BODY 2. 16 16 15 14)  
 NIL

RESULTS FOR L 3

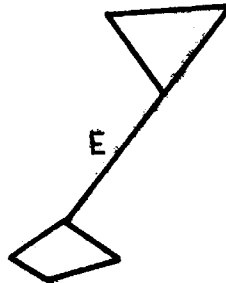
Scene R3 Two bodies are found in this scene. Vertex F is classified as of type 'T', hence only one link there exists between :2 and :4.

All scenes have regions, vertices and lines (edges) joining vertices and separating regions. We generally omit the names of the vertices from the drawing (figure 'R3'); we are also omitting the coordinate axes.

Since each region has an inside and an outside, the following are invalid or illegal configurations in a scene:



A line ending nowhere: illegal.



Our scenes should be such that, to disconnect a separate component of the graph into two components, we have to remove (delete) at least two edges. The graph above is "illegal" as input to our program, since the criterion is not met: removing edge E will disconnect the graph (cf. page 37).

Incidentally, some optical illusions are "recognized" or rejected because they come from illegal scenes of the type just described (cf. section 'Optical Illusions').

See 'Illegal scenes', page 217, in section 'On noisy input.'

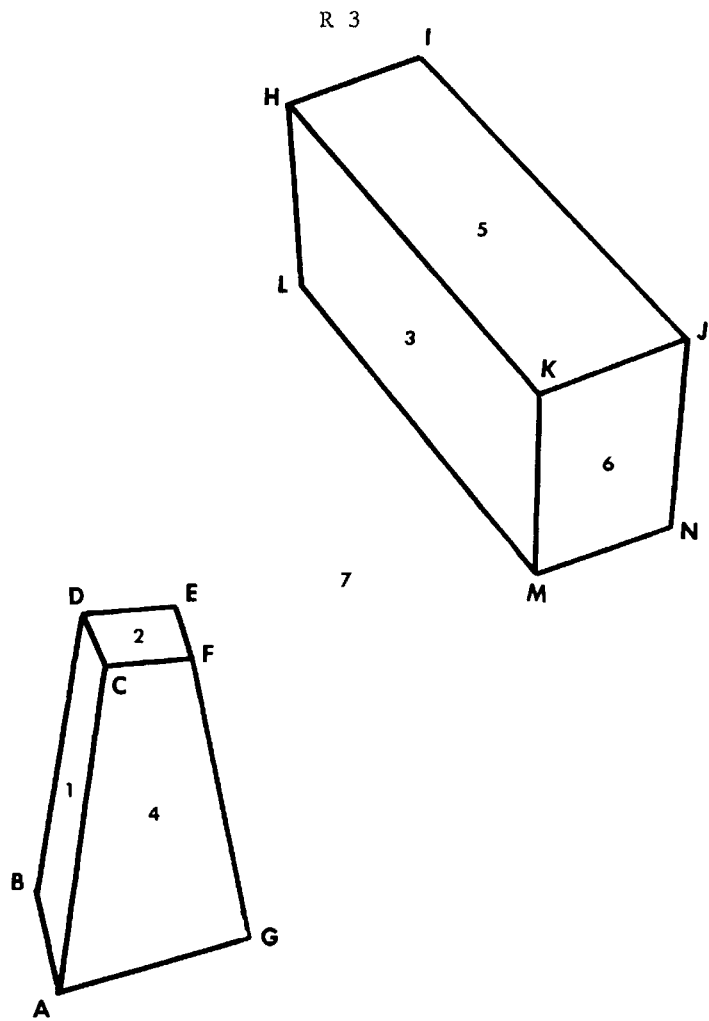


FIGURE 'R 3'  
 A scene analyzed by the program.

SEE 58 ANALYZES R3  
EVIDENCE  
LOCALEVIDENCE  
TRIANG  
GLOBAL  
((NIL)) ((X:5)) G0009 G0006 G0006 G0005 ((X:5)) G0010 G0009 G0007 G0006 ((X:3)) G0010 G0006 G0007 G0005 ((X:2)) G0013 G001  
2 G0011 ((X:1)) G0015 G0014 G0013 G0011 ((X:4)) G0015 G0014 G0012 ((X:7))  
((NIL)) ((NIL)) ((X:6 X:5 X:3)) G0005 G0009 G0006 G0010 G0008 G0007 G0005 ((NIL)) ((X:2 X:1 X:4)) G0015 G0013 G001  
1 G0015 G0014 G0012 ((X:7))  
LOCAL  
((NIL)) ((NIL)) ((X:6 X:5 X:3)) G0005 G0009 G0006 G0010 G0008 G0007 G0005 ((NIL)) ((X:2 X:1 X:4)) G0015 G0013 G0011 G0015 G001  
4 G0012 ((X:7))  
LOCAL  
((X:2 X:1 X:4)) G0015 G0013 G0011 G0015 G0014 G0012 ((X:6 X:5 X:3)) G0005 G0009 G0006 G0010 G0006 G0007 G0005))  
LOCAL  
SMB  
RESULTS  
(BODY 1. 18 X:2 X:1 X:4)  
(BODY 2. 18 X:6 X:5 X:3)  
NIL

RESULTS FOR R 3

Scene SPREAD Body :41-42 was found; also :8-18-19. In the first case, there was one strong link between :41 and :42, because of the heuristic (g) of table 'GLOBAL EVIDENCE' (page 87), and SINGLEBODY completed the object. In the second case, heuristic (g) could not be applied, and SMB had to join :19 with :18.

Bodies :29-30-31-32 and :25-26-27-28 are adequately found. Also the badly occluded long body :10-9-11-12-3 is found.

Body :21-6-25-20 is found as one body. An older version of SEE {Guzmán FJCC 68} used to report two: :6-21 and :5-20. The change is as follows: one link is placed between :6 and :5 because of the matching T's, the other link is a weak one placed because :5 and :20 form a LEG; a weak link is also placed between :6 and :5.

:24 gets reported isolated, instead of together with :22-23, because no Leg is seen; but see comment (page 30) in section 'Simplified View of Scene Analysis'.

SEE tries to find a "minimal" answer; minimal in the sense that it will try to explain the scene with the minimum possible number of bodies (cf. section 'The Concept of a Body'). That is the reason which joined :41 and :42 in one body, instead of two, which is another possible correct answer. That is also true of :19-18-8, interpreted as one parallelepiped with a vertical face (:19) and an horizontal face (:18-8).

The background of SPREAD is also computed (see page 226 of section 'Background Discrimination by Computer').



# SPREAD

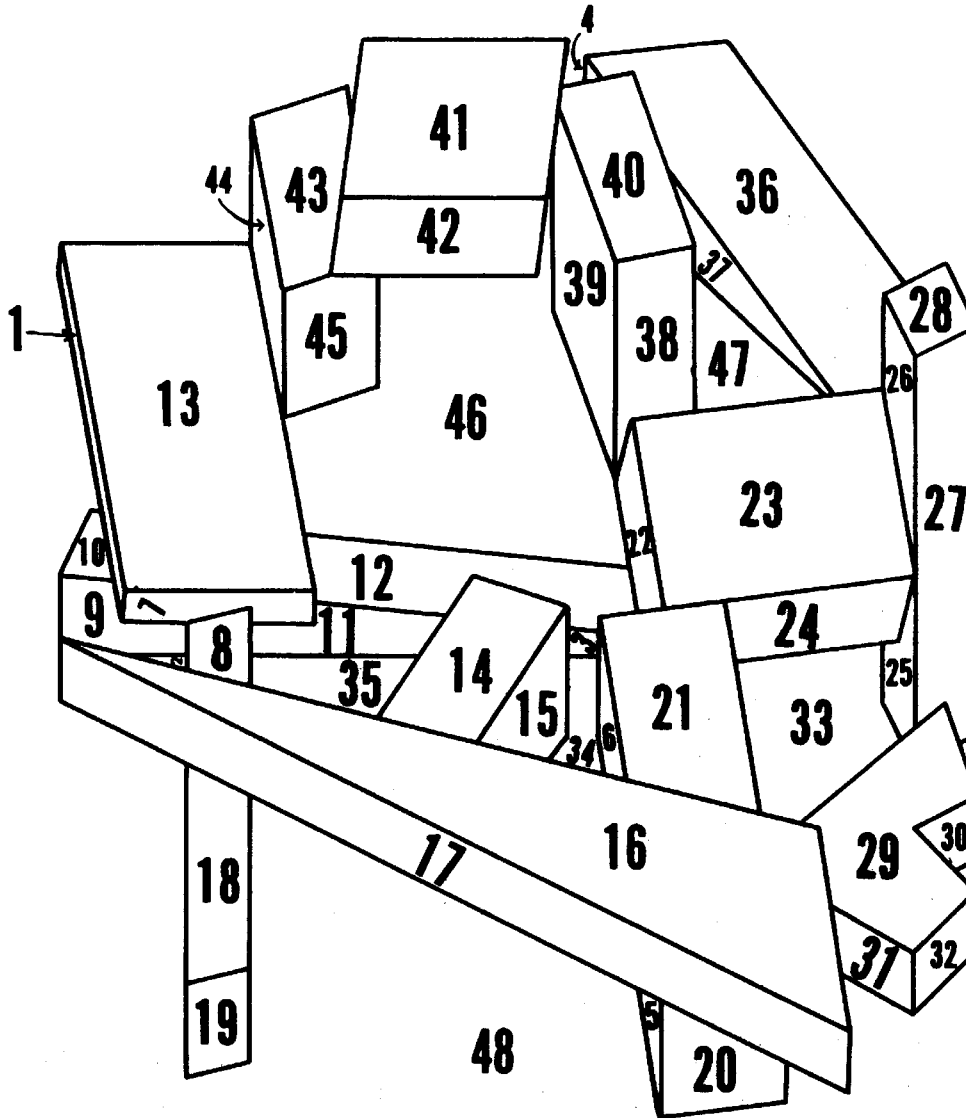


FIGURE 'S P R E A D'

Bodies :10-9-11-12-3 and :6-21-5-20 are properly found. Also is correctly identified the body :19-18-8, which is a parallelepiped with a vertical face (:19) and an horizontal face (:8-18).

QUOTE (BINTO = 0.05, COLTO = 0.01);  
 SEE 58 ANALYZES SPREAD  
 EVIDENCE  
 LOCALEVIDENCE  
 TRIANE  
 GLOBAL  
 (NIL) ((115) 60026 60025) ((114) 60026 60025) ((135) ((119) ((118) 60031 60029) ((131) 60037 60035 60034) ((132) 6003  
 6 60037 60036 60035) ((133) ((126) 60037 60046 60044 60043) ((128) 60047 60045 60044 60042) ((145) 60053 60052 60050) ((  
 (142) 60049) ((143) 60054 60053 60051 60050) ((144) 60054 60052 60051) ((116) 60033) ((112) ((181) 60031 60029) ((121) 60  
 061 60040) ((116) 60061 60044 60040) ((117) 60027 60026) ((113) 60062 60056 60055) ((112) 60065 60063) ((111) 60064  
 60060 60027 60026) ((117) 60062 60056 60055) ((119) 60064 60060 60030) ((110) 60065 6  
 063 60030) ((115) 60041 60032) ((118) 60033) ((120) 60027) ((110) 60066 60046 60045 60043) ((129) 60039 60  
 038 60036 60034) ((124) ((125) 60046) ((127) 60067) ((136) 60024 60022 60021) ((122) 60068) ((146) 600  
 23 60022 60021) ((141) 60049) ((123) 60045 60042) ((139) 60024 60023) ((136) 60024 60022 60021) ((122) 60068) ((146) 600  
 (NIL) (NIL) ((115 114) 60025 60026) ((114) 60025 60026) ((135) ((119) ((118) 60031 60029) ((131) 60037 60035 60034) ((132) 6003  
 ) ((145 143 141) 60054 60053 60051 60050) ((144) 60054 60052 60051) ((116) 60033) ((112) ((181) 60031 60029) ((121) 60  
 19) 60064 60027 60026) ((117) 60062 60056 60055) ((112) 60065 60063) ((111) 60064  
 32) ((130) 60039) ((128 126 127) 60043 60042 60041) ((112 110 109) 60045 60043 60042) ((115) 60041 60032) ((117) 60033) ((120) 60  
 9 60038 60036 60034) ((124) ((125) 60046) ((127) 60067) ((136) 60024 60022 60021) ((122) 60068) ((146) 600  
 ((141) 60049) ((143) 60054 60053 60051 60050) ((144) 60054 60052 60051) ((116) 60033) ((112) ((181) 60031 60029) ((121) 60  
 LOCAL ASSUMES (136) (14) SAME BODY)  
 (LOCAL ASSUMES (130) (131) 132 129) SAME BODY)  
 (LOCAL ASSUMES (116) (117) SAME BODY)  
 (LOCAL ASSUMES (121 16) (15) SAME BODY)  
 (LOCAL ASSUMES (15 121 16) (120) SAME BODY)  
 (LOCAL ASSUMES (13 11 19) (112 110) SAME BODY)  
 LOCAL  
 (NIL) ((115 114) 60025 60026 60025) ((135) ((119) ((118) 60031 60029) ((131) 60037 60035 60034) ((132) 6003  
 60054 60052 60051) ((117 116) 60033) ((112) ((116 16) 60029 60031 60029) ((120 15 12) 16) 60032 60031 60040) (NIL)  
 (NIL) ((113 17 11) 60056 60052 60059 60059 60057 60056 60055) ((112 110 13 11) 19) 60055 60053 60054 60052 60056 60054  
 60060 60030) (NIL) (NIL) (NIL) ((131 132 129 130) 60037 60035 60036 60030 60030) ((128 126 127) 60043 60042 60041) ((115 110 109) 60045 60043 60042)  
 60044 60042 60066 60046 60045 60043) (NIL) ((124) ((125) 60046) ((127) 60067) ((136) 60024 60022 60021) ((122) 60068) ((146) 600  
 IL) ((148) ((141) 60049) ((143) 60054 60053 60051 60050) ((144) 60054 60052 60051) ((116) 60033) ((112) ((181) 60031 60029) ((121) 60037 60035 60034) ((132) 6003  
 LOCAL  
 (SINGLEBODY ASSUMES (123) (122) SAME BODY)  
 (SINGLEBODY ASSUMES (142) (141) SAME BODY)  
 (SINGLEBODY ASSUMES (14 136) (137) SAME BODY)  
 (SINGLEBODY ASSUMES (128 126 127) (125) SAME BODY)  
 (NIL) ((139 140 134) 60023 60023 60024 60022 60021) ((123 122) 60046 60042) (NIL) ((14 136 137) 60037 60041) (NIL) (NIL  
 ) ((124) ((128 126 127 125) 60043 60047 60044 60042 60046 60045 60044) ((131 132 129 130) 60037 60035 60036 60036 60036  
 60036 60039) ((112 110 13 11 19) 60055 60053 60054 60052 60056 60054) ((113 17 11) 60056 60052 60056 60054 60056 60059  
 60087 60055 60085) ((170 15 21 16) 60032 60061 60041 60040) ((110 16) 60029 60031 60029) ((117 116) 60033) ((117 116) 60033) ((117 116) 60033) ((117 116) 60033)  
 44) 60054 60053 60050 60054 60053 60051) ((142 141) 60049) ((119) ((118 114) 60025 60023 60023) ((122) 60068) ((146) 600  
 LOCAL  
 (SMB ASSUMES (19 116) SAME BODY)  
 RESULTS  
 (THE FIRST 1- BODIES ARE ((124)))  
 (BODY 2. 18 139 140 136)  
 (BODY 3. 18 123 122)  
 (BODY 4. 18 14 136 137)  
 (BODY 5. 18 128 126 127 125)  
 (BODY 6. 18 131 132 129 130)  
 (BODY 7. 18 112 110 13 11 19)  
 (BODY 8. 18 113 17 11)  
 (BODY 9. 18 120 15 121 16)  
 (BODY 10. 18 117 116)  
 (BODY 11. 18 145 143 144)  
 (BODY 12. 18 142 141)  
 (BODY 13. 18 119 116 18)  
 (BODY 14. 18 115 114)  
 NIL

RESULTS FOR SPREAD

Scenes STACK and STACK\* In both cases all the bodies were accurately identified by our program, which is written in LISP. In both cases the body :4-15-16 is found.

These scenes show that in many instances one could drastically alter the position of a vertex, without modifying the output of SEE (compare figure 'STACK' with 'STACK\*').

Other examples would show that the vertices of type 'L' can be arbitrarily displaced, so long as their type remains 'L' and other vertices do not change type, without detrimental effect. This displacement may possibly affect some heuristics that use concepts of parallelism or colinearity, but not the rules that use the shape or type of a vertex (cf. table 'VERTICES', page 69) for placing and inhibiting links. Read 'Misplaced vertices' in page 211, in section 'On noisy input.'

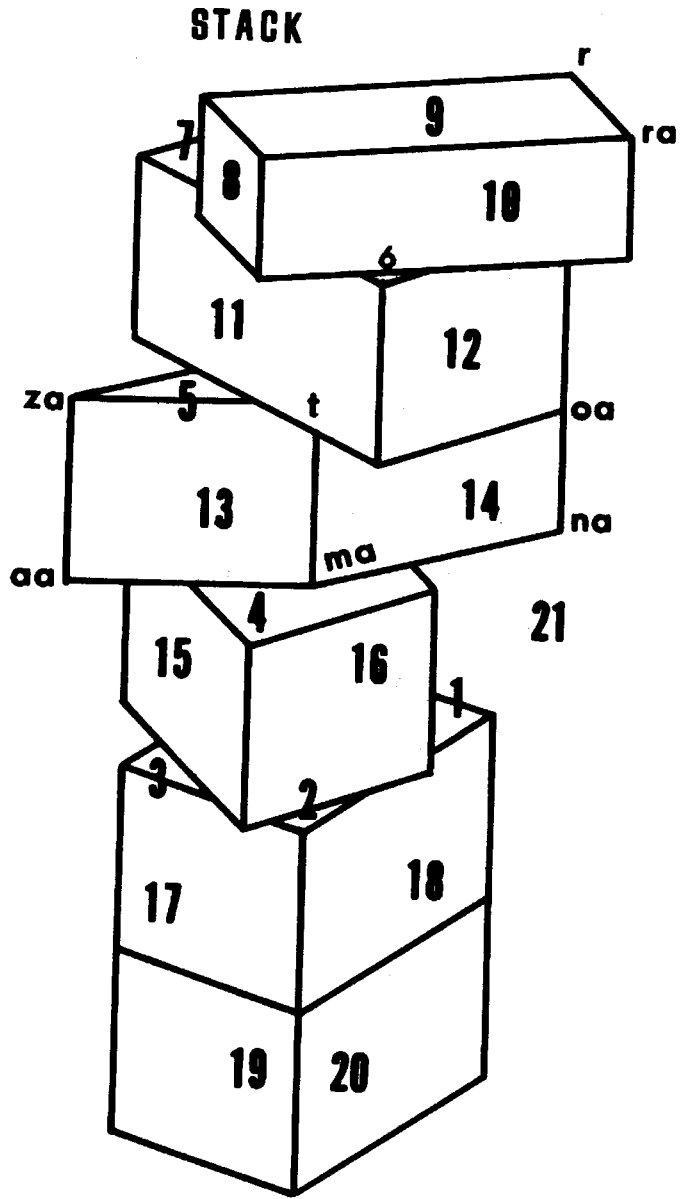


FIGURE 'S T A C K'

Every body is correctly identified. Compare with scene STACK\*. This pair of drawings illustrate the fact that it is often possible to disturb the coordinates (the position) of a vertex, without introducing errors in the recognition.

**STACK \***

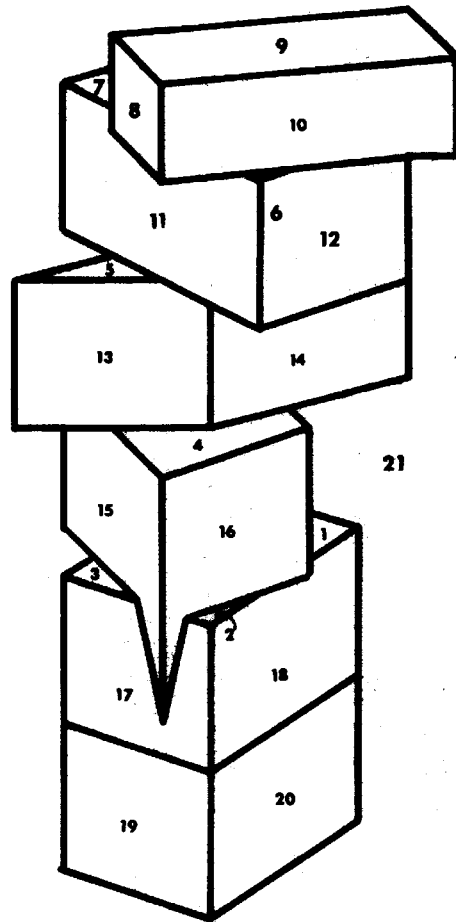


FIGURE 'S T A C K \*'

Every body is correctly found. Compare with scene STACK.

SEE 56 ANALYZES 11 (STACK, STACK\*)

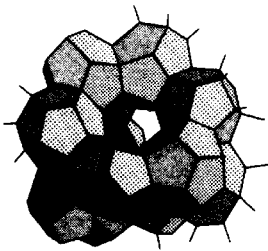
EVIDENCE  
 LOCALEVIDENCE  
 TRIANG  
 GLOBAL  
 (NIL) ((120) 00047 00046) ((119) 00047 00046) ((115) 00036) ((113) 00051 00040 00036) ((119) 00056 00054 00053 00039) ((1  
 7) 00057 00052) ((118) 00056 00055 00054 00038) ((111) 00060 00059 00052 00050) ((116) 00059 00058 00057) ((110) 00055 000  
 53 00039 00038) ((112) 00060 00058 00050) ((114) 00061 00049 00042 00041) ((114) 00051 00040) ((121)) ((11) 00062 00044)  
 ((119) 00065 00063 00045 00044) ((116) 00061 00043 00041 00037) ((12) 00066 00064 00063 00062) ((13) 00066 00045) ((115)  
 00049 00043 00042 00037) ((117) 00065 00064 00048 00045))  
 (NIL) (NIL) ((120) 119) 00046 00047 00046) ((15) 00036) (NIL) (NIL) ((17) 00057 00052) (NIL) (NIL) ((19) 18 110) 00  
 053 00056 00054 00055 00053 00039 00038) ((16 11 12) 00058 00057 00059 00052 00060 00058 00050) (NIL) ((13 14) 00040  
 00036 00051 00040) ((121)) ((11) 00062 00044) (NIL) (NIL) ((14 16 15) 00042 00061 00041 00049 00043 00042  
 00037) ((13 12 18 17) 00048 00066 00062 00063 00044 00065 00064 00048 00045))  
 (NIL) ((120) 119) 00046 00047 00046) ((15) 00036) (NIL) (NIL) ((17) 00053 00056 00054 00055 00053 00039 000  
 38) ((17 16 11 12) 00052 00057 00059 00052 00060 00058 00050) ((113 14) 00040 00036 00051 00040) ((121)) (NIL) (NIL)  
 (NIL) ((14 16 115) 00042 00061 00041 00049 00043 00042 00037) ((11 13 12 18 17) 00044 00066 00062 00063 00044 00065 00064 00048 00045) G  
 0064 00048 00045))  
 LOCAL  
 (LOCAL ASSUMES (15) (113 114) SAME BODY)  
 LOCAL  
 (NIL) ((120 119) 00046 00047 00046) ((113 114 15) 00036 00051 00040 00036) (NIL) ((19 18 110) 00053 00052 00054 00055 G  
 0053 00039 00038) ((17 16 11 12) 00052 00057 00059 00052 00060 00058 00050) (NIL) ((121)) (NIL) ((14 16 115) 00042 G  
 061 00041 00049 00043 00042 00037) ((11 13 12 18 17) 00044 00066 00062 00063 00044 00065 00064 00048 00045))  
 LOCAL  
 ((11 13 12 18 17) 00044 00066 00062 00063 00044 00065 00064 00048 00045) ((14 16 115) 00042 00061 00041 00049 00043  
 G0042 00037) ((17 16 11 12) 00052 00057 00059 00052 00060 00058 00050) ((19 18 110) 00053 00056 00054 00055 00053 0003  
 9 00038) ((113 114 15) 00036 00051 00040 00036) ((120 119) 00046 00047 00046))  
 LOCAL  
 SMB  
 RESULTS  
 (BODY 1. 15 11 13 12 18 17)  
 (BODY 2. 15 14 16 15)  
 (BODY 3. 15 17 16 11 12)  
 (BODY 4. 15 19 18 110)  
 (BODY 5. 15 13 14 15)  
 (BODY 6. 15 120 119)  
 NIL

RESULTS FOR STACK AND STACK\*

Scene L10 The concave object :11-15-14-7-6 presents no problem, since there are plenty of visible vertices (figure 'L10'), and SEE makes good use of them.

SINGLEBODY is necessary to join regions :13 and :2.

The bodies of a scene do not need to be prismatic in shape, nor convex. Their vertices could have errors in their two-dimensional position. Table 'ASSUMPTIONS' (page 255) specifies the suppositions that our program obeys.



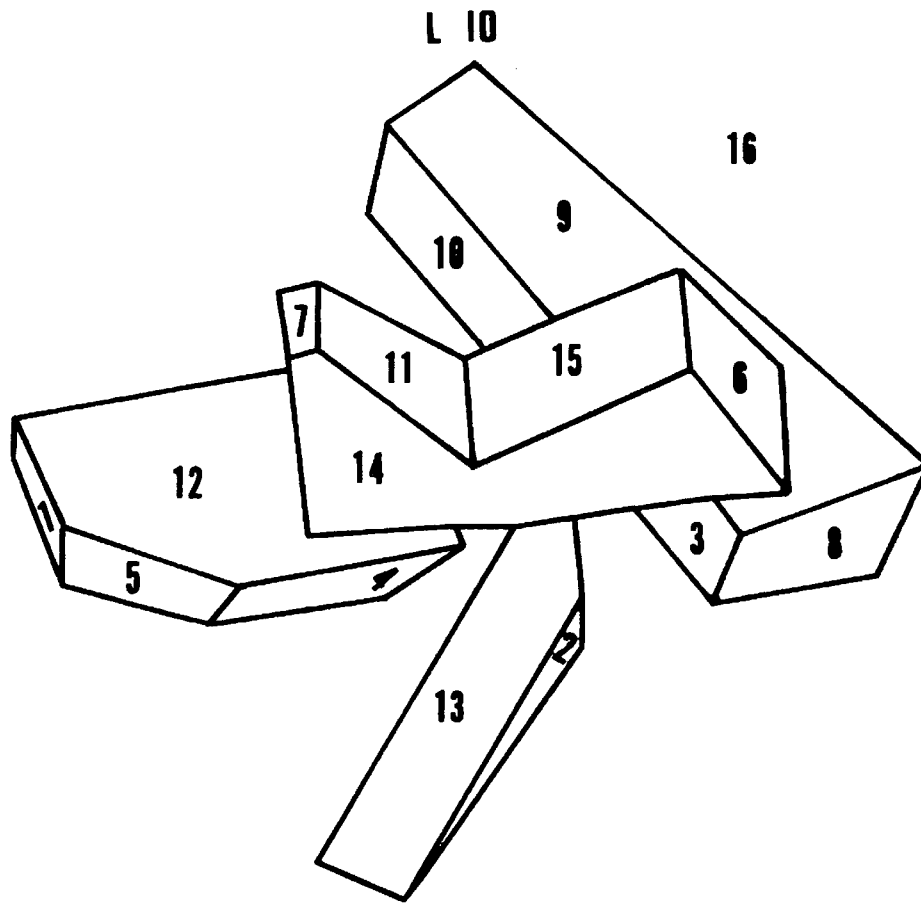


FIGURE 'L 1 0'

Singlebody had to join :2 with :13.  
All four bodies were happily identified.



SEE 56 ANALYZES L10  
EVIDENCE  
LOCAL EVIDENCE  
TRIANG  
GLOBAL  
(NIL) ((8) G0040 G0039 G0037 G0035 G0034 G0033) ((81) G0041 G0039 G0038 G0037) ((88) G0045 G0044 G0042 G0032) ((16) G0040 G0048 G0047 G0046) ((19) G0051 G0050 G0045 G0043 G0032) ((110) G0059 G0051 G0050) ((117) G0057 G0056 G0055 G0054) ((118) G0058) ((123) G0059 G0044 G0043 G0042) ((113) G0058) ((111) G0060 G0055 G0054 G0053) ((115) G0060 G0052 G0049 G0048) ((114) G0057 G0056 G0053 G0052 G0047 G0046) ((114) G0061 G0036 G0035 G0033) ((112) G0061 G0041 G0040 G0038 G0036 G0034) ((116))  
(NIL) (NIL) (NIL) (NIL) (NIL) (NIL) ((12) G0056) ((18) 19 10 13) G0042 G0045 G0032 G0051 G0050 G0059 G0054 G0055 G0057 G0056 G0053  
G0052 G0047 G0046) (NIL) ((15) 11 14 12) G0035 G0041 G0039 G0037 G0036 G0033 G0061 G0040 G0038 G0036 G0034)  
((116))  
LOCAL  
(NIL) (NIL) (NIL) (NIL) ((12) G0056) ((18) 19 10 13) G0042 G0045 G0032 G0051 G0050 G0059 G0043 G0042) ((113) G005  
8) (NIL) ((16) 15 17 11 14) G0047 G0060 G0049 G0048 G0060 G0055 G0054 G0057 G0056 G0053 G0047 G0046) ((15) 11 14  
12) G0035 G0041 G0039 G0037 G0036 G0035 G0033 G0061 G0041 G0040 G0038 G0036 G0034) ((116))  
LOCAL  
(SINGLEBODY ASSUMES (12) (13) SAME BODY)  
((15) 11 14 12) G0035 G0041 G0039 G0037 G0036 G0035 G0033 G0061 G0040 G0038 G0036 G0034) ((16) 15 17 11 14) G00  
47 G0050 G0049 G0048 G0060 G0055 G0054 G0057 G0056 G0053 G0047 G0046) (NIL) ((18) 19 10 13) G0042 G0045 G0032 G005  
1 G0050 G0039 G0044 G0043 G0042) ((12) 113) G0056))  
LOCAL  
SMB  
RESULTS  
(BODY 1. 15 15 11 14 12)  
(BODY 2. 15 16 15 17 11 14)  
(BODY 3. 15 18 19 10 13)  
(BODY 4. 16 12 113)  
NIL  
L10

RESULTS FOR L10

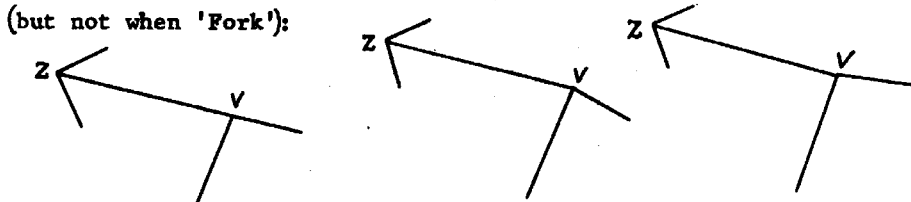
Scene R10 Four bodies are found by our program in R10.

The scene is a good example of a "noisy" scene, in which edges that should be straight look crooked. This is because the coordinates of each vertex are "imprecise"; the vertices have some error in their coordinates. Other scenes also show this tendency; they accurately represent the data analyzed by SEE (the scenes in their final form were drawn by program, then inked manually), and should not be considered as "sloppy drawing jobs".

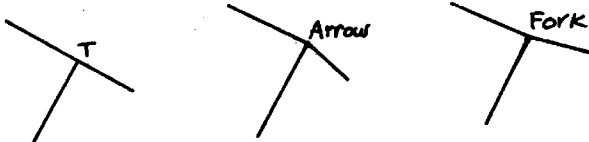
SEE has several ways to cope with these imperfections:

- (1) tolerant definitions of parallelism and colinearity.
- (2) insensitivity of heuristics to displacements of the vertex.

For instance, vertex V will inhibit the link that Z proposes, either when V is of type 'Arrow' or when it is of type 'T' (but not when 'Fork'):



- (3) Large variations in the coordinates of a vertex are possible before that vertex changes type. Vertex of type 'T' are an exception, changing into a Fork or an Arrow by a small displacement.



Nevertheless, it is possible to "straighten" these vertices, by following the suggestion in the comments to scene R17.

The section 'On Noisy Input' deals with these matters.

R 10

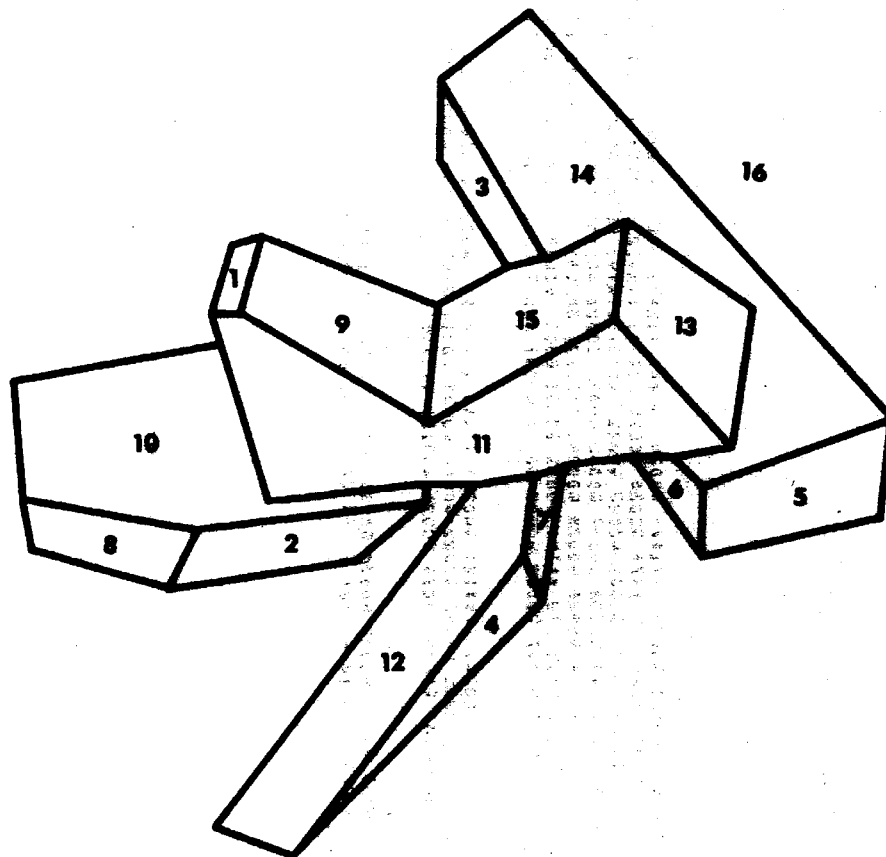


FIGURE 'R 1 0'

The scene contains "noisy" vertices; hence, some edges look bent. SEE has resources to cope with these problems.

Figures L10 and R10 form a stereo pair. In figure 'L10 - R10' in page 247, information from both scenes is combined to find the position of these objects in three-dimensional space. See section 'Stereo Perception'.



Scene TOWER There is no need to make use of LOCAL or SINGLEBODY in this scene, since there are plenty of global (strong) links among the different regions. :18-22 and :17-23 get links thanks to the heuristic that analyzes vertex of type "X".

There are several "false" vertices, formed by coincidences of edges and "genuine" vertices: the vertex common to :9, 11, 12 and 13; the one common to :2, 4, 5, 6. They do not cause problem, because

- (1) in the case of the vertex common to :9, 11, 12 and 13, it is of type 'MULTI', and no link is laid.
- (2) In the case of the vertex shared by regions :2, 4, 5, and 6, it is an "X" that will establish one link between :4 and :5 (which is correct), and another between :2 and :6 (which will do no harm, since we need two "wrong" or misplaced links to cause a recognition mistake).

Compare with scene 'REWOT'.



SEE 56 ANALYZES TOWER

EVIDENCE  
LOCALEVIDENCE

TRIANG

GLOBAL

(NIL) ((20) G0019 G0016 G0017 G0016) ((19) G0022 G0020 G0019 G0016) ((21) G0022 G0020 G0018 G0017) ((18) G0023 G002  
 1) ((22) G0023 G0021) ((23) G0026 G0024) ((10) G0041 G0029 G0026 G0025) ((11) G0041 G0026 G0027) ((13) G0042 G0032  
 G0030) ((14) G0043 G0042 G0032 G0031) ((16) G0046 G0044 G0036 G0035 G0033) ((12) G0047 G0046 G0040 G0038 G0037) ((12)  
 G0043 G0031 G0030) ((17) G0036 G0034 G0033) ((19) G0029 G0027 G0025) ((18) G0044 G0035 G0034) ((15) G0045 G0014 G0013) (  
 (16)) ((17) G0026 G0024) ((15) G0048 G0015 G0014) ((14) G0048 G0045 G0015 G0013) ((13) G0049 G0047 G0039 G0038) ((124  
 )) ((11) G0049 G0040 G0039 G0037))  
 (NIL) (NIL) (NIL) ((20 19 21) G0017 G0020 G0019 G0016 G0022 G0020 G0018 G0017) (NIL) ((18 22) G0021 G0023 G0021) (  
 (NIL) (NIL) (NIL) (NIL) (NIL) (NIL) ((13 14 12) G0030 G0042 G0032 G0043 G0031 G0030) (NIL) ((10 11 19) G0025 G  
 (NIL) (NIL) (NIL) (NIL) (NIL) (NIL) ((16 17 18) G0046 G0035 G0036 G0044 G0033 G0034) (NIL) ((16)) ((123 17) G0024 G002  
 041 G0028 G0029 G0027 G0025) ((16 17 18) G0046 G0035 G0036 G0044 G0033 G0034) (NIL) ((12 13 11) G0046 G0037 G0047 G0038 G0049  
 6 G0024) (NIL) ((15 15 14) G0015 G0014 G0048 G0045 G0015 G0013) (NIL) ((124)) ((12 13 11) G0046 G0037 G0047 G0038 G0049  
 G0040 G0039 G0037))

LOCAL

(NIL) (NIL) ((20 19 21) G0017 G0020 G0019 G0016 G0022 G0020 G0018 G0017) ((18 22) G0021 G0023 G0021) (NIL) (NIL) (  
 (NIL) ((13 14 12) G0030 G0042 G0032 G0043 G0031 G0030) ((10 11 19) G0025 G0041 G0026 G0029 G0027 G0025) ((16 17 18)  
 G0046 G0036 G0033 G0044 G0035 G0034) ((16)) ((123 17) G0024 G0026 G0024) ((15 15 14) G0015 G0014 G0048 G0045 G0  
 015 G0013) ((124)) ((12 13 11) G0046 G0037 G0047 G0038 G0049 G0040 G0039 G0037))

LOCAL

((12 13 11) G0046 G0037 G0047 G0038 G0049 G0040 G0039 G0037) ((15 15 14) G0015 G0014 G0048 G0045 G0015 G0013) ((123 11  
 7) G0024 G0026 G0024) ((16 17 18) G0046 G0035 G0036 G0044 G0033 G0034) ((10 11 19) G0025 G0041 G0026 G0029 G0027  
 G0025) ((13 14 12) G0030 G0042 G0032 G0043 G0031 G0030) ((16)) ((123 17) G0024 G0026 G0024) ((15 15 14) G0015 G0014 G0048 G0045 G00  
 19 G0016 G0022 G0020 G0018 G0017))

LOCAL

SMB

RESULTS

(BODY 1. 15 12 13 11)  
 (BODY 2. 15 15 15 14)  
 (BODY 3. 15 123 117)  
 (BODY 4. 15 16 17 18)  
 (BODY 5. 15 110 111 19)  
 (BODY 6. 15 113 114 112)  
 (BODY 7. 15 116 122)  
 (BODY 8. 15 120 119 121)  
 NIL

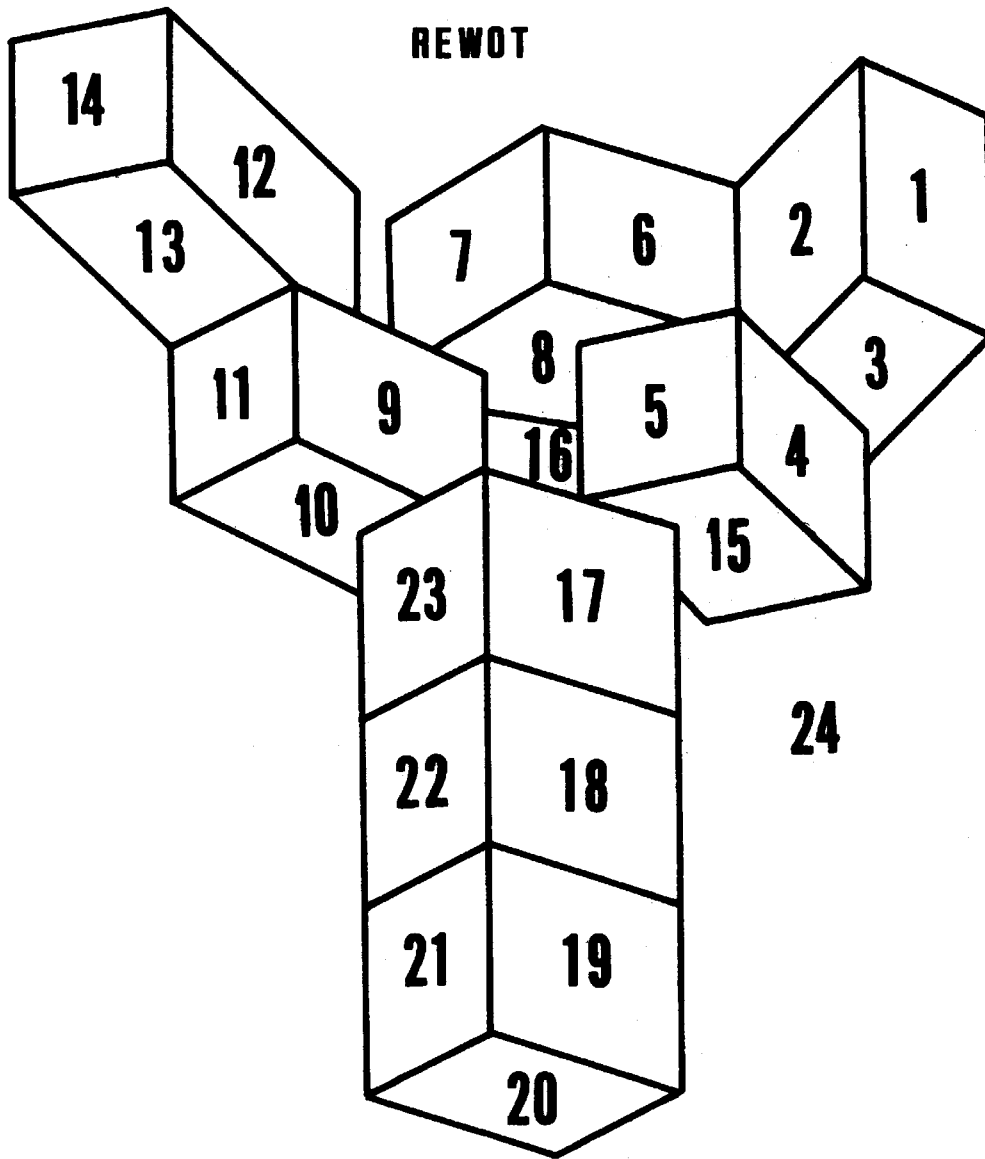
RESULTS FOR TOWER

Scene REWOT This scene (see figure 'REWOT') is the same as the scene TOWER (see figure 'TOWER'), but upside down. The program obtains identical results for both scenes (see 'Results for Tower' and 'Results for Rewot'), because SEE does not use information about a body supporting or leaning on another body. For instance, it was not assumed that body :1-2-3 is partially supporting (in figure 'TOWER') body :4-5-15; clearly this assumption fails in case of figure 'REWOT'. But since the assumption is not followed, the program succeeds in both cases (gives same results).

See table 'ASSUMPTIONS' (page 255) for suppositions that the program makes or presumptions that it does not need.

The regions :16 and :24 had to be marked as part of the background, following standard practice (cf. 'Input Format').





**FIGURE 'R E W O T'**

This scene is the same as the scene TOWER,  
 but with Y replaced by 100. - Y, and  
 X replaced by 100. - X : it is upside  
 down. SEE still finds eight bodies.

SEE 58 ANALYZES REWOT

EVIDENCE

LOCALEVIDENCE

TRIANG

GLOBAL

((NIL)) ((:20)) G0134 G0133 G0132 G0131) ((:19)) G0137 G0135 G0134 G  
0131) ((:21)) G0137 G0135 G0133 G0132) ((:18)) G0138 G0136) ((:22))  
G0138 G0136) ((:23)) G0141 G0139) ((:10)) G0156 G0144 G0143 G0140)  
((:11)) G0156 G0143 G0142) ((:13)) G0157 G0147 G0145) ((:14)) G0158  
G0157 G0147 G0146) ((:6)) G0161 G0159 G0151 G0150 G0148) ((:2)) G01  
62 G0161 G0155 G0153 G0152) ((:12)) G0158 G0146 G0145) ((:17)) G0151  
G0149 G0148) ((:9)) G0144 G0142 G0140) ((:8)) G0159 G0150 G0149) (  
(:5)) G0160 G0129 G0128) ((:16)) ((:17)) G0141 G0139) ((:15)) G0163  
G0130 G0129) ((:4)) G0163 G0160 G0130 G0128) ((:3)) G0164 G0162 G01  
54 G0153) ((:24)) ((:1)) G0164 G0155 G0154 G0152))  
((NIL)) (NIL) (NIL) ((:20 :19 :21)) G0132 G0135 G0134 G0131 G0137 G  
0135 G0133 G0132) (NIL) ((:18 :22)) G0136 G0138 G0136) (NIL) (NIL)  
(NIL) (NIL) (NIL) (NIL) (NIL) ((:13 :14 :12)) G0145 G0157 G0147 G  
0158 G0146 G0143) (NIL) ((:10 :11 :9)) G0140 G0156 G0143 G0144 G01  
42 G0140) ((:6 :7 :8)) G0161 G0150 G0151 G0148 G0159 G0150 G0149)  
(NIL) ((:16)) ((:23 :17)) G0139 G0141 G0139) (NIL) ((:15 :5 :4)) G0  
130 G0129 G0163 G0160 G0130 G0128) (NIL) ((:24)) ((:2 :3 :1)) G016  
1 G0152 G0162 G0153 G0164 G0155 G0154 G0152))

LOCAL

((NIL)) (NIL) ((:20 :19 :21)) G0132 G0135 G0134 G0131 G0137 G0135 G  
0133 G0132) ((:18 :22)) G0136 G0138 G0136) (NIL) (NIL) (NIL) ((:13  
:14 :12)) G0145 G0157 G0147 G0158 G0146 G0145) ((:10 :11 :9)) G014  
0 G0156 G0143 G0144 G0142 G0140) ((:6 :7 :8)) G0161 G0150 G0151 G0  
148 G0159 G0150 G0149) ((:16)) ((:23 :17)) G0139 G0141 G0139) ((:1  
5 :5 :4)) G0130 G0129 G0163 G0160 G0130 G0128) ((:24)) ((:2 :3 :1))  
G0161 G0152 G0162 G0153 G0164 G0155 G0154 G0152))

LOCAL

((:12 :3 :1)) G0161 G0152 G0162 G0153 G0164 G0155 G0154 G0152) ((:  
15 :5 :4)) G0130 G0129 G0163 G0160 G0130 G0128) ((:23 :17)) G0139 G  
0141 G0139) ((:6 :7 :8)) G0161 G0150 G0151 G0148 G0159 G0150 G0149  
) ((:10 :11 :9)) G0140 G0156 G0143 G0144 G0142 G0140) ((:13 :14 :1  
2) G0145 G0157 G0147 G0158 G0146 G0145) ((:18 :22)) G0136 G0138 G0  
136) ((:20 :19 :21)) G0132 G0135 G0134 G0131 G0137 G0135 G0133 G01  
32))

LOCAL

SMB

RESULTS

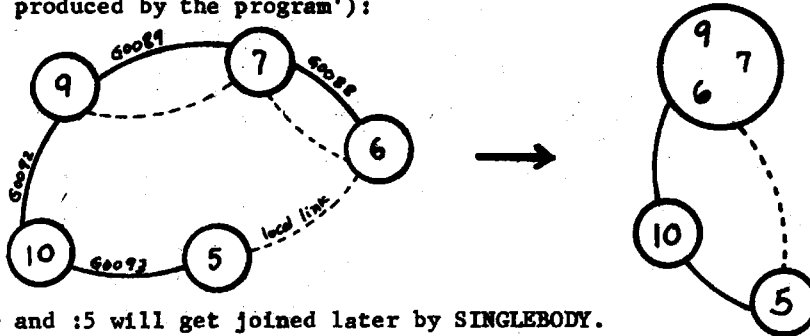
(BODY 1. IS :2 :3 :1)  
(BODY 2. IS :15 :5 :4)  
(BODY 3. IS :23 :17)  
(BODY 4. IS :6 :7 :8)  
(BODY 5. IS :10 :11 :9)  
(BODY 6. IS :13 :14 :12)  
(BODY 7. IS :18 :22)  
(BODY 8. IS :20 :19 :21)

NIL

RESULTS FOR REWOT

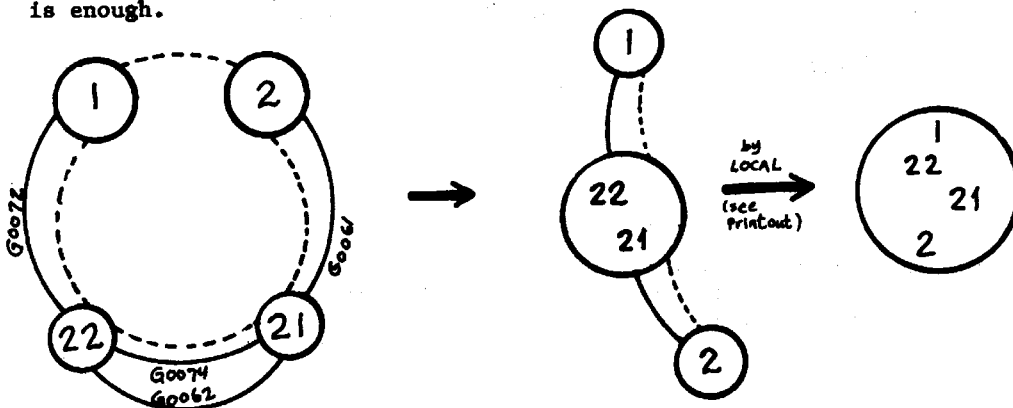
Scene WRIST\* The concave objects are properly identified. W places a link between :23 and :4, and another between :30 and :4. CC does not inhibit the link between :17 and :19 ordered by the Arrow NA, because NOSABO was never called, since the first rule of 'ARROW' (page 84) was applied.

The only mistake was that objects :9-7-6 and :10-5 should be fused and reported as only one. There is a link between :9 and :10 put by heuristic (g) of table 'GLOBAL EVIDENCE'. It is not enough. There is also a weak link between 'Triangles' :5 and :6. OB is not a 'Leg', so there is no weak link between :10 and :5. The situation is as follows (see chains of links in 'RESULTS FOR WRIST\*'; how to read these chains is explained in page 110, 'Explanation of the print-out produced by the program'):



:10 and :5 will get joined later by SINGLEBODY.

Almost the same thing occurs with :1-2-22-21, but in this case vertex A produces one strong link between 22 and 21, and vertex R, by heuristic (g) of table 'Global Evidence', also links 22 with 21. This is enough.



WRIST \*

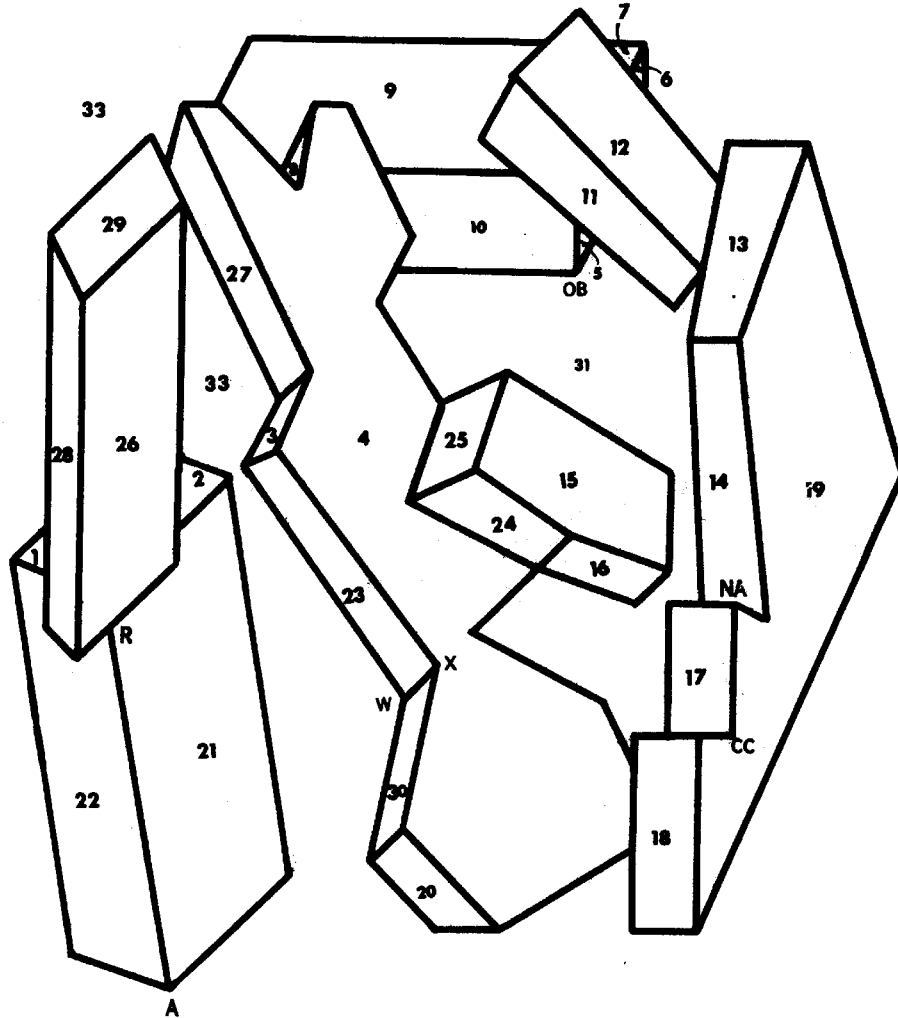


FIGURE 'W R I S T \*'

Instead of one, two bodies were found in :9-7-6 and :10-5  
 Insufficiency of links was the offending reason. All other  
 objects were correctly found.



Scenes L2 and R2 Two objects are found, as expected.

These scenes form a stereographic pair: two pictures taken from the same scene from slightly different locations, maintaining parallel the optical axes of the cameras, and the same magnification. A program, not yet completed, is designed with the following ideas: Left and right pictures are independently processed by SEE; L2 and R2 in this example. The answers are

ANALYSIS OF L2	ANALYSIS OF R2
(BODY 1. IS :2 :4)	(BODY 1. IS %:1 %:2 %:4)
(BODY 2. IS :1 :5 :3)	(BODY 2. IS %:3 %:6 %:5)

The question is now: Is body :2-:4 the same body as %:1-%:2-%:4, or is it %:3-%:6-%:5 ? It is required, after decomposition of the scene into bodies, to match the left bodies with the right bodies. If this is accomplished, one could then locate the figure in three dimensional space, from the two-dimensional coordinates of the figure in the left and right scenes.

In this way it will be known where these objects are located in the "real world".

This "matching" mentioned above is complicated as follows:

- It is possible that the number of objects observed in one view is different from the number in the other.
- On a given object, it is possible that SEE will make a mistake in the left view, but not in the right view; as a consequence, two bodies on the left have to be matched with one on the right.

If the two axes of the camera are on an horizontal plane, a vertex in the left scene and its corresponding vertex in the right scene (if visible) will have the same y-coordinate, such as H in L2 and XI in R2. Other known relations exist, derived from the relative position of the axes of the camera, magnification, etc. See section 'Stereo Perception'.

R 2

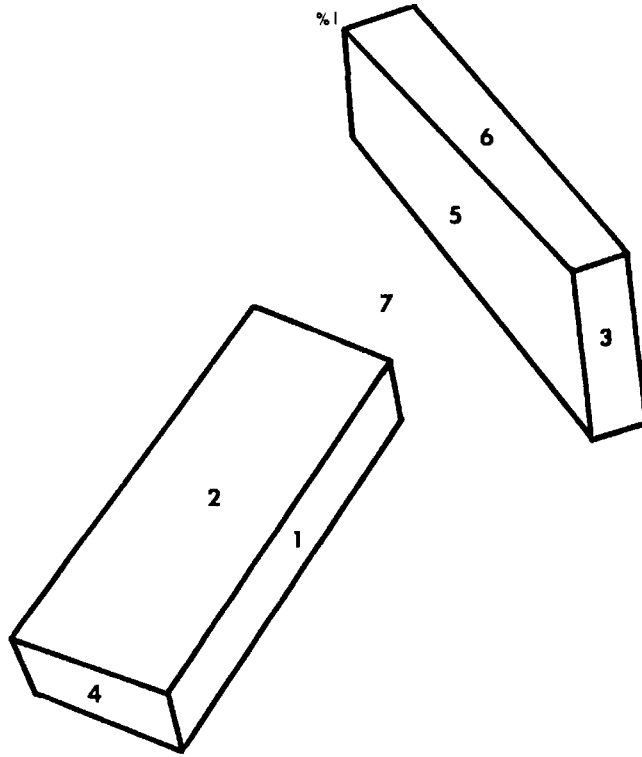


FIGURE "R 2"  
Two bricks are found.

SEE 55 ANALYZES R2  
 EVIDENCE  
 LOCALEVIDENCE  
 TRIANG  
 GLOBAL  
 ((NIL) ((X:3) G0009 G0006 G0005 G0004) ((X:6) G0010 G0009 G007 G0005) ((X:5) G0010 G0006 G0007 G0004) ((X:1) G0014 G001  
 3 G0012 G0011) ((X:2) G0016 G0015 G0014 G0011) ((X:4) G0016 G0015 G0013 G0012) ((X:7)))  
 ((NIL) (NIL) (NIL) ((X:3 X:6 X:5) G0004 G0009 G0005 G0010 G0006 G0007 G0004) (NIL) (NIL) ((X:1 X:2 X:4) G0012 G0015 G001  
 4 G0011 G0016 G0015 G0013 G0012) ((X:7)))  
 LOCAL  
 ((NIL) (NIL) ((X:3 X:6 X:5) G0004 G0009 G0005 G0010 G0006 G0007 G0004) (NIL) ((X:1 X:2 X:4) G0012 G0015 G0014 G0011 G001  
 6 G0015 G0013 G0012) ((X:7)))  
 LOCAL  
 ((X:1 X:2 X:4) G0012 G0015 G0014 G0011 G0016 G0015 G0013 G0012) ((X:3 X:6 X:5) G0004 G0009 G0005 G0010 G0006 G0007 G000  
 4))  
 LOCAL  
 SMB  
 RESULTS  
 (BODY 1. 16 X:1 X:2 X:4)  
 (BODY 2. 16 X:3 X:6 X:5)  
 NIL

RESULTS FOR R2



L 2

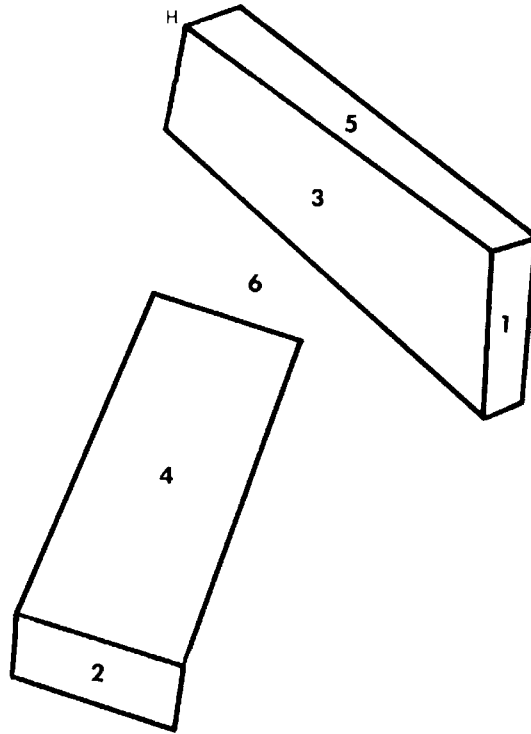


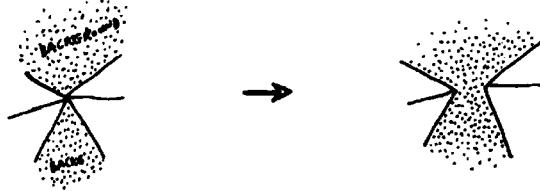
FIGURE 'L 2'

Even if (possibly) a face of object :4-2 is missing,  
in this case SEE makes the correct identification.  
Section 'On Noisy Input' deals with imperfect  
information.

SEE SB ANALYZES L2  
 EVIDENCE  
 LOCALEVIDENCE  
 TRIANG  
 GLOBAL  
 (NIL) (11) 60009 60006 60007 60004 ((15) 60010 60009 60006 60006) ((13) 60010 60007 60006 60004) ((14) 60011) ((12) 6  
 0011) ((16))  
 (NIL) (NIL) (NIL) ((11 15 13) 60007 60010 60009 60006 60010 60007 60006 60004) ((14) 60011) ((12) 60011) ((16))  
 LOCAL  
 (LOCAL ASSUMES (14) (12) SAME BODY)  
 (NIL) (NIL) ((11 15 13) 60007 60010 60009 60006 60010 60007 60006 60004) ((12 14) 60011) (NIL) ((16))  
 LOCAL  
 ((12 14) 60011) ((11 15 13) 60007 60010 60009 60006 60010 60007 60006 60004))  
 SMB  
 RESULTS  
 (BODY 1. 18 12 14)  
 (BODY 2. 18 11 15 13)  
 NIL

RESULTS FOR L2

Scene L19 The small triangle :15 just could not get joined with the remainder of the body :16-20-19, and two objects were found. There is a weak link between :15 and :19, but it did not help since there is no link between :15 and :16. What happens is that regions :1, :15, :13 and :22 all meet forming a vertex of type MULTI; this vertex should (in some future version of SEE) be split into two, since both :1 and :37 are the background- The rule for this splitting seems to be



:11 was joined with :4, but isolated from :12-27-5. There are no T-joints between these two nuclei that could give 'hints' (i. e., links) for their unification.

The two large concave objects were properly isolated.

Compare with R19 and WRIST\*.

See 'Merged vertices', page 221 in section 'On noisy input.'

L 19

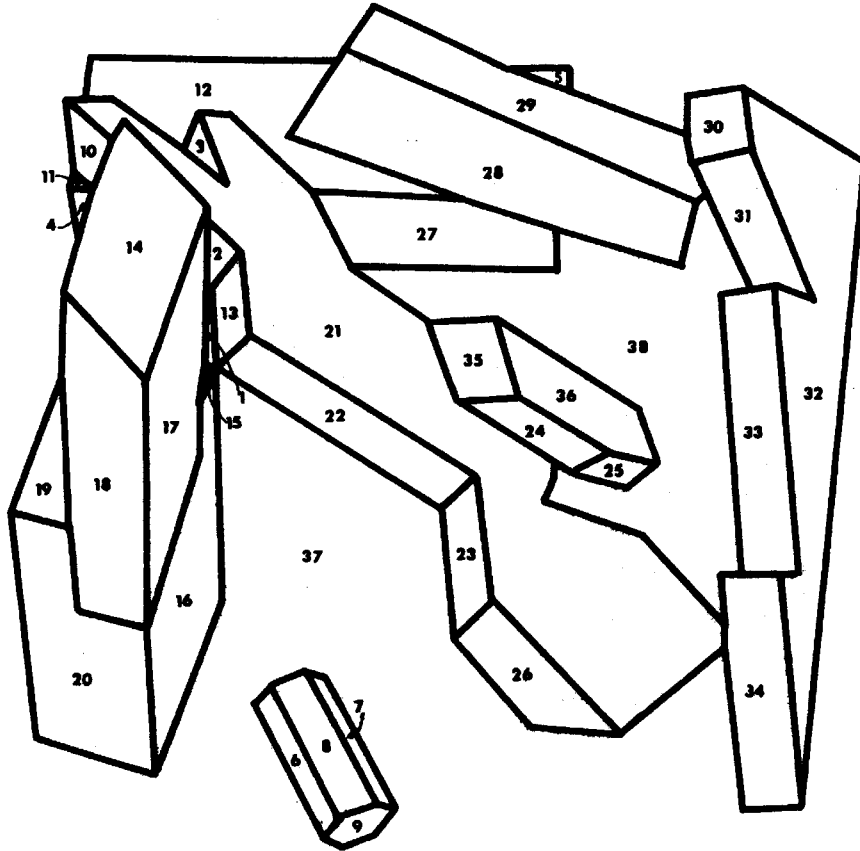


FIGURE 'L 1 9'

It was easy to find :6-7-8-9, the hexagonal prism.  
:15 was reported as a single object: a mistake. The two big  
concave objects were appropriately identified.



Scene R19 As in L19, here the triangle :27 is detached from :5-32-33, two bodies being reported. There is no strong link between :27 and :33. There is a weak link between :27 and :5, because both are 'triangles' facing each other, but that is not enough. A weak link is never enough.

All other bodies are properly found, including :10-16-2-3.

Vertex RA, of course, contributes with no links. The situation could change if we discover that RA is a false vertex, that is, one composed by the merge of two genuine ones. SUGGESTION There is enough enformation, I think, since :34 and :37 are background, and this will suggest a way to "divide" vertex RA into two simpler ones. This idea of dividing vertices of type MULTI into simpler ones should be applied with caution, since there will be genuine vertex of type MULTI (which should not be split). The main use of this technique will be for helping single regions to join some other body, a task performed now, not too satisfactorially, by SMB.

Compare with L19 and WRIST\*.  
See 'merged vertices', page 221.

R 18

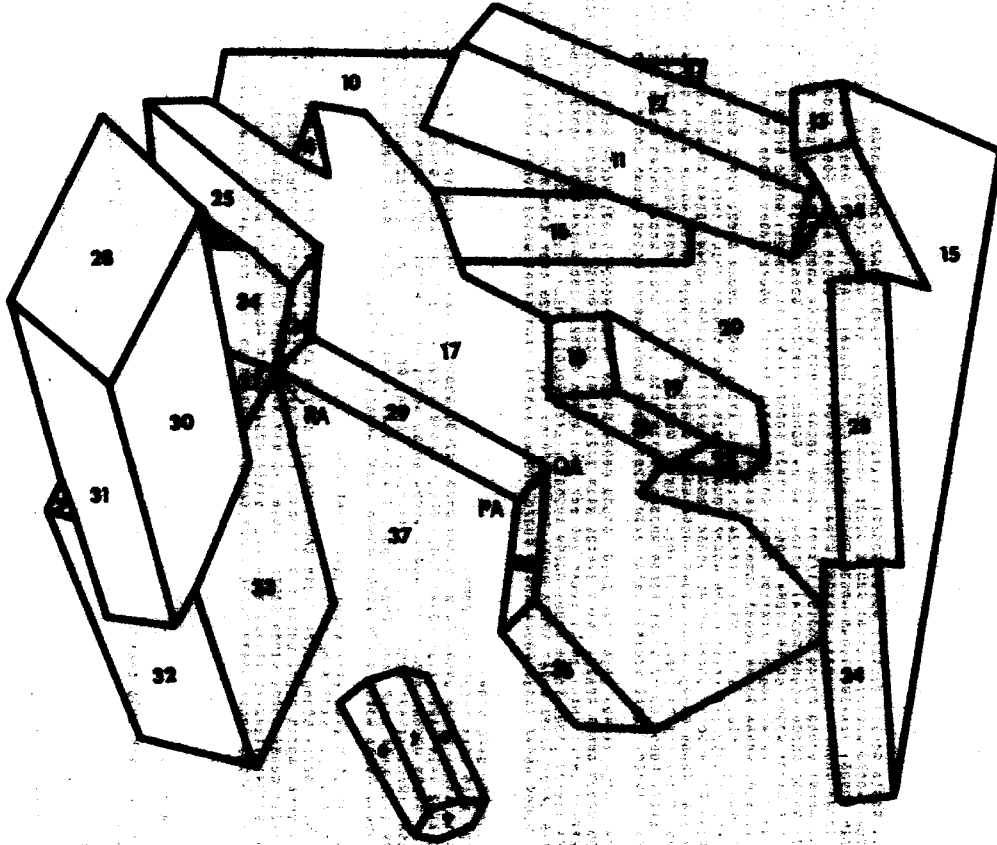


FIGURE 'R 1 9'

127 was separated from 133-32-5. All other objects were correctly found.



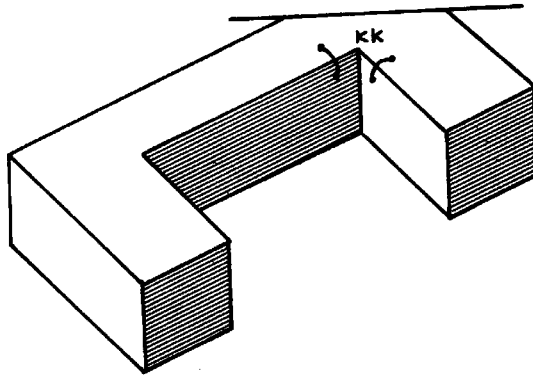


Scene CORN The pyramid :8-9-10 was easily identified because a vertex of type PEAK produces many links. In the bottom, bodies :1-2-3-4 and :12-13-11 were separated, because the fork between :4 and :12 has the background as a region, and did not contribute with any links. Certainly, this is a possible interpretation. Another interpretation is to regard the object :1-2-3-4-11-12-13 as a prism with the shape of a "C".

SINGLEBODY was needed to join :4 with :2-3-1, the only link being placed by heuristic (g) of table 'GLOBAL EVIDENCE.'

The program knows that :22 is the background.

If we could see the hidden vertex KK (if it indeed exists), two links would be put and we will have had one body:



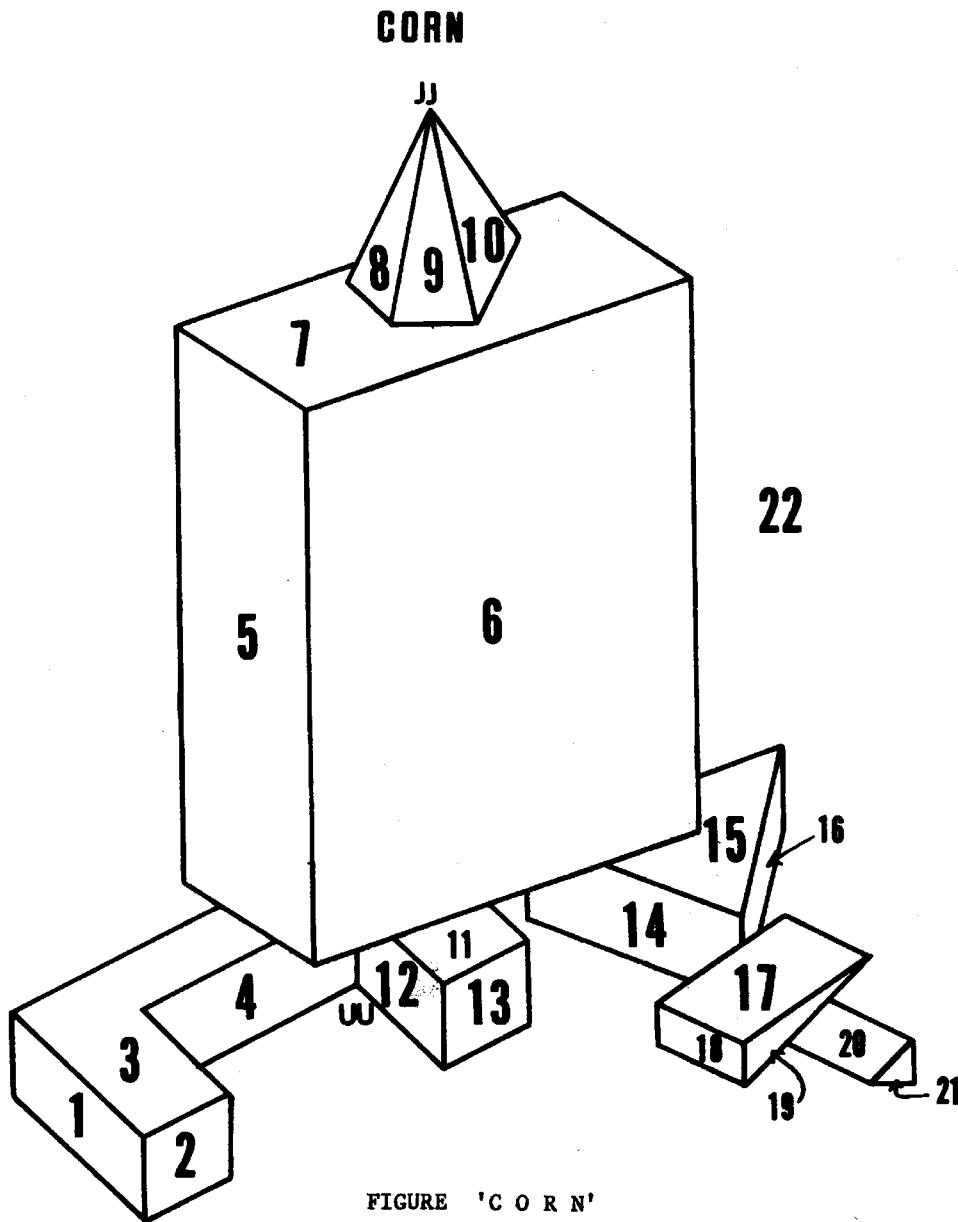


FIGURE 'C O R N'

The pyramid at the top was identified properly. Two bodies were found at the bottom, which is a plausible interpretation: :1=2=3=4 and :11=12=13.

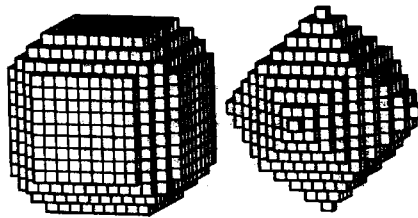
SEE 58 ANALYZES CORN  
EVIDENCE  
LOCAL EVIDENCE  
TRIANG  
GLOBAL  
(NIL) (12) 60019 60016 60017 60015 (18) 60026 60024 (19) 60027 60026 60025 60024 (110) 60027 60025 (117) 60028  
60023 60022 60020 (115) 60031 60030 60013 (116) 60032 60030 60029 60013 (121) 60035 60034 (120) 60036 60035 6003  
4) (119) 60039 60038 60037 60033 (118) 60041 60040 60038 60037 (117) 60041 60040 60039 60033 (114) 60036 60032 60  
031 60029 (113) 60044 60043 60042 60014 (111) 60046 60045 60044 60042 (112) 60046 60045 60043 60014 (116) 60047 6  
0028 60022 60021 (124) 60048 (125) 60047 60023 60021 60020 (122) (113) 60049 60048 60016 60015 (111) 60049 6  
019 60017 60016)  
(NIL) (NIL) (NIL) (118 19 110) 60027 60026 60024 60027 60025 (NIL) (NIL) (121 120) 60034 60036 6003  
5 60034 (NIL) (NIL) (119 118 117) 60037 60041 60038 60037 60041 60040 60039 60033 (115 116 114) 60013 60030 60013 60  
036 60032 60031 60029 (NIL) (NIL) (113 111 112) 60014 60045 60044 60042 60046 60045 60043 60014 (NIL) (114) 60048 (1  
17 16 15) 60028 60028 60022 60047 60023 60020 (122) (NIL) (112 111 11) 60017 60048 60016 60015 60049 60019 60017  
60016))  
LOCAL  
(NIL) (NIL) (118 19 110) 60027 60026 60024 60027 60025 (NIL) (NIL) (121 120) 60034 60036 60035 60034 (NIL) (119 116  
117) 60037 60041 60038 60037 60041 60040 60039 60033 (115 116 114) 60013 60030 60013 60036 60032 60031 60029 (NIL) (1  
113 111 112) 60014 60045 60044 60042 60046 60045 60043 60014 (114) 60048 (117 16 15) 60020 60026 60022 60047 60023 60  
021 60020 (122) (112 111 11) 60017 60048 60016 60015 60049 60019 60017 60016))  
LOCAL  
(SINGLEBODY ASSUMES (12 13 11) (14) SAME BODY)  
(112 13 11 14) 60017 60048 60016 60015 60019 60019 60017 60016 (117 16 15) 60020 60028 60022 60047 60023 60021 60020)  
(NIL) (113 111 112) 60014 60045 60044 60042 60046 60045 60043 60014 (115 116 114) 60013 60030 60013 60036 60032 60031  
60029 (119 118 117) 60037 60041 60038 60037 60041 60040 60039 60033 (121 120) 60034 60036 60035 60034 (118 19 110)  
60027 60026 60024 60027 60025))  
LOCAL  
SMB  
RESULTS  
(BODY 1. 18 12 13 11 14)  
(BODY 2. 15 17 16 15)  
(BODY 3. 16 113 111 112)  
(BODY 4. 15 115 116 114)  
(BODY 5. 13 119 118 117)  
(BODY 6. 18 121 120)  
(BODY 7. 18 18 19 110)  
NIL

RESULTS FOR CORN

Scene L9 Here the tolerances SINTO and COLTO that allow for "sloppy parallelism" have made T's out of NA and PA. Therefore, these vertices do not contribute any links for :1. Moreover, the "T" PA inhibits the link suggested by QA between :1 and :8. That being all, :1 gets reported as a single body (see next page).

By decreasing the tolerances, correct identification is possible (see the correct identification in page 155).

See 'Tolerances in collinearity and parallelism', page 215 .





SEE 56 ANALYZES L9

EVIDENCE

LOCALEVIDENCE

TRIANG

GLOBAL

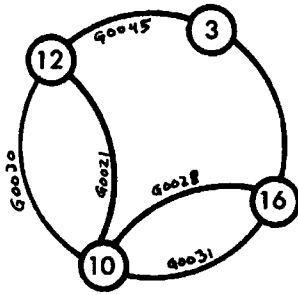
(NIL) ((11)) ((18)) 60012 ((13)) 60026 60013 ((119)) 60019 60015 60014 ((12)) 60021 60020 60019 60018 60017 ((120)) 6002  
3 60022 60020 60017 ((118)) 60030 60028 60023 60022 60021 60018 60016 60015 ((115)) 60031 60029 60016 60014 ((114)) 6002  
7 60013 ((14)) 60031 60030 60029 60028 ((111)) 60035 60033 60032 60027 60025 ((110)) 60036 60035 60034 60033 ((112)) 600  
36 60034 60032 60026 60025 ((116)) 60024 ((116)) 60039 60038 ((115)) 60044 60043 60040 60039 60038 60037 ((119)) 60044 6004  
2 60037 60012 ((17)) 60043 60042 60040 ((117)) 60045 60041 ((113)) 60045 60041 60024 ((121))  
(NIL) ((11)) ((18)) 60012 ((13)) 60026 60013 ((119)) 60019 60015 60014 ((12)) 60021 60020 60019 60018 60017 ((120)) 6002  
5 12 20 18 14) 60029 60014 60019 60020 60017 60023 60022 60021 60018 60016 60015 60031 60030 60029 60028 (NIL) (NIL)  
((111 110 112) 60032 60027 60036 60035 60033 60032 60026 60025 ((116)) 60024 (NIL) (NIL) (NIL) (NIL) (16 15 19 )  
7) 60043 60039 60036 60044 60037 60012 60043 60042 60040 (NIL) ((117 113) 60041 60045 60041 60024) ((121))  
(NIL) ((11)) ((18)) 60012 ((13)) 60026 60013 ((119)) 60019 60015 60014 ((12)) 60021 60020 60019 60018 60017 ((120)) 6002  
60014 60019 60020 60017 60023 60022 60021 60018 60016 60015 60031 60030 60029 60028 (NIL) ((11 110 112) 60032 60027 6  
0036 60035 60033 60036 60034 60032 60026 60025 ((116)) 60024 (NIL) ((11 110 112) 60032 60027 6  
0043 60042 60040) ((117 113) 60041 60045 60041 60024) ((121))  
LOCAL  
LOCAL ASSUMES ((13)) ((14)) SAME BODY)  
LOCAL ASSUMES ((16)) ((15 19 17)) SAME BODY)  
(NIL) ((11)) ((17)) ((16 15 19 17 18)) 60039 60038 60044 60037 60043 60042 60040 60012 ((114 13) 60027 60026 60013) (NIL) (NIL)  
) ((119 115 12 20 18 14) 60015 60029 60014 60019 60020 60017 60023 60022 60021 60016 60015 60031 60030 60029 600  
28) ((111 110 112) 60032 60027 60036 60035 60033 60036 60032 60026 60025) ((116) 60024) (NIL) ((117 113) 60041 600  
45 60041 60024) ((121))  
(NIL) ((11)) ((16 15 19 17 18)) 60039 60038 60044 60037 60043 60042 60040 60012 (NIL) (NIL) ((119 115 12 20 18 14) 60  
015 60029 60014 60019 60020 60017 60023 60022 60021 60016 60015 60031 60030 60029 60028) ((114 13 11 10 12) 600  
26 60013 60027 60035 60033 60036 60034 60032 60026 60025) ((116) 60024) ((117 113) 60041 60045 60041 60024) ((121))  
LOCAL  
(SINGLEBODY ASSUMES ((17 13)) ((16) SAME BODY)  
((117 113 116) 60041 60045 60041 60024) (NIL) ((114 13 11 10 12) 60026 60013 60027 60035 60033 60036 60034 60032 600  
029 60028) ((116 15 19 17 18) 60039 60036 60044 60037 60043 60042 60040 60012) ((111))  
LOCAL  
SMB  
RESULTS  
(THE FIRST 1. BODIES ARE ((11)))  
(BODY 2. 15 17 13 16)  
(BODY 3. 18 14 13 11 10 12)  
(BODY 4. 18 19 15 12 20 18 14)  
(BODY 5. 18 16 15 19 17 18)  
NIL

See also next page.

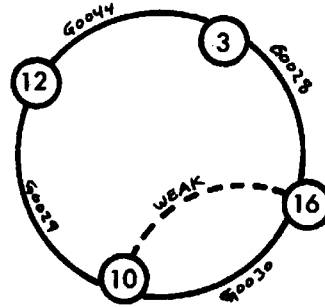
RESULTS FOR L9



Scenes R9 and R9T Four bodies are found in R9, five in R9T. The difference is that Y and JA (see figure at bottom of this page) are not "matching T's" in R9T. The strong links among :12, :3, :10, and :16 are:



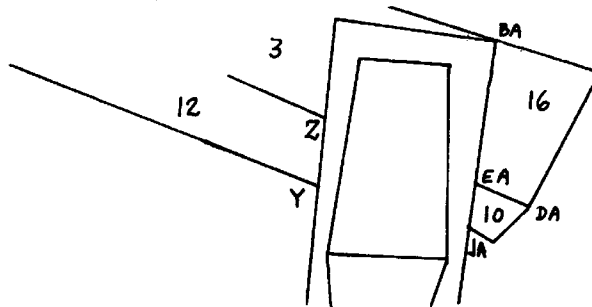
LINKS FOR R 9



LINKS FOR R 9 T

In R9, the two strong links (G0030 and G0021) between :12 and :10 were put by the matching T's Z-EA and Y-JA; of the two strong links between :10 and :16, one was because DA is an arrow; the other, because EA is a "T" for which heuristic (g) of table 'GLOBAL EVIDENCE' applies.

But in scene R9T, not having Y and JA as matching T's, a link between :10 and :12 dis appears; and also nuclei :16 and :10 can not be linked by heuristic (g) of table 'GLOBAL EVIDENCE'. SEE decides to report two bodies there: :3-12 and :16-10 instead of one as in scene R9.



Are Y and JA matching T's or not? Different answers produce different analyses of the scene.

These scenes show that the analyses can be quite sensitive to the "right" definition of parallelism and colinearity.



SEE 58 ANALYZES R9  
EVIDENCE  
LOCAL EVIDENCE  
TRIANG  
LOCAL  
(NIL) ((X:20) 60016 60017 60016 60014 60013 60012) ((X:19) 60020 60019 60018 60016 60015) ((X:13) 60023 60022 60020) ((  
X:15) 60026 60025 60023 60022) ((X:10) 60031 60030 60028 60021) ((X:16) 60031 60029 60028) ((X:8) 60027 60019 60015 6001  
4 60012) ((X:17) 60032 60027 60026 60025 60024) ((X:7) 60032 60024 60017 60013) ((X:9) 60036 60034 60033) ((X:14) 60036  
60035 60033) ((X:6) 60038 60037) ((X:18) 60037) ((X:5) 60035 60034) ((X:11) 60044 60042 60041 60039) ((X:1) 60043 60042  
60038) ((X:12) 60045 60030 60021) ((X:13) 60046 60029) ((X:2) 60046 60044 60043 60040 60039) ((X:4) 60046 60041 60040) ((  
X:21))  
(NIL) (NIL) (NIL) (NIL) (NIL) (NIL) (NIL) ((X:20) X:19 X:8 X:13 X:15 X:17 X:7) 60013 60018 60016 60019 60015  
60014 60012 60020 60023 60022 60027 60026 60025 60032 60024 60017 60013) (NIL) ((X:6) 60038 60037) ((X:18) 60037) (  
(X:9) X:14 X:5) 60036 60033 60035 60034) (NIL) (NIL) (NIL) ((X:10) X:16 X:12 X:3) 60031 60028 60030 60021 60045 60029) (  
NIL) ((X:1) X:11 X:2 X:4) 60030 60042 60046 60044 60043 60039 60046 60041 60040) ((X:21))  
LOCAL  
LOCAL ASSUMES (X:6) (X:1) X:11 X:2 X:4) SAME BODY)  
(NIL) (NIL) (NIL) (NIL) ((X:20) X:19 X:8 X:13 X:15 X:17 X:7) 60013 60018 60016 60019 60015 60014 60012 60020 60023  
60022 60027 60026 60025 60032 60024 60017 60013) (NIL) ((X:1) X:11 X:2 X:4 X:6) 60042 60044 60043 60039 60046 60041 6004  
0 60038 60037) ((X:18) 60037) ((X:9) X:14 X:5) 60036 60033 60035 60034) (NIL) ((X:10) X:16 X:12 X:3) 60031 60028 60030 600  
21 60045 60029) (NIL) ((X:21))  
LOCAL  
(SINGLEBODY ASSUMES (X:1) X:11 X:2 X:4 X:6) (X:18) SAME BODY)  
((X:10) X:16 X:12 X:3) 60031 60028 60030 60021 60045 60029) ((X:9) X:14 X:5) 60036 60033 60035 60034) (NIL) ((X:1) X:11 X:  
2 X:4 X:6 X:18) 60042 60044 60043 60039 60046 60041 60040 60038 60037) ((X:20) X:19 X:8 X:13 X:15 X:17 X:7) 60013 60018 6  
0016 60019 60015 60014 60012 60020 60023 60022 60027 60026 60025 60032 60024 60017 60013))  
LOCAL  
SNB  
RESULTS  
(BODY 1. IS X:10 X:16 X:12 X:3)  
(BODY 2. IS X:9 X:14 X:5)  
(BODY 3. IS X:1) X:11 X:2 X:4 X:6 X:18)  
(BODY 4. IS X:20 X:19 X:8 X:13 X:15 X:17 X:7)  
NIL

RESULTS FOR R9

R 9

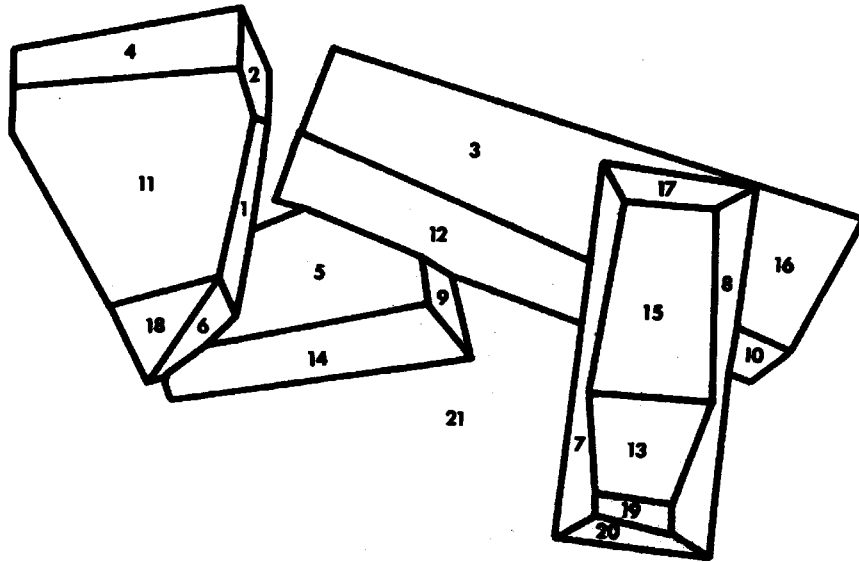


FIGURE 'R 9'

The four bodies were found.  
SINGLEBODIES was needed to join :18  
with :6-11-1-4-2.

R 9 T

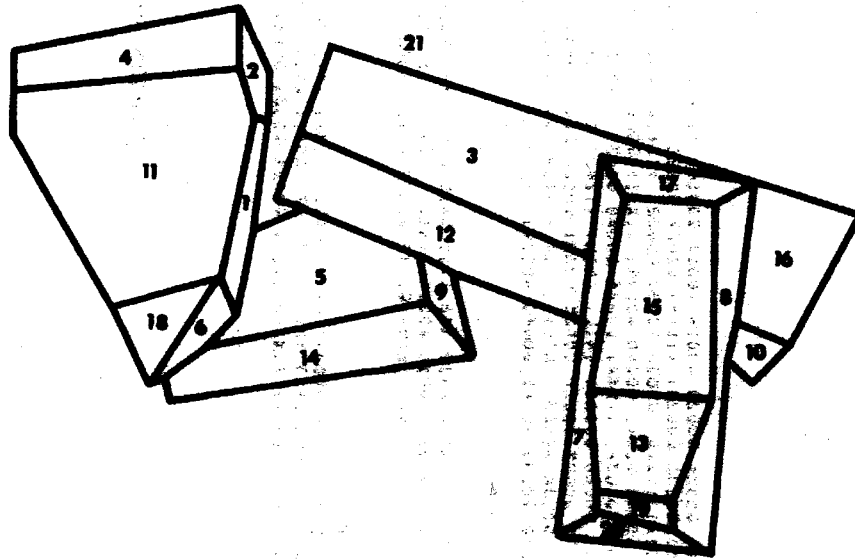


FIGURE 'R 9 T'

SINGLEBODIES joins :18 with the other portion of that body; LOCAL is needed to join :6 to that portion, and :6 with :10. Nevertheless, since :12 and :10 were not found to be the same face, body :16-10 is found, and Body :12-3.

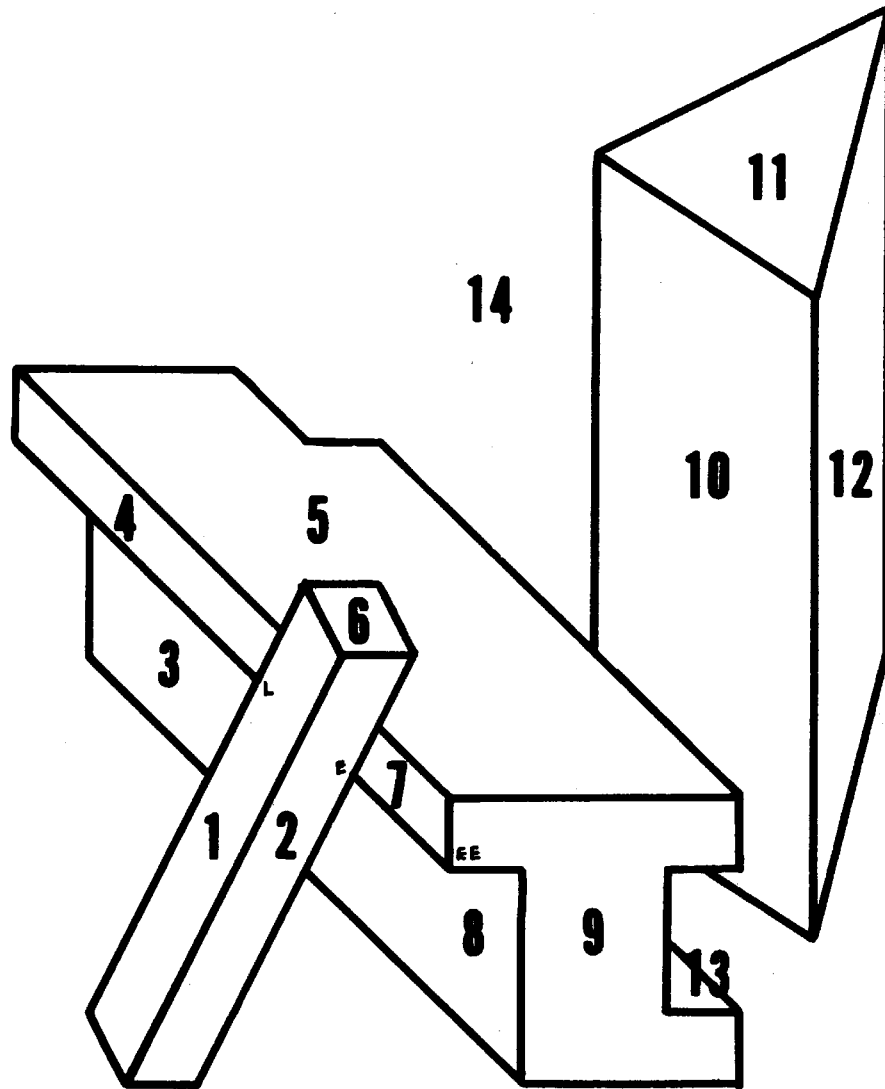


Scene TRIAL This scene has been analyzed in great detail in the section that describes the program SEE. Its links are found in graphic form in figure 'TRIAL - LINKS', or in written form (lists) in "RESULTS FOR TRIAL".

LOCAL had to join :13 with the remainder of that body.

ALFA 1968

**TRIAL**



**FIGURE 'T R I A L'**

SEE 58 ANALYZES TRIAL  
EVIDENCE  
LOCAL EVIDENCE  
TRIANG  
GLOBAL  
(NIL) ((11)) 60014 60013 60011 60010 ((112)) 60015 60014 60013 60012 ((113)) 60021 ((119)) 60022 60021 60020 60019 60017  
60016 ((110)) 60015 60012 60011 60010 ((113)) 60034 60025 60024 ((114)) 60033 60032 60026 60025 60023 ((116)) 60031 60030  
60029 60027 ((115)) 60026 60023 60022 60018 60017 ((117)) 60033 60032 60019 60018 60016 ((118)) 60034 60024 60020 ((112)) 60  
035 60031 60029 60026 ((114)) ((111)) 60035 60030 60026 60027))  
(NIL) (NIL) (NIL) ((113)) 60021 (NIL) ((111) 112 110) 60013 60015 60014 60013 60012 60011 60010 (NIL) (NIL) (NIL)  
(NIL) (NIL) ((11 19 15 17 13 1A) 60025 60021 60016 60026 60023 60022 60017 60033 60032 60019 60018 60016 60025 60034 60  
024 60020) (NIL) ((114)) ((116 12 11) 60027 60031 60029 60035 60030 60026 60027))  
LOCAL  
LOCAL ASSUMES ((13) ((14 19 15 17 13 18) SAME BODY)  
LOCAL  
(NIL) (NIL) ((14 19 15 17 13 1A 113) 60021 60026 60023 60022 60017 60033 60032 60019 60018 60016 60025 60034 60024 6002  
0 60021) ((111 112 110) 60011 60015 60014 60013 60012 60011 60010) (NIL) (NIL) ((114)) ((116 12 11) 60027 600  
31 60029 60035 60030 60026 60027))  
LOCAL  
((116 12 11) 60027 60031 60029 60035 60030 60026 60027) ((111 112 110) 60011 60015 60014 60013 60012 60011 60010)  
((114 19 15 17 13 18 113) 60021 60026 60023 60022 60017 60033 60032 60019 60018 60016 60025 60034 60024 60020 60021))  
LOCAL  
SMR  
RESULTS  
(BODY 1. 15 16 12 11)  
(BODY 2. 15 11 112 110)  
(BODY 3. 15 14 19 15 17 13 18 113)  
NIL

RESULTS FOR TRIAL

Scene ARCH SEE analyzes scene ARCH (see figure 'ARCH') with results displayed in 'RESULTS FOR ARCH'. This is an scene composed of many degenerate views of objects. It is an ambiguous scene (see section on Optical Illusions), in that several good interpretations are possible.

The program reports :7 and :17 as one body, which could be plausible. :16, :9 and :10 get reported as independent objects. In the scene from where this picture or line drawing was taken, :7, :17 and :16 were the vertical face of an object. :10 was the vertical face of another, :9 being its horizontal (top) face. In cases like this, in order to choose the "right" one of several possible interpretations, more information has to be supplied to the program, such as lighting, textures, color, etc.

No link was put by A between :3 and :29, or by UB between :5 and :19, because D and W are GOODTs. In one case, G provides with more links and causes :3-8-29-31 to be reported as one body, which is correct; in the other case, Q can not supply any links, and that body is split in two: :5-4 and :19-18. This is a mistake of GOODT, who accepts W as a genuine T. If this were not the case, the arrow UB would establish a link between :5 and :19, avoiding the mistake. GOODT could stand some improvement.

The body :22-23 was identified correctly.



# ARCH

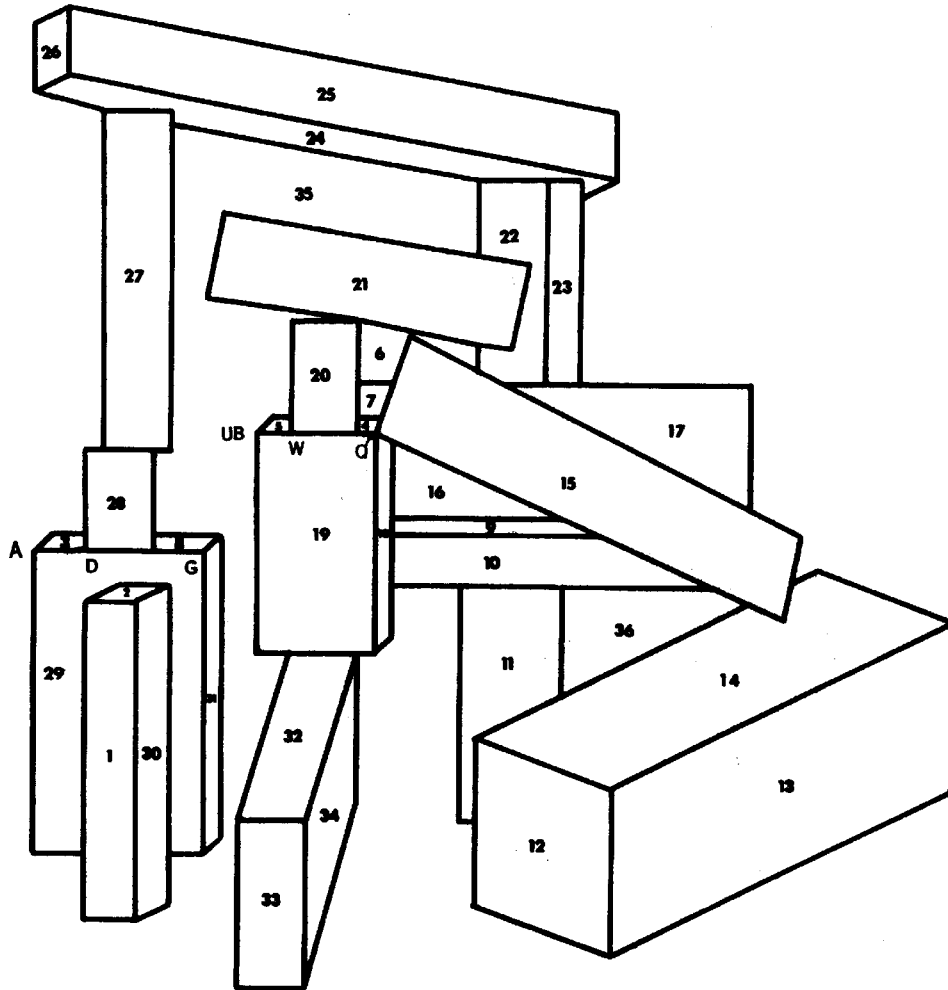


FIGURE "A R C H"

Ambiguous scene that could be correctly interpreted in several different manners. :7-17 was reported as a single body (see table 'RESULTS FOR ARCH'), and also :9.

The body :5-4-19-18 was split in two: :5-4 and :19-18, but not :3-8-29-31, which was counted as one body.



Scene HARD This scene consists of objects of the same shape, namely triangular prisms. All are correctly identified, including the long and twice occluded :3-21-22-23-24-28-29. :1-2-33 was also found. LOCAL had to be used to join :15 with :16, and also :11 with :12.

In an older version of the program, :7 was identified as a single body, and :6 as another, because they have no visible "useful" vertices to place links [Guzmán PISA 68]. Now SEE joins :6 and :7, because both are "GOODPALS". See "Operation of the Program; SMB"(page 99).

These scenes are sometimes obtained from a picture, so that they are the result of a perspective transformation. Some other scenes are drawn more or less in an orthogonal or isometric projection. SEE does not depend heavily in the type of projection; there are only a few heuristics that use notions of parallelism.

# HARD

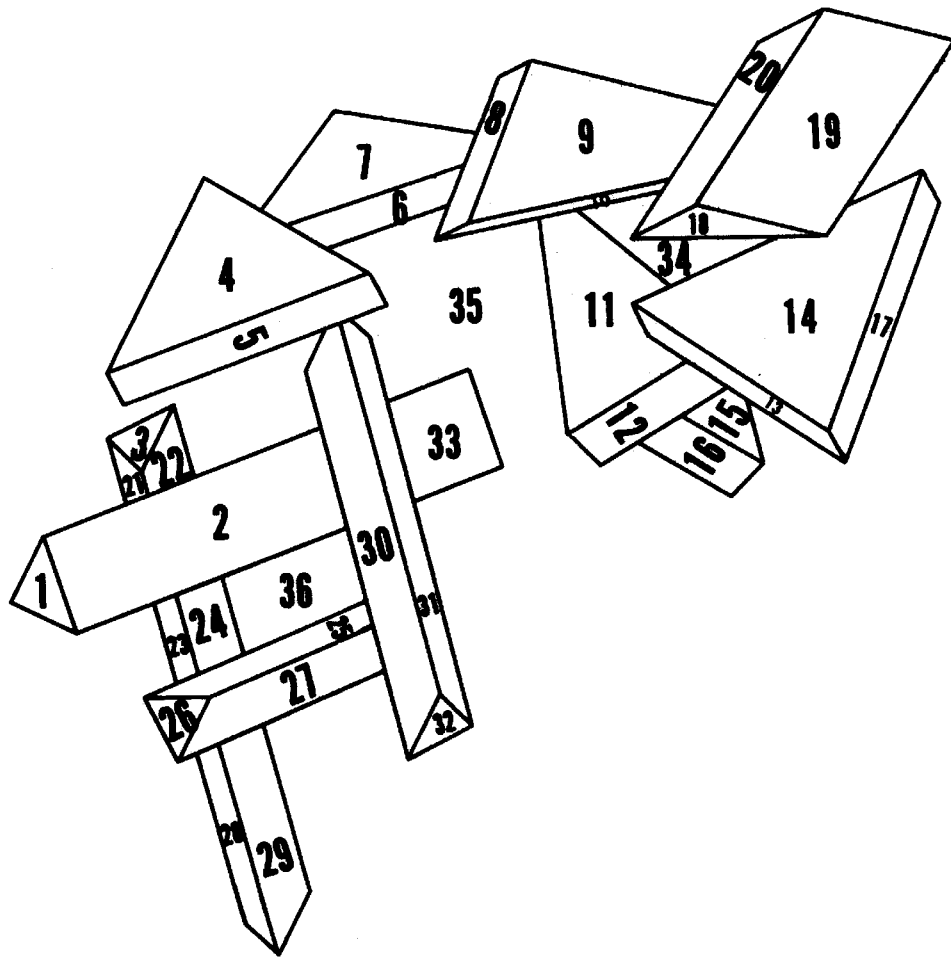


FIGURE 'H A R D'

All the bodies were correctly found.  
The most difficult was :6-7, since SMB  
had to join both regions, which do  
not have "useful" visible vertices.



Scene L4 The body :10-9 was reported isolated from :13-2-3, due to insufficiency of links. See comments to figure R17, also. The algorithm that localizes matching T's could stand improvement. It sometimes produces "bad links" such as between :4 and :13, and between :6 and :3, because it found two T's that looked like they were matching (this mistake did not happen, actually, because vertex R is not a T, but a fork!), EA and R in this case. The suggestion in page 173 will lessen, but not suppress, these "mistakes".

L 4

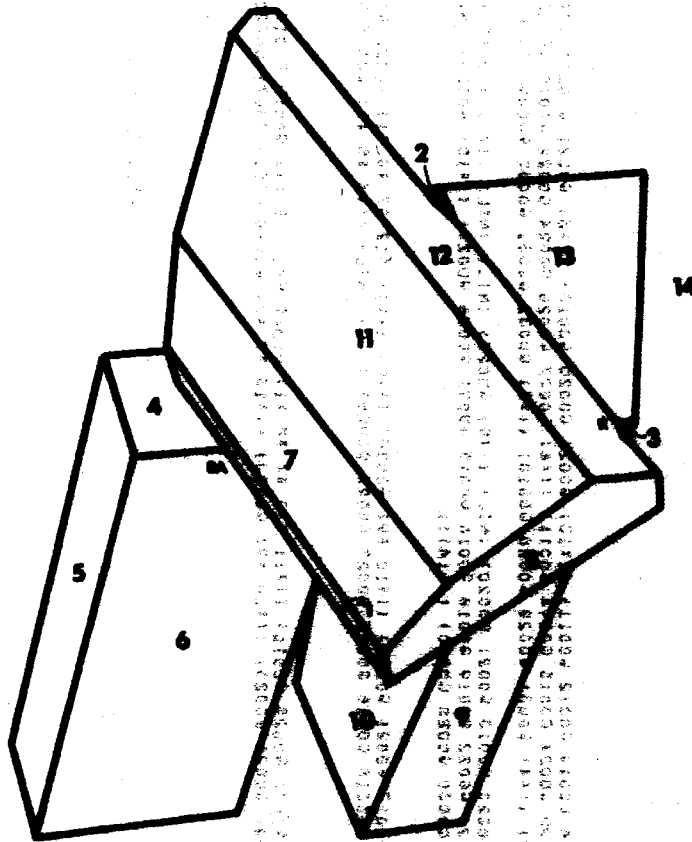


FIGURE 'L-4'

Body :2-3-13 was reported separated  
from body :10-9. Too few T-joints.

SEE 58 ANALYZES L4  
EVIDENCE  
LOCALEVIDENCE  
TRIANG  
GLOBAL  
(NIL) ((:2) G0013) ((:11) G0016 G0017 G0016 G0014 G0012 G0011) ((:13) G0021 G0020 G0013) ((:3) G0021 G0020) ((:12) G002  
2 G0019 G0017 G0012) ((:9) G0023) ((:7) G0025 G0024 G0015 G0014 G0011) ((:8) G0027 G0026 G0024 G0022 G0019 G0018 G0016 G  
0015) ((:11) G0027 G0026 G0025) ((:10) G0023) ((:4) G0031 G0029 G0028 G0010) ((:5) G0032 G0031 G0030 G0029) ((:6) G0032 G  
0030 G0028 G0010) ((:14))  
(NIL) ((:2) G0013) (NIL) ((:13 :3) G0020 G0013 G0021 G0020) (NIL) ((:9) G0023) (NIL) ((:11 :12 :7 :8 :1) G0  
022 G0017 G0012 G0015 G0014 G0011 G0026 G0024 G0022 G0019 G0018 G0016 G0015 G0027 G0026 G0025) ((:10) G0023) (NIL) (NIL)  
((:4 :5 :6) G0028 G0032 G0031 G0029 G0030 G0028 G0010) ((:14))  
LOCAL  
(LCAL ASSUMES (:9) (:10) SAME BODY)  
(NIL) ((:2) G0013) (NIL) ((:13 :3) G0020 G0013 G0021 G0020) ((:10 :9) G0023) (NIL) ((:11 :12 :7 :8 :1) G0022 G0017 G001  
2 G0015 G0014 G0011 G0026 G0024 G0022 G0019 G0018 G0016 G0015 G0027 G0026 G0025) (NIL) (NIL) ((:4 :5 :6) G0028 G0032 G00  
31 G0029 G0032 G0030 G0028 G0010) ((:14))  
LOCAL  
(SINGLEBODY ASSUMES (:13 :3) (:12) SAME BODY)  
((:4 :5 :6) G0028 G0032 G0031 G0029 G0030 G0028 G0010) ((:11 :12 :7 :8 :1) G0022 G0017 G0012 G0015 G0014 G0011 G0  
026 G0024 G0022 G0019 G0018 G0016 G0015 G0027 G0026 G0025) ((:13 :3 :2) G0020 G0013 G0021 G0020) (NIL))  
LOCAL  
SMB  
RESULTS  
(BODY 1. 15 :4 :5 :6)  
(BODY 2. 15 :11 :12 :7 :8 :1)  
(BODY 3. 15 :10 :9)  
(BODY 4. 15 :13 :3 :2)  
NIL

RESULTS FOR I4



Scene R4 The table 'RESULTS FOR R4' shows what happens when the tolerances are too large. Five bodies are found. Vertex B is considered to be a "T", and inhibits the links suggested by the Arrows R and A. As a result, :1 gets cut off ;7-9-5-10.

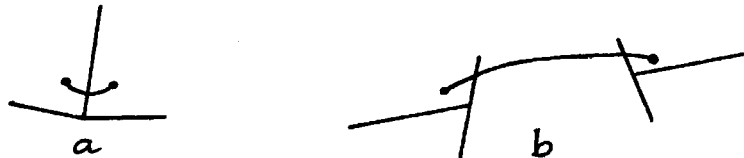
The way :2 gets isolated is as follows: T and AA claim to be matching T's, the link suggested by U is inhibited by Z (a Corner), and :2 gets disconnected from :3-4.

The correct solution is obtained after reducing the values of COLTO and SINTO to 0.05 and 0.005 (see listings; COLTO decides if two lines are colinear, SINTO if they are parallel), respectively. The results appear also in 'RESULTS FOR R4', and we can see now that only three bodies (the correct ones) are identified.

Suggestion Lines like the one below should be SUGGESTION "straightened" either by SEE or (better) by the preprocessor; for example, B K L N and D G H O in figure R17. See section 'On Noisy Input'.



Conservatism and Tolerance More strict tolerances do not make the program more conservative in all cases: the link in (a) fails to be placed if the program has too loose (large) tolerances, because A will be transformed into a "T" (it will be considered to be a "T"), losing the link; the link in (b) fails to be laid if the tolerances are too strict, because the T-joints will not be colinear.



In (a), links disappear if tolerances are too big; in (b), if they are too small. In both cases, conservative behavior (cf. page 212) appears.

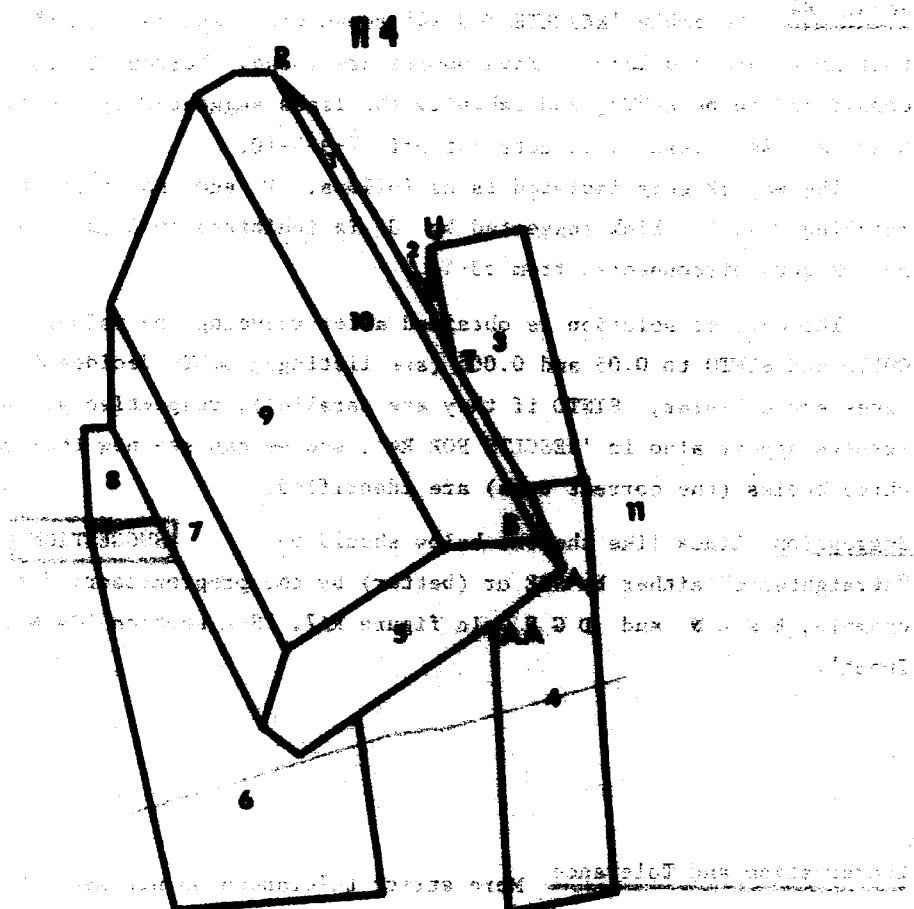


FIGURE: 'R4'

Either three or five bodies are found, according to the values of certain parameters. These scenes are "noisy" in the sense that the coordinates of the vertices depart from their "ideal" position by as much as one millimeter, or about 1% of the total size of the image, which is about one decimeter. This error is not large enough to affect long lines, but it may substantially change the direction of short segments.



Scene MOMO The long body :29-30-34-20-19 gets identified as follows: :29 and :30 get two links, and :30 with :19 also, so we have the nucleus :29-30-19. Two links (because of matching T's) join :34 with :20, to form nucleus :34-20. Regions :30 and :34 receive a strong link, by heuristic (g) of table 'GLOBAL EVIDENCE', and :19 with :20 by the same reason. That completes the body.

The fork that is common to :12, 13 and 14 puts a link between :12 and :13, but it is not enough to cause mis-recognition. A link is put by that same Fork between :13 and :14, as it should be, but the link between :12 and :14 is inhibited by NOSABO.

There is a program that finds regions of a scene belonging to the background, when not indicated as such in the input. For MOMO, the results of this program appear in page 131 .

# MOMO

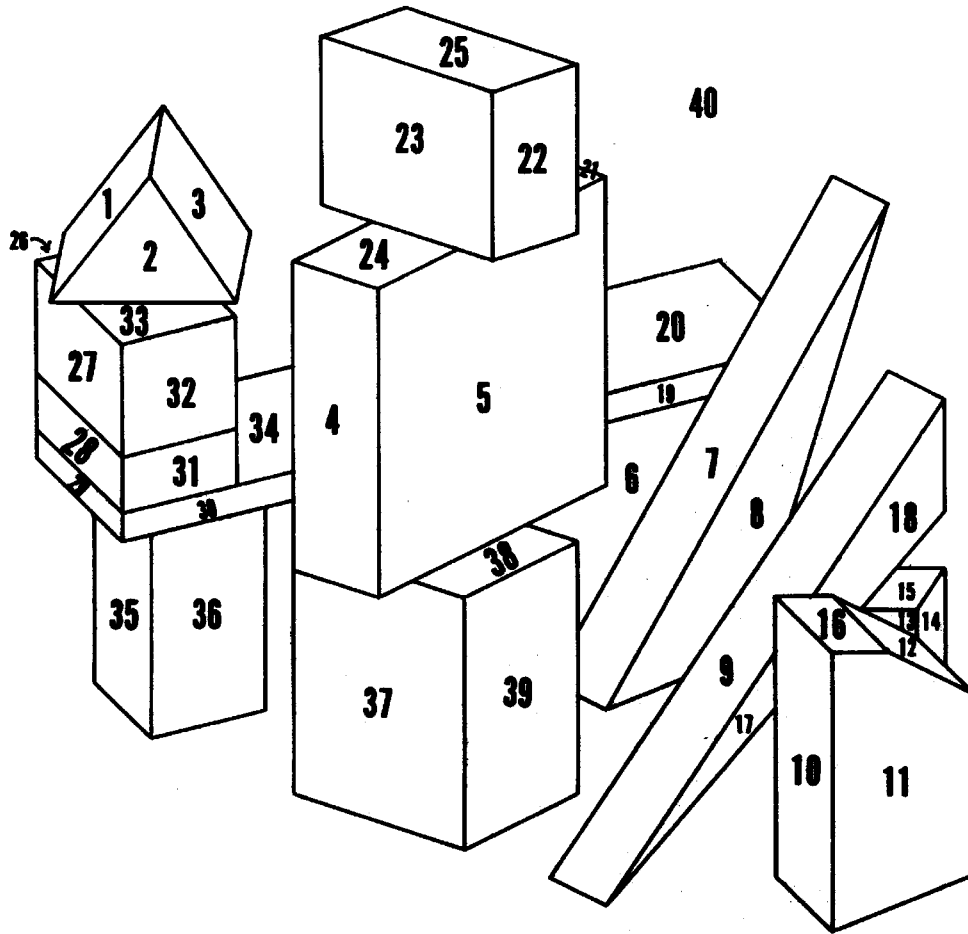


FIGURE 'M O M O'

All bodies are correctly identified.



Scene BRIDGE Region :10 gets a strong and a weak link with :4, and that is enough to join them. The same is true for :7.

The links of scene BRIDGE (see 'RESULTS FOR BRIDGE') are discussed and displayed in pages 95-98, figures 'LINKS-BRIDGE' (page 95), 'NUCLEI-BRIDGE' (page 96), 'NEW-NUCLEI-BRIDGE' (page 97), and 'FINAL-BRIDGE' (page 98).

Because RA and SA are matching T's, two wrong links are placed: one between :22 and :28, and the other between :21 and :29. This is not enough to cause an error, because we need two mistakes (two reinforcing each other), two wrong strong links, to fool the program. But that could happen.

It is interesting to note the way in which the long "horizontal table" :25-24-21-27-9-12 was put together. To this effect, see figures 'LINKS-BRIDGE' and 'NUCLEI-BRIDGE'.

Vertex JB produces only one link between :5 and :8. Vertex KB inhibits the link (through NOSABO) between :8 and :9, and the link between :5 and :9 gets inhibited by S, because it is a T (cf. NOSABO, page 82).

The concave object :7-6-5-4-8-10-11 gets properly identified. We may say that, in general, the more "crooked" or complicated an object is, the easier will be for SEE to isolate it, because there will be many vertices contributing with valuable links.

No mistake was made by SEE on BRIDGE; its eight bodies were correctly identified (see 'RESULTS FOR BRIDGE', page 181).

The background of 'BRIDGE' was also correctly isolated; see that in page 230, section 'On background discrimination by computer'.

# BRIDGE

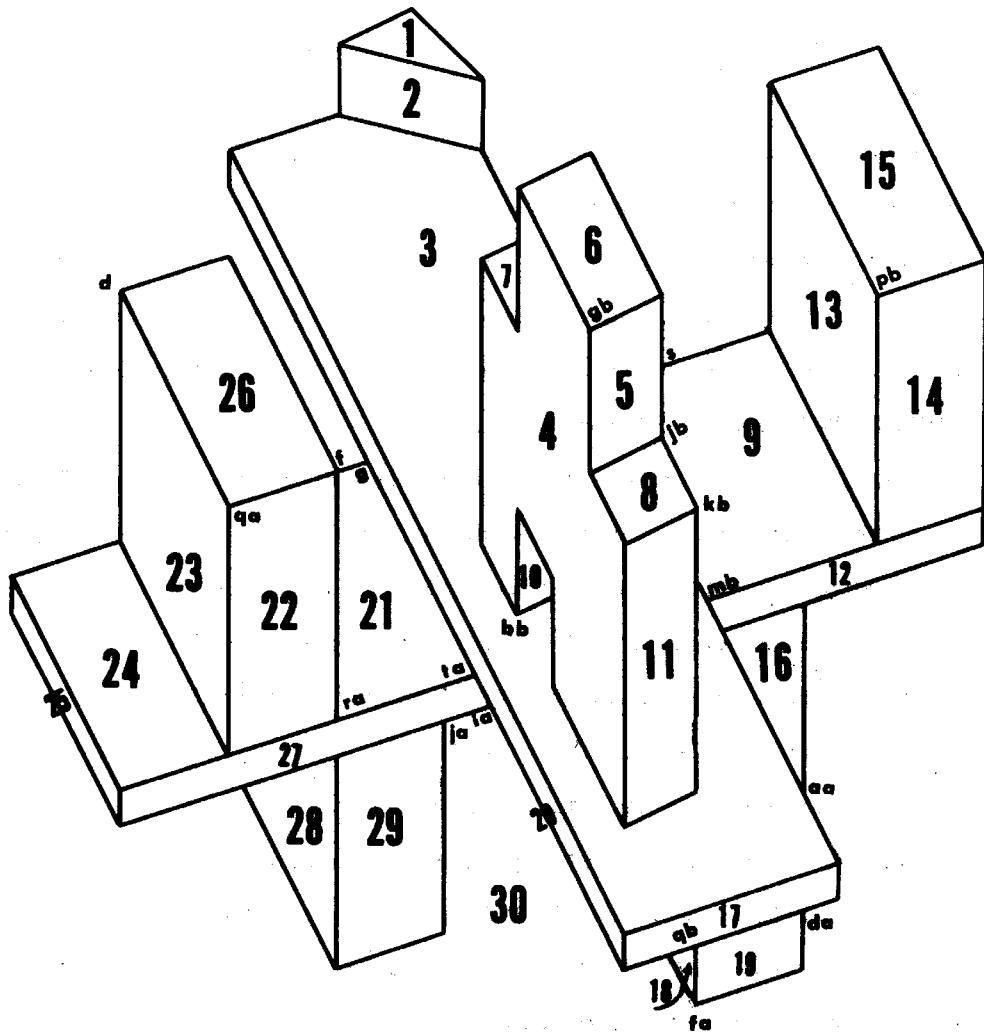


FIGURE 'B R I D G E'



SEE 56 ANALYZES BRIDGE  
EVIDENCE  
LOCAL EVIDENCE  
TRIANG  
GLOBAL  
(NIL) ((18) 60020 60016 60017 60016) ((17) 60023) ((110) 60024) ((111) 60025 60019 60016) ((120) 60036 60031) ((18  
29) 60036 60030) ((127) 60039 60037 60036 60039 60015) ((118) 60041) ((119) 60042 60041) ((117) 60043 60040 60027 60026)  
((116) 60042) ((112) 60039 60015 60013) ((114) 60044 60012 60011) ((115) 60045 60044 60012 60010) ((113) 60045 60011 60  
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3 60021 60019) ((111) 60049 60048) ((12) 60049 60048) ((12) 60050 60043 60028 60027) ((120) 60050 60040 60028 60026) ((12  
1) 60051 60030 60029 60014) ((122) 60052 60034 60033 60031) ((124) 60053 60052 60034 60032) ((123) 60053 60033 60032) ((  
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0048) (NIL) ((117 13 120) 60026 60043 60027 60050 60040 60028 60026) (NIL) (NIL) ((122 126 123) 60033 60031 60052  
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(BODY 4. 18 11 12)  
(BODY 5. 18 114 115 113)  
(BODY 6. 18 119 118 116)  
(BODY 7. 18 129 128)  
(BODY 8. 18 116 111 115 116 14 110 17)  
NIL

RESULTS FOR BRIDGE

## DISCUSSION

We have described a program that analyzes a three-dimensional scene (presented in the form of a line drawing) and splits it into "objects" on the basis of pure form. If we consider a scene as a set of regions (surfaces), then SEE partitions the set into appropriate subsets, each subset forming a three-dimensional body or object.

The performance of SEE shows to us that *it is possible to separate a scene into the objects forming it, without needing to know in detail these objects*; SEE does not need to know the 'definitions' or descriptions of a pyramid, or a pentagonal prism, in order to isolate these objects in a scene containing them, even in the case where they are partially occluded.

The basic idea behind SEE is to make global use of information collected locally at each vertex: this information is noisy and SEE has ways to combine many different kinds of unreliable evidence to make fairly reliable global judgments.

The essentials are:

- (1) Representation as vertices (with coordinates), lines and regions
- (2) Types of vertices.
- (3) Concepts of links (strong and weak), nuclei and rules for forming them.

The current version of SEE is restricted to scenes presented in symbolic form.

Since SEE requires two strong evidences to join two nuclei, it appears that its judgments will lie in the 'safe' side, that is, SEE will almost never join two regions that belong to different bodies. From the analysis of scenes shown above, its errors are almost always of the same type: regions that should be joined are left separated. We could say that SEE behaves "conservatively," especially in the presence of ambiguities.

Divisions of the evidence into two types, strong and weak, results in a good compromise. The weak evidence is considered to favor linking the regions, but this evidence is used only to reinforce evidence from more reliable clues. Indeed, the weak links that give extra weight to nearly parallel lines are a concession to object-recognition, in the sense of letting the analysis system exploit the fact that rectangular objects are common enough in the real world to warrant special attention.

Most of the ideas in SEE will work on curves too.

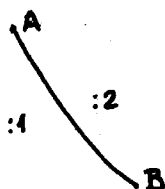
## CURVED OBJECTS

How to extend SEE to work with objects possessing curved surfaces.

Introduction and Summary Most of the heuristics that establish links at each vertex are unconcerned if the edges are curved or straight; a few heuristics get affected: those that use the concepts of collinearity and parallelism.

Thus, it is necessary to redefine and broaden these concepts.

1. A slight generalization is obtained if each segment is represented as having two slopes (initial and final). The functions PARALLEL and COLINEAR of SEE are already modified for this (cf. listings).



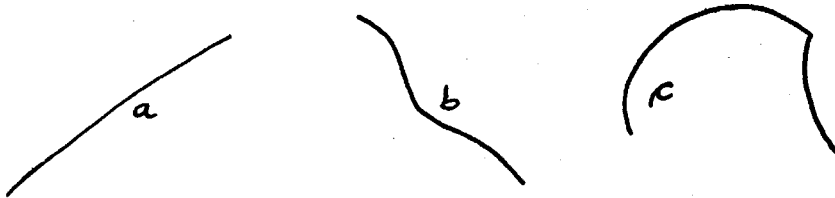
SEE does not care if the line joining two vertices is a straight or curved line. The information about the segment A-B that is relevant to SEE is:

- (a) There is a line between vertex A and vertex B.
- (b) The coordinates of A and B.
- (c) The segment A-B separates region :1 from :2.

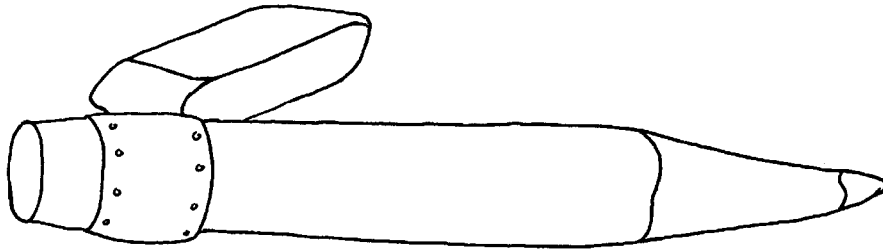
2. Attempts to take limited account of the shape of the segment carry us to

(a) gently bent segments (definition) are those with bounded slope [Bounded curvature will lead to another definition].

A quasi-rectilinear object has faces, vertices and gently bent edges or segments; it is expected that SEE will work well for them. We should try some scenes. SUGGESTION

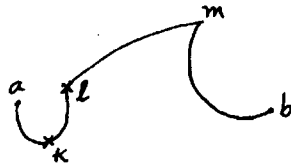


a, b: gently bent segments. c: non-gently bent segment. A gently bent segment has a slope that at any point of the segment does not differ more than epsilon from the mean slope of the segment. All slopes fall in an interval around the mean slope. Gently bent segments form quasi-rectilinear objects.



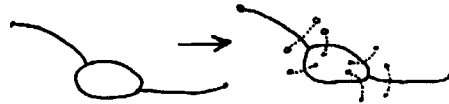
Quasi-rectilinear objects. It is expected that SEE will work well for them.

- (b) partition of a non-gently bent segment into several gently bent. Many of the bodies have vertices and curved edges, but the bodies are not quasi-rectilinear (a piece of chewed gum, leaves of a tree). By breaking the edges into gently bent sub-segments, they become quasi-rectilinear bodies. The breaks will occur in points where the curvature is large. There has to be devised away to break a segment in a unique manner. To avoid breaking a body into two by the introduction of these artificial vertices, we propose to introduce also artificial links between regions, to account for the artificial vertex.



The non-gently bent segment  $ab$  gets broken into gently bent segments  $ak, kl, lm, mb$ , by the artificial introduction of "new" vertices  $k, l, m$ .

Here, the introduction of additional vertices has to be accompanied by 'artificial' or reinforcing links, to preserve the individuality of the body (of the owner of such vertices).

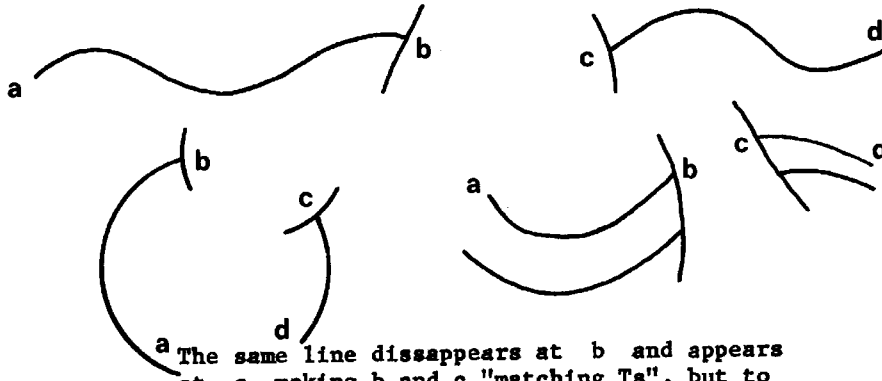


3. More complete consideration of the shape of the segments is obtained as follows:

- (a) For parallelism, by requiring that two segments be parallel only if one is a translation of the other. Generally, this is a comparison that takes a time proportional to the length of the segment. Chain encoding {Freeman} {Conrad} is suggested.

(b) For colinearity, by discovering properties or features that "carry through" or are common. Among these are:

1. Mathematical "regularity" of the segments. Both segments are described by the same or similar polynomials, etc.
2. Heuristic properties: there must exist properties which will select with high probability the "right" continuation.
3. Outside of the set of geometric properties, we have color, texture, etc.



The same line disappears at b and appears at c, making b and c "matching Ts", but to discover this fact it is necessary to have a concept of "good continuation" or "good contour".

Alternatively, we may forget these properties here and include them into models of our curved objects, but then we are forced to make searches in our scene like those made by DT or TD [my M.S. Thesis].

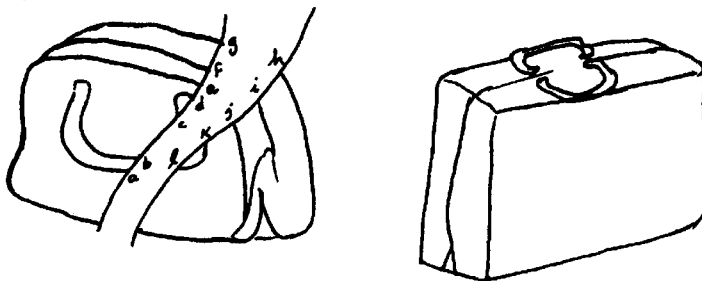


Fig. 'S U I T C A S E S'

Heuristic properties of segments (yet to be determined) could select a "correct" match for endings a, b, ..., k, l.

4. Bodies with no edges and vertices are in principle easily identified by SEE. See fig. 'FRUIT'.

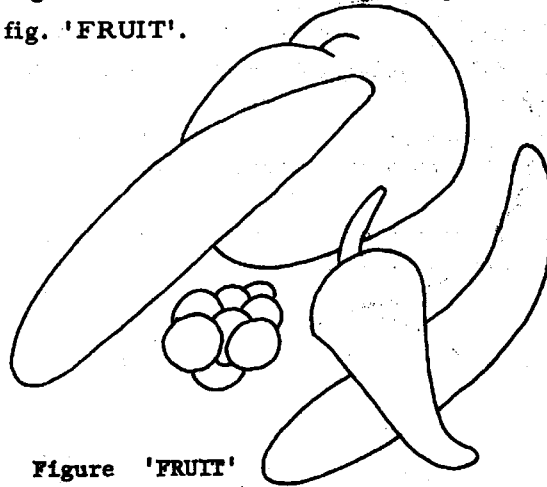


Figure 'FRUIT'

The bodies have no curved edges, and no vertices. The entire surface is smooth; no sharp edges or pointy corners. Examples: an inflated balloon, a frankfurt, a face, a cloud.

It is doubtful that we could do something here with SEE. We could try to postulate "artificial" vertices, using stereo perhaps, at the points where the 3-dim curvature is large, and then postulate lines between such vertices. This looks bad.

Or we could reason as follows: since these objects do not have vertices or edges, then the only vertices appearing in the scene must separate two bodies. They will be mainly T-joints. (cf also page 46)

In principle, separation into bodies looks promising, but recognition (the answer to "what is the name of this object?") seems difficult. Nevertheless, it is not clear that with such a simple set of heuristics we could work successfully with objects as complicated as a human face, a blob of falling water, an amoeba, the surface of the sea (?).

At some point, we have to know what we want. As the complexity increases, the concept of "body" depends less and less in geometrical properties (disposition of edges, vertices, ...) and more and more on purpose (Is a skeleton an object? Or perhaps the femur bone alone? The answer varies with our intention -- with the context).

Thus, models are necessary again.

See also 'Do not use over-specialized assumptions. . .', page 252.

## APPENDIX TO SECTION ON CURVE OBJECTS

This appendix may be omitted in a first reading.

Requirements for the preprocessor The preprocessor that feeds data

to SEE has to find only:

1. The lines of the scene.
2. The vertices.
3. The local slopes at each vertex.
4. See also comments to figure R17.
5. Illegal scenes (page 2(7)) should be detected by the preprocessor.

REQUIREMENTS  
FOR THE  
PREPROCESSOR

How bad will curved objects be In objects where the curves edges are gently bent, SEE will work fairly well. The more an edge departs from its rectilinear equivalent, the worse SEE will work; T-joints will be difficult to find, a FORK may transform into a 'T', etc. (I am talking about the current SEE, described in the listings).



Additional information could be used So far, we are trying to identify objects on the basis of form alone, i. e., geometrical considerations. This is asking a machine to do more than a human being does. Ambiguous line drawings, such as ARCH, become unambiguous when we introduce shading, lighting, texture, color, etc. All of these properties could be used by SEE. In fact, consider how easy it would be to identify bodies if each one of them is of different color (and we could sense that fact).

Psychological evidence Knowledge of the algorithms used by human beings for shape continuation (page 188) is relevant. We quote from Krech and Crutchfield {1958}:

**Grouping by Good Form.** Other things being equal, *stimuli that form a good figure will have a tendency to be grouped.* This is a very general formulation intended to embrace a number of more specific variants of the theme, traditionally classified as follows.

1. *Good continuation.* The tendency for elements to go with others in such a way as to permit the continuation of a line, or a curve, or a movement, in the direction that has already been established (see Fig. 37c).

2. *Symmetry.* The favoring of that grouping which will lead to symmetrical or balanced wholes as against asymmetrical ones.

3. *Closure.* The grouping of elements in

such a way as to make for a more closed or more complete whole figure.

4. *Common fate.* The favoring of the grouping of those elements that move or change in a common direction, as distinguished from those having other directions of movement or change in the field.

It seems plausible to consider that the percepts resulting from all of the above determinants would be such as to meet the criterion of a good figure, that is, one that tends to be more continuous, more symmetrical, more closed, more unified.

Now the reader will see that a difficulty with this general proposition regarding grouping centers on the crucial phrase "good figure." How can we know which

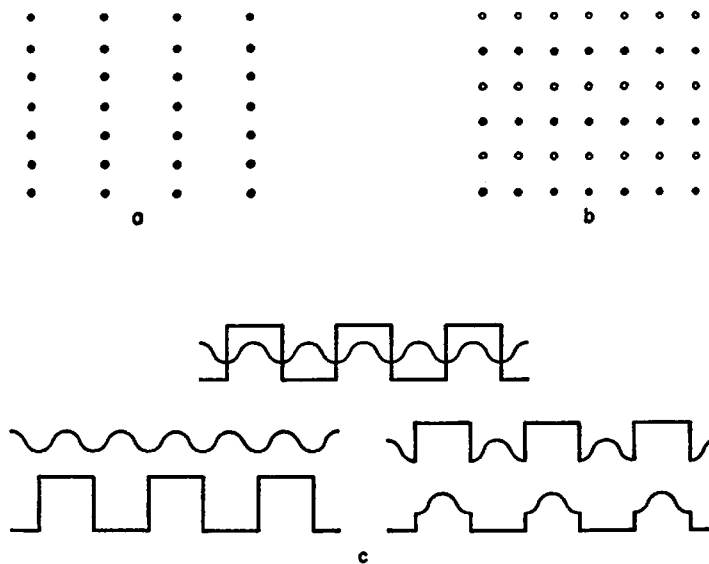


FIG. 37. Examples of grouping. In *a*, the dots are perceived in vertical columns, owing to their greater spatial proximity in the vertical than in the horizontal direction. In *b*, with proximity equal, the rows are perceived as horizontal, owing to grouping by similarity. In *c*, the principle of good continuation results in

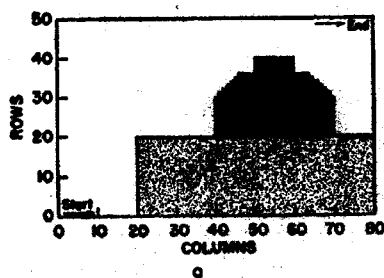
seeing the upper figure as made up of the two parts shown to the left below, even though logically it might just as well be composed of the two parts shown to the right below, or indeed of any number of other combinations of two or more parts. (Adapted from Wertheimer, 1923.)



## BOX 21

### How to Measure "Goodness"

Attneave has made an ingenious experimental attack on the problem of measuring the "goodness" of a figure. The subject is given a sheet of graph paper composed of 4,000 tiny squares (50 rows by 80 columns). His task is to guess whether the color of each successive square is black, white, or gray. The experimenter has in mind what the completed figure will look like (fig. a).



Without knowing what the completed figure will be, the subject starts by guessing the square in the lower left corner. When he has correctly identified the color, he moves on to guess the next square to the right. He continues this process to the end of the row and then starts on the left end of the next row above. In this manner he successively guesses each of the 4,000 squares.

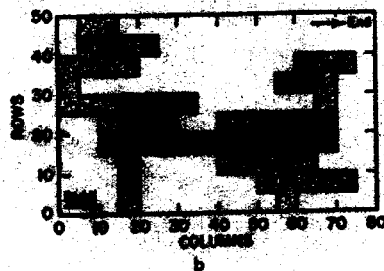
On the average, Attneave's subjects made only 15 to 20 wrong guesses for the entire figure. How was this possible? The answer is that the figure was deliberately designed so that knowledge of part of the figure was sufficient to enable the subject to make fairly valid predictions about the remainder of the figure. This was accomplished by making all the white squares contiguous with one another, and similarly the black and the gray squares. Moreover, the con-

tours separating the white, black, and gray areas are simple and regular. Where the figure tapers, it tapers in a regular way. And it has symmetry; after exploring one side, it is easy to predict the other side. Thus, the subject having discovered that the first few squares are white continues to guess white, and he is correct until he hits the gray contour at the 20th column. After one or two errors, he then continues to guess gray. On the next row above, he tends to repeat the pattern of the first.

All these factors of compactness, symmetry, good continuation, etc., are aspects of what is implied by a "good figure." Thus an objective measure of the "goodness" of a figure is the ease with which the subject can predict its total form from minimal information about a part.

Other figures can be similarly tested. For example, figure b would prove to be a less "good" figure because the number of errors in guessing would be larger.

Attneave's particular method will not, of course, apply to all kinds of figures or all kinds of perceptual organizations. But it does demonstrate that there are ways in which "goodness" can be objectively determined.

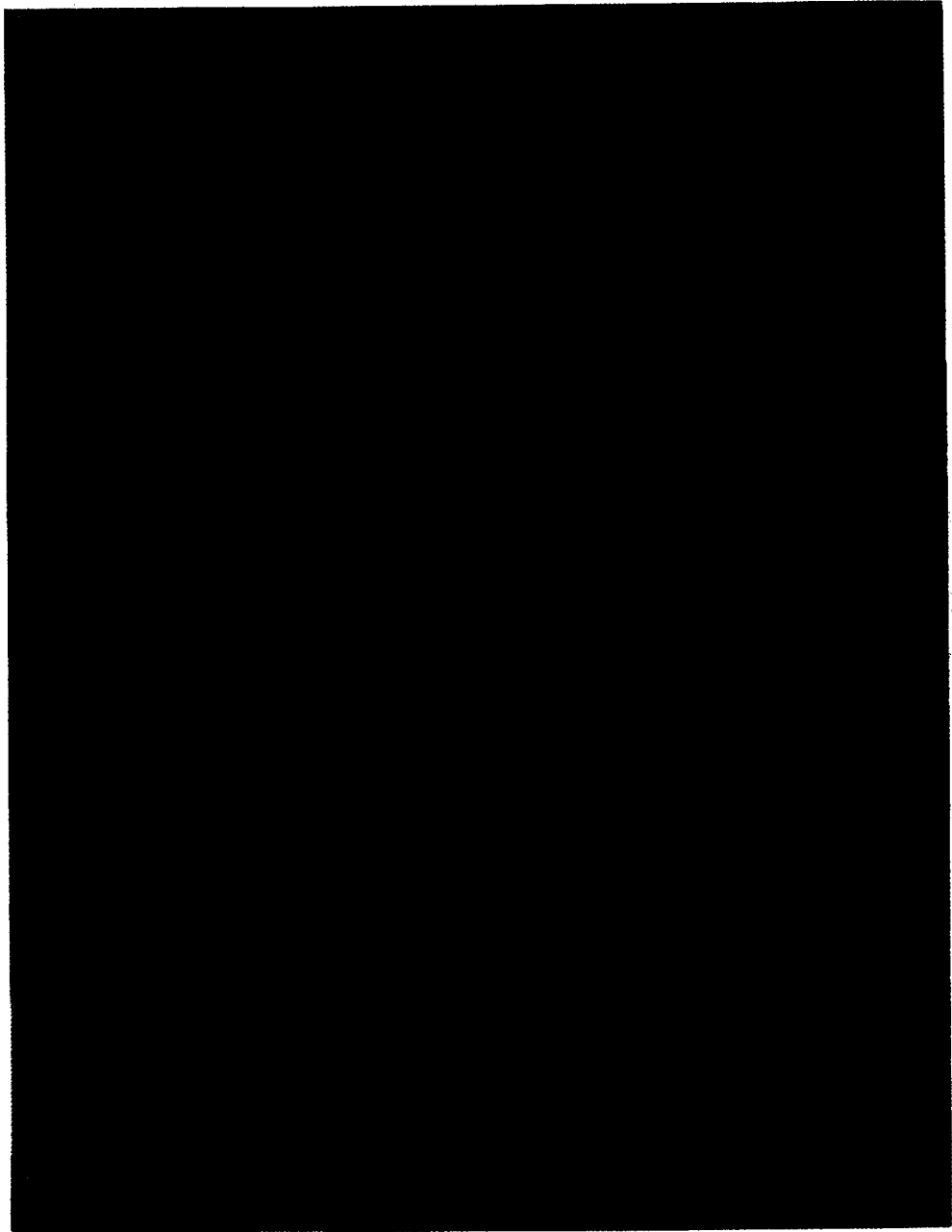


ATTNEAVE, F. 1954. Some informational aspects of visual perception. *Psychol. Rev.*, 61, 182-93.

configuration of stimuli is "better" than another?

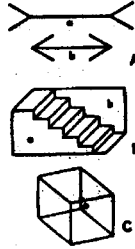
To escape from this difficulty, we need to have *independent* criteria of what is a good figure. Some approach can be made to this; for instance, in the case of "symmetry" there are objective rules we can apply to determine the relative symmetry of various figures. The same is true of simple cases of "closure." (See Box 21 for a relevant experiment.)

But we are far from being able to state such criteria when we deal with the highly complex configurations of our normal perceptual experience. Part of the difficulty stems from the fact of individual differences among perceivers. One man's mess may be another man's order. And this may reflect the important role of *learning and past experience* in the genesis of "good figure."



## ON OPTICAL ILLUSIONS

**il-lu-sion** \i-l'u-zhon\ *n* [ME, fr. MF, fr. LL *illusio*, *illusio*, fr. L, action of mocking, fr. *illusus*, pp. of *illudere* to mock at, fr. *ill-* + *ludere* to play; mock — more at LUDICROUS] 1 *a* *obj*; the action of deceiving *b* (1); the state or fact of being intellectually deceived or misled; MISAPPRHENSION (2); an instance of such deception 2 *n* (1); a misleading image presented to the vision (2); something that deceives or misleads intellectually *b* (1); perception of something objectively existing in such a way as to cause misinterpretation of its actual nature (2); MALLUCINATION 1 (3); a pattern capable of reversible perspective 2; a fine plain *unapparent* bobbinet or tulle usu. made of silk and used for veils, trimmings, and dresses *SYM see* DELUSION — *il-lu-sion-ary* \i-l'u-zho-n-er-ē\ *adj* — *il-lu-sion-ary* \i-l'u-zho-n-er-ē\ *adj*



optical illusions: fig. A: *a* equals *b* in length; fig. B: either side *a* or side *b* may appear longer the observer; fig. C: *a* may be regarded as either the near or the far corner of the block

Given the nature of SEE, we will restrict the meaning of 'optical illusion' to illusions formed by solids, that is, ambiguities or inconsistencies when we (or the program SEE) try to find 3-dim bodies in a scene; thus, the Müller-Lyer illusion ("A" in the topmost figure) is not considered.

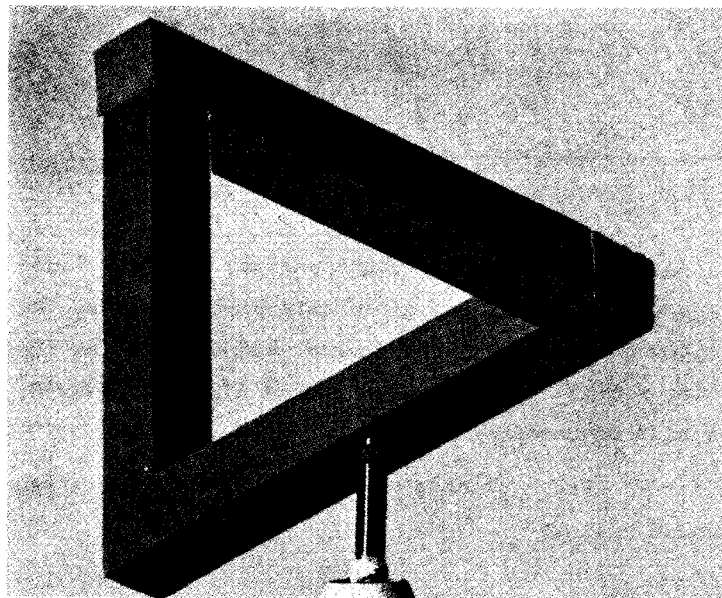
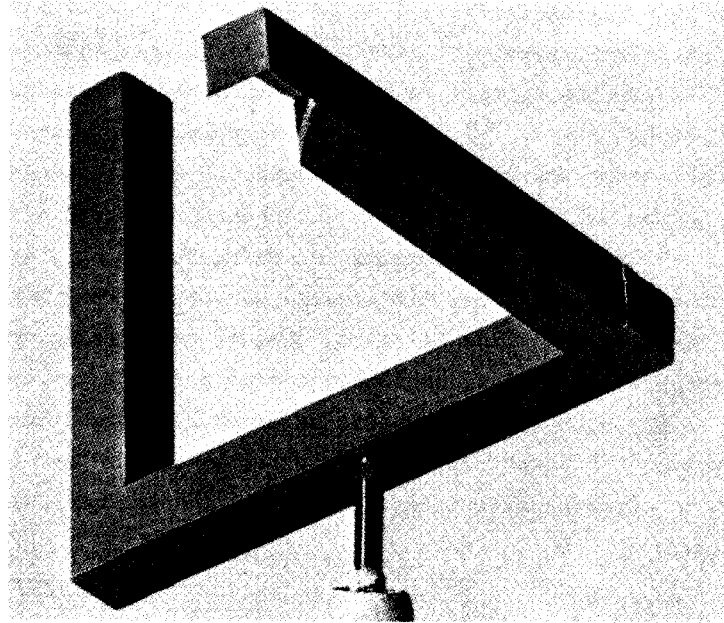
Three kinds of illusions According to this, we may elementarily classify the "scenes that are unlikely to occur" (that is, those that are not "standard" or "normal") in three types:

- == Possible but no "good" interpretation.
- == Ambiguous -- several good interpretations.
- == Impossible: without interpretation.

Like POLYBRICK {Guzmán}, SEE is not specifically designed to handle optical illusions. It was primarily designed to analyze "real world" scenes; hence, an input scene that produces an illusion (in a human) is not likely to occur as input to SEE. Nevertheless, in the same way that we may overtest a program for square roots by asking for the square root of 'APPLE',  $\sqrt{\text{APPLE}}$ , we may test SEE with some ambiguous scenes. Let us see what happens.


POSSIBLE BUT NO "GOOD" INTERPRETATION Some objects do not 'make sense' because they violate rules that most objects obey. Nevertheless, it





ACTUAL IMPOSSIBLE TRIANGLE was constructed by the author and his colleagues. The only requirement is that it be viewed with one eye (or photographed) from exactly the right position. The top photograph shows that two arms do not actually meet. When viewed in a certain way (*bottom*), they seem to come together and the illusion is complete.

(From Gregory).

One of the strong rules used by humans is that objects whose pictures show straight lines have indeed straight edges; another strong rule is to assume the corners to be like the corners of a cube (faces meeting at right angles)  . Under these rules, the above triangle does not make sense and people will classify it as an "impossible" object ('VARIANT' will be an "impossible" object; Penrose's Triangle will be "3 sticks forming an impossible configuration or scene; "mounted in a funny way"; can not be seen as representing a single object lying in space). For instance, Gregory [Scientific American] tries to explain that the triangle has a real 3-dim object as originator, by constructing a body consisting of three rectangular parallelepipeds ("bricks") joined at right angles, and then taking a picture from a special direction, so that the free ends a and b seem to touch:

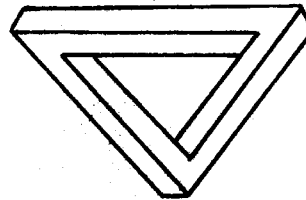
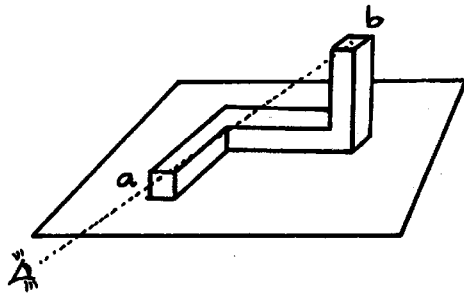


Fig. 'VARIANT'

These rules (faces meet at right angles; straight lines mean straight edges) are deeply ingrained into people, but nature does not need to follow them always. The Penrose Triangle can be obtained by photographing a 3-dim triangle with curved edges and skewed corners, where each side touches the other two.

SEE finds three objects in figure 'Penrose Triangle.' Other examples follow.

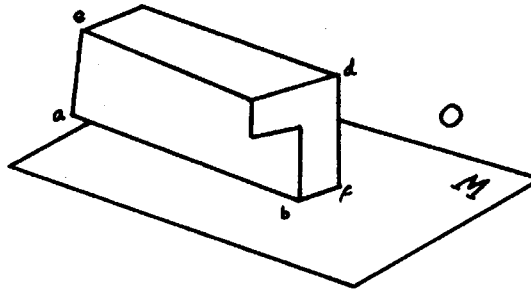


Figure 'B L A C K'

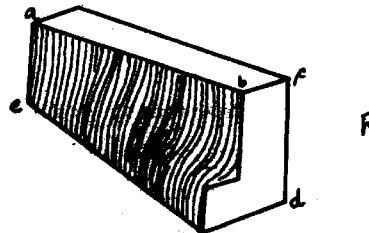
People assume that faces meet at right angles, and this object violates that rule, making it "impossible" or odd-looking.

It is possible to construct object 'BLACK' with planar faces. See figure 'TEST OBJECTS' page 209. SEE finds one body in 'BLACK'.

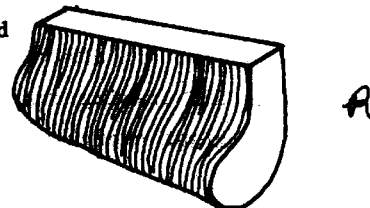
The object at right looks impossible if we assume all faces to be flat. If face *aeb* is curved, object is plausible. *R* is its reflection on mirror *M*, and *Q* a smoother version of *R*. *Q* looks "normal"; by deforming *Q* we could obtain *R*.



Unlike humans, SEE does not hold these "very common rules" as inviolable; SEE does not have any special problems with these "strange but true" objects.



A misleading suggestion of superiority should not be concluded from these rare cases; in other situations SEE makes mistakes that a human being does not (see figure 'SPREAD').



Of course, SEE holds its own rules (for example, those of table 'Global Evidence') as inviolable; hence, given a "rare enough scene" it will make mistakes (cf. assertion in page 5', after the Theorem). This is a similarity of behavior, I think, between people and SEE -- each one follows rather rigidly a small set of rules. (see also conclusion at end of section).

Besides, often humans will see the 'impossible' object as an object, doing SEE's job just as well.

Figure  
'STAIRCASE'

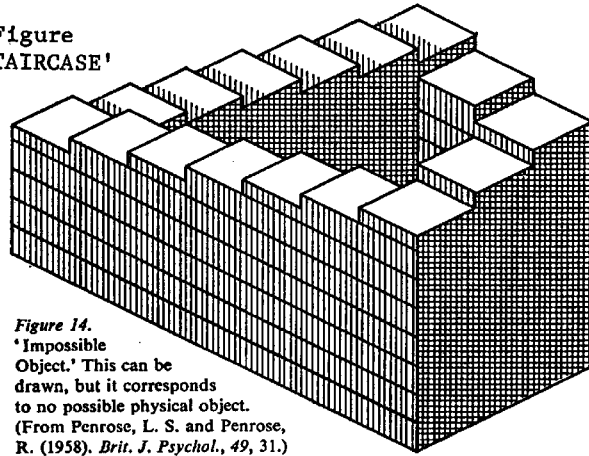
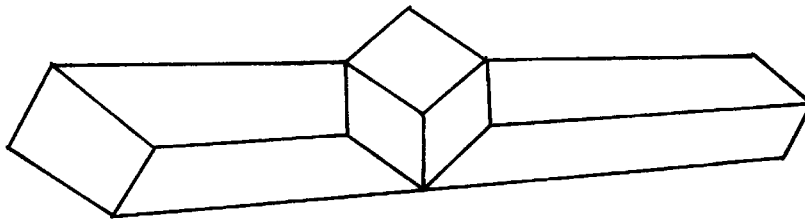


Figure 14.  
'Impossible  
Object.' This can be  
drawn, but it corresponds  
to no possible physical object.  
(From Penrose, L. S. and Penrose,  
R. (1958). *Brit. J. Psychol.*, 49, 31.)  
(caption by Gregory)

The "always descending staircase." [Gregory, in {Foss}]  
The caption is wrong, this object could be constructed in the real world,  
if some surfaces are curved and/or the faces at the corners do not meet  
at right angles. Example of an object "possible but without 'good'  
interpretation." See also Metatheorem on page 39. Again, the "impo-  
ssibility" or oddness of 'STAIRCASE' comes from assuming the rules  
'straight lines in the drawing correspond to straight edges in 3-dim'  
and 'faces meet at right angles, like corners of a cube' inviolable.

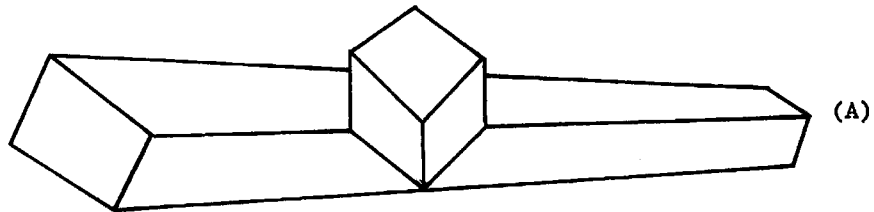
AMBIGUOUS - TWO GOOD INTERPRETATIONS

These are scenes that can be interpreted in several correct (non-paradoxical) manners, which are also "sensible" (as opposed to the Trivial Solution of page 41). For instance, an scene like

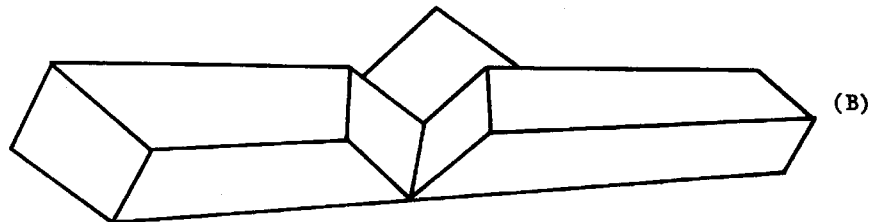


that can be interpreted as



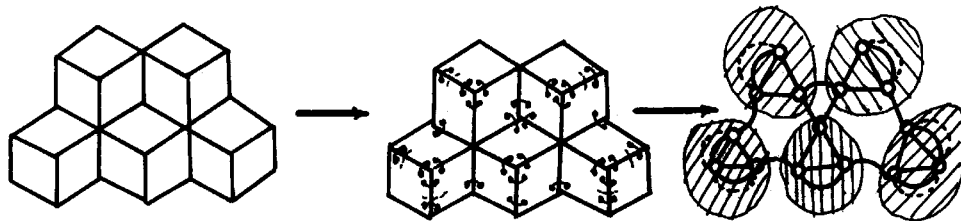


or as

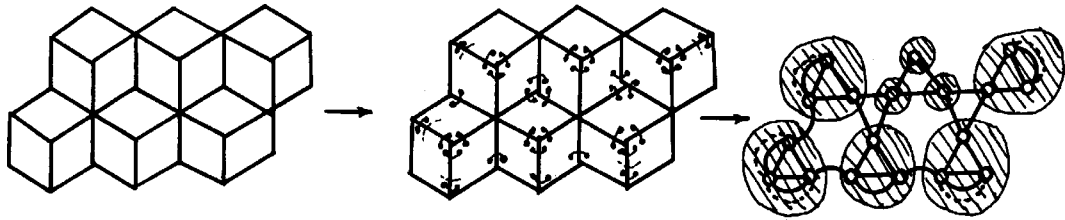


SEE will generally give one of the possible answers, although not necessarily the one preferred by humans. In this example, SEE chose ( B ).

The following scene, locally ambiguous, is correctly parsed by our program.



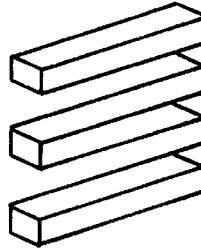
Sometimes, the conservatism of SEE and its partial insufficiency to make very global judgements will leave a body unconnected; for instance, the three faces of one cube below will be reported each one as a separate object, due to insufficient links.




IMPOSSIBLE: WITHOUT INTERPRETATION

Images that can not be product of photographing (projecting) a 3-dim scene. These objects do not have physical existence.

This scene is without interpretation, meaning no 3-dim scene (with 3-dim bodies) could have produced it.



In figures like the above one, men are unaware of the extension of the background, and  makes sense even if B is background. SEE is unable to make this mistake, and its analysis of the scene will reflect the fact: the preprocessor will complain that one region, the background, is neighbor of itself. See comments to scene R3, page 113.

Of course, in these cases there is no answer to the question "which are the bodies in the scene?" Whatever answer SEE (or anybody else) gives, it is wrong.

Nevertheless, according to our meta-theorem (page 33), there is an extremely easy way to discover and reject these impossible scenes: all of them are necessarily illegal scenes (q.v., page 217). And we know how to detect illegal scenes. SEE (or its preprocessor, rather) already does that.

SEE detects all impossible scenes, by refusing the data as an illegal scene.

A PROGRAM TO DISCOVER HUMAN OPTICAL ILLUSIONS

Some scenes get classified by our metatheorem as 'possible but not "good" interpretation', and likewise by SEE, which does not refuse to analyze any legal scene.

Nevertheless, a person will stubbornly classify them as 'odd-looking' or 'not making sense' or 'impossible', even if we teach him the solution obtained by SEE (figures 'Penrose Triangle', 'Black', 'Staircase', 'CONTRADICTION').

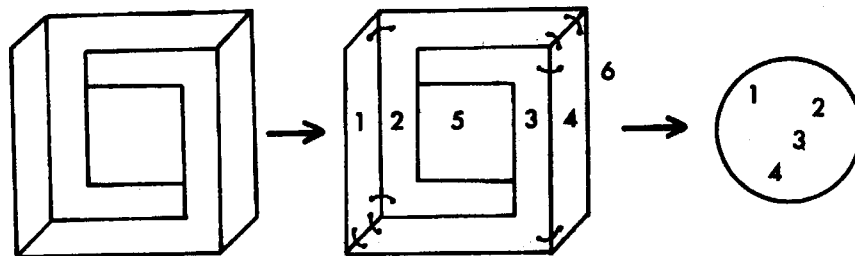


Figure 'CONTRADICTION'

One object is found by SEE; (:1 :2 :3 :4).  
 As such (since it is a legal scene), SEE classifies it as 'possible but not "good" interpretation'. A person will classify it as "not making 3-dim sense": a human optical illusion. Is it possible to reconcile these views?

Of course, the metatheorem (page 39) insures that there is at least one solution, so SEE's interpretation is "right" (it has chosen one correct answer, generally not the trivial solution given by the metatheorem), and the mortal is wrong. Also, the theorem of page 50 insures that any system (human or computer) that uses too "local" rules (see fig. 'MACHINE') will make at least one mistake, no matter what rules he (or it) uses.

H-optical illusions There is thus a disagreement between SEE and our fellow subject, because SEE has classified the scene as 'possible but no 'good' interpretation' and our man has said 'contradictory as a three-dimensional scene'. Let us call these human optical illusions (such as 'Contradictory', 'Staircase', etc.) by the name h-optical illusions.

What to do in these disagreements? Who is right?

SEE is right Above comments seem to indicate that the electronic data-processor is correct. The human has used excessively "local" rules. That being the case, we can teach and train (if avoiding future errors is desirable) our subjects to "understand", rationalize and make sense out of these h-optical illusions. Indeed, that is what is tried in figures 'Black', 'Penrose Triangle', etc. Different people may show different degrees of (H-optical) illusion before training and after training (see Box). This training is possible (see Box).

In other words, if SEE is right, the computer scientist has nothing to do, it is all up to the psychologists and educators.

Man is right We may hold the view that the human answer is still preferable. Then, to our relief, man is right and SEE is wrong. It is necessary (perhaps) to modify and correct SEE, so as to emulate personal behavior. \* We suggest a way to do this.

A program to discover h-optical illusions It is possible to enable SEE to detect these h-optical illusions, so that it will classify the legal scenes into "possible" or "h-optical illusions."

**SUGGESTION**

As the problem of discriminating between background and objects (see section 'On background discrimination by Computer'), this is an interesting project from the "psychological" point of view but, as in the background case, it is not essential at the moment for our vision-robot work.

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\* Strictly, there is a third possibility: both are wrong.

## BOX

There is generally a wealth of available information—though none entirely reliable—for settling the size and distance of external objects, with sufficient precision for normal use. As is well known, the visual system makes use of a host of 'depth cues', such as gradual loss of detailed texture with increasing distance, haziness due to the atmosphere and nearer objects partly hiding those more distant. These cues were discussed in the nineteenth century by the great von Helmholtz (1925), who fully realised their importance, and they have been the subject of many investigations since, especially by J. J. Gibson (1950). Whatever the richness of depth cues, however, the visual input is always ambiguous. Though the brain makes the best bet on the evidence—it may always be wrong.

The kind of mistakes which occur when the bet is on the favourite though the favourite is not placed, is shown most dramatically by the demonstrations of Adelbert Ames (1946). The most impressive demonstration is given simply with a room which is non-rectangular, but so shaped that it gives the *same retinal image* as a rectangular room to an eye placed in a certain position. Now clearly this room, though queer shaped, *must* appear the same as a normal rectangular room, for it gives the same image to the eye. But consider what happens when objects are placed inside the Ames room. The further wall recedes at one side, so that an object or person standing in one corner is actually at a different distance than is a second object placed at the other far corner. These objects (or people) appear, however, to be at the same distance—and they are seen the *wrong size*. This is clear evidence that we assume rooms to be rectangular (because they usually are) and we interpret the size of objects according to their distance as given by this assumption. When the assumption is wrong we see wrongly. What Ames did was to rig the odds, and then we make the wrong decision on size and distance. A child may appear larger than a man. We may know this is absurd and yet continue to see a bizarre world. The retinal image is all right, but the odds have produced the wrong internal file cards and then the human seeing machine is upset, and gives a wrong answer.

It is interesting that the Ames room is seen correctly by peoples, such as the Zulus, brought up in a 'circular culture' of beehive huts where there are few reliable perspective features, such as rectangular corners and parallel lines, in their visual environment. To the Zulus, the odds are not rigged by the Ames room—to them this is not misleading perspective. They are not subject to this illusion, but accept the room as the shape it is, and see the objects in it correctly in distance and size. This is a matter of very real importance. It shows that when we are transferred to an alien or bizarre environment, where our filing cards are inappropriate, we interpret the images in the eyes according to principles found reliable in the previous, familiar world—but now they may systematically mislead and then perception goes wrong. Space travellers beware! {Gregory, in {Collins and Michie}}

A possible way to attack the problem is

- (1) To identify each link with whoever proposed it.
- (2) To set up systems of simultaneous "symbolic" equations.
- (3) To solve them by elimination.

We elaborate:

- (1) Mark each link with the name of the heuristic that produces it. After obtaining the 'maximal' nuclei by GLOBAL and LOCAL, several links are left (for example, three in fig. 'FINAL-BRIDGE') and ignored by the current SEE. Instead, one could see what kind of links they are, and one has in this way more information about the type of contradictions in the scene.
- (2) Introduce a 'conditional' link: regions :1 and :2 belong to the same body if region :3 does not. An OR link is now possible by use of the conditional, since  $a \Rightarrow b \equiv b \vee \neg a$ .
- (2.3) Introduce a 'NOT' link: :3  $\neq$  :5, regions :3 and :5 do not belong to the same body.
- (2.6) As in ordinary algebraic equations, a system of  $n$  simultaneous equations means that all of them must be satisfied; the "AND" of all must be true. Thus, AND is implicit in our notation. So far, we have OR, AND, NOT, IMPLIES (conditional): we have more than necessary.

At the end, we have a system of simultaneous equations like these, where :1 = :2 means both belong to same body; this is an equivalence relation so I use the = sign:

$$\begin{aligned} & :1 = :2 \quad \text{OR} \quad :3 = :5 \\ & :3 \neq :2 \quad \Rightarrow \quad :1 = :4 \quad \quad \quad (E) \\ & \dots \end{aligned}$$

We now proceed to "solve" these equations. Three things could happen:

- == Exactly one solution is found. This is the normal case, and that solution tells what the bodies are. Familiar, "clear", possible scenes will fall in this case.
- == More than one solution is found consistent with our equations.

All are reported. This is the case "Ambiguous -- several good interpretations."

== No solution is found. This is a genuine optical illusion, corresponding to a contradiction in the equations. For instance, in fig. 'CONTRADICTORY', equations set by the T-joints between :2 and :3 would be inconsistent with those set by the Arrows and Forks.

How to solve the equations (E) by the solution to (E) we mean a division of the scene (:1, :2, ..., :n) by means of a partition of the form

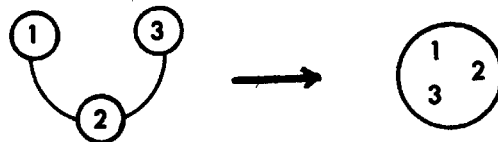
$$\begin{aligned} (:1 = :5 = :7 = :6), \\ (:3 = :2), \\ (:4) \end{aligned}$$

which is consistent with (E).

In the current SEE,

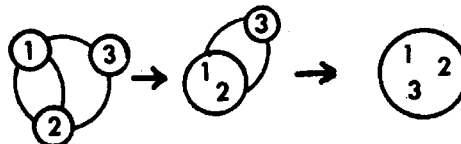
- (a) The equations are only equalities:  $:1 = :2$ .  
Also, equations of the type  $:1 \neq :2$  are taken into account by inhibitory mechanisms, such as NOSABO.  
No conditional links exist.
- (b) Since all equations are of the type  $:2 = :3$ , the solution is obtained by applying transitivity, that is,

$$\begin{array}{l} 1 = 2 \\ 2 = 3 \end{array} \Rightarrow (1 = 2 = 3) \quad \begin{array}{l} \text{parentheses} \\ \text{indicate nuclei.} \end{array}$$



Except that we require two antecedents for application of transitivity (two strong links):

$$\begin{array}{l} 1 = 2 \\ 2 = 1 \\ 1 = 3 \\ 2 = 3 \end{array} \Rightarrow \begin{array}{l} (1 = 2) \\ 1 = 3 \\ 2 = 3 \end{array} \Rightarrow (1 = 2 = 3)$$



An exhaustive search (which successively tests each possible partition) of the solution to (E) is impractical except in very small scenes, and heuristic methods are needed.

I suggest to start from the equalities such as  $1 = 2$   
 $2 = 3$

and to form nuclei<sup>as</sup> with the current SEE, except that at each step we check to see if our current nuclei satisfy all of (E); for disjunctive equations such as " $4 = 5$  OR  $6 \neq 7$  OR  $4 = 6$ " we try each branch of the OR in turn, rejecting those who conduce to no solution (this may be pretty combinatorial, too).

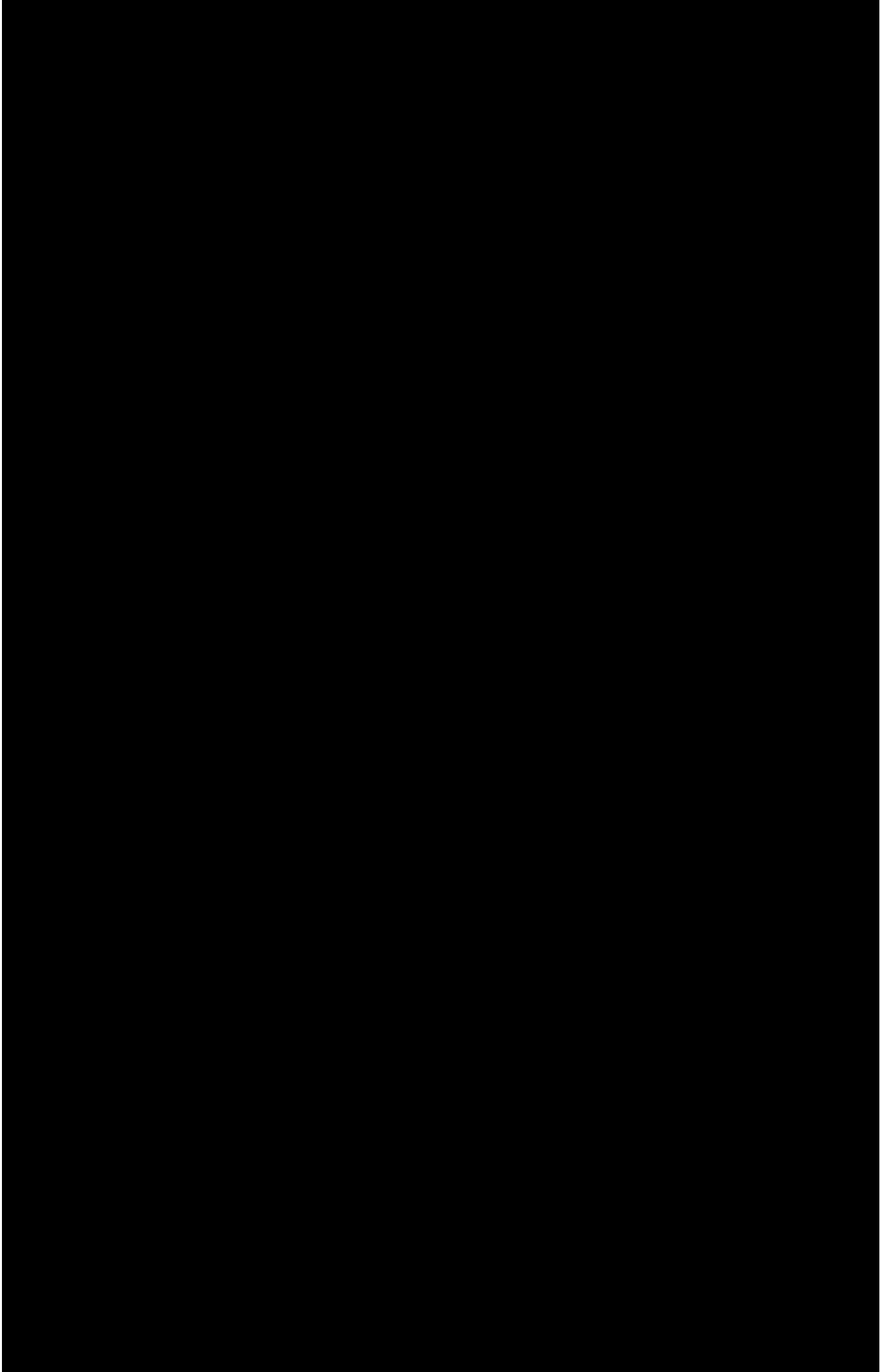
Perhaps it is possible to use more Logic here -- some sort of theorem proving.

Conclusions and conjectures The similarities between SEE and people (see also 'Human perception vs. computer perception, page 254) stem from the fact that, like SEE, people seem to use only a small number of rules (although not necessarily those used by SEE), which work in almost all cases, but when these rules conduct to an ambiguity or inconsistency ("conflicts"), there is reticence to abandon them, and mistakes or impossibilities are produced.

It is possible that, like SEE, people use primarily local clues, and with less frequency more global information to disambiguate interpretations. I think that, in the presence of objects (in 2-dim line drawings, such as 'MOMO', for instance) not seen before, humans follow general rules not unlike those used by SEE to distinguish or decompose a scene into bodies. Rules that apply to all polyhedra have to be invoked, since in presence of previously unseen objects, humans can not use a model of the object.

The more familiar an object is (or if we have reason to suspect it or expect it), the faster we abandon the general rules and propose its model as a possible explanation of part of an scene; we then jump to a model matching routine (a la DT {MAC TR 37}) that tries to fit the model to part of the scene (to a semi-isolated body); general rules a la SEE prevent us from overflowing with our model into other bodies, and help us to deal with partially occluded bodies.





## ON NOISY INPUT

The performance of our programs is analyzed when the data has imperfections consisting of (1) misplaced vertices, (2) missing edges, (3) spurious extra lines, (4) missing faces, (5) two vertices merged.

The section 'Analysis of Many Scenes' contains results of SEE when applied to imperfect scenes.

Summary It is easy to predict the operation of SEE when the two-dimensional data supplied is clean, in the sense of being an accurate representation of the three-dimensional scene.

In practice, of course, errors will occur in the data and it becomes important to know how sensitive our program is to them.

SEE has some serendipity. Many of the imperfections in the data do not cause mistakes in the linking procedure, or the link misplacements are not enough to cause erroneous identification. But mistakes are made.

Here is how different types of imperfections are handled:

== The assignment of types to vertices is highly insensitive to errors in the position of each vertex, except T'S that become Forks of Arrows. Two cures to the exceptions were found, only the first of which is implemented:

- (1) Allow tolerances in concepts of parallelism and colinearity.
- (2) Allow a long but slightly twisted rectilinear segment to be "straightened", as indicated in comments on scene R17.

== Missing edges are subdivided in three classes (discussed below); two of them produce recoverable or detectable errors (hence, susceptible of correction or prevention). It will be difficult to detect if a segment of the third class is missing; these will produce recognition mistakes.

== Additional lines, like the ones caused by edges of shadows, are not easily detected as spurious or superfluous. Their presence mainly produces a diminution in the number of useful links, thus sometimes causing too conservative behavior -- i.e., proposition of too many bodies.

== Whole faces may be missing. Ordinarily (see scenes L2, L9T).

the remaining part of the body gets correctly identified.

#### OBTAINING THE DATA

The scenes analyzed by our program in this thesis were obtained by one of two methods:

By free drawing A line drawing representing three-dimensional objects was made; the coordinates of each vertex were accurately measured (or computed) and the information was put in the 'Input Format' form previously described. Also the regions belonging to the background were indicated as such.

These scenes have mnemonic names such as TRIAL, BRIDGE, etc.

What kind of projection did you use? Were these isometric drawings? Since no assumption is made on the rectilinear objects being drawn, the drawings are not isometric, or perspective, or ... projections. They could be any of them. It is not assumed that "we are dealing with prisms, with faces of a body meeting at right angles (like the corners of a cube),"<sup>or</sup> with convex objects. Neither the drawings nor the program make any assumption of this type. If the reader wishes to adopt the assumption specified above in quotation marks, then the drawings will correspond to orthogonal projections of three-dimensional scenes.

No support hypothesis is needed: if necessary, the objects could be floating in a transparent fluid having their same density.

By construction Arbitrary but not too complicated objects were cut from pine wood, with flat surfaces, and painted black. Their edges were painted white. By placing them on a black table (see first few pictures of this thesis) in different positions and combinations, three-dimensional scenes were created (see figure 'TEST OBJECTS'). Pictures were taken with high contrast film slightly under-exposed so as to render black everything but the lines. Diffuse illumination eliminated shadows [Great help was received in the pictorial task

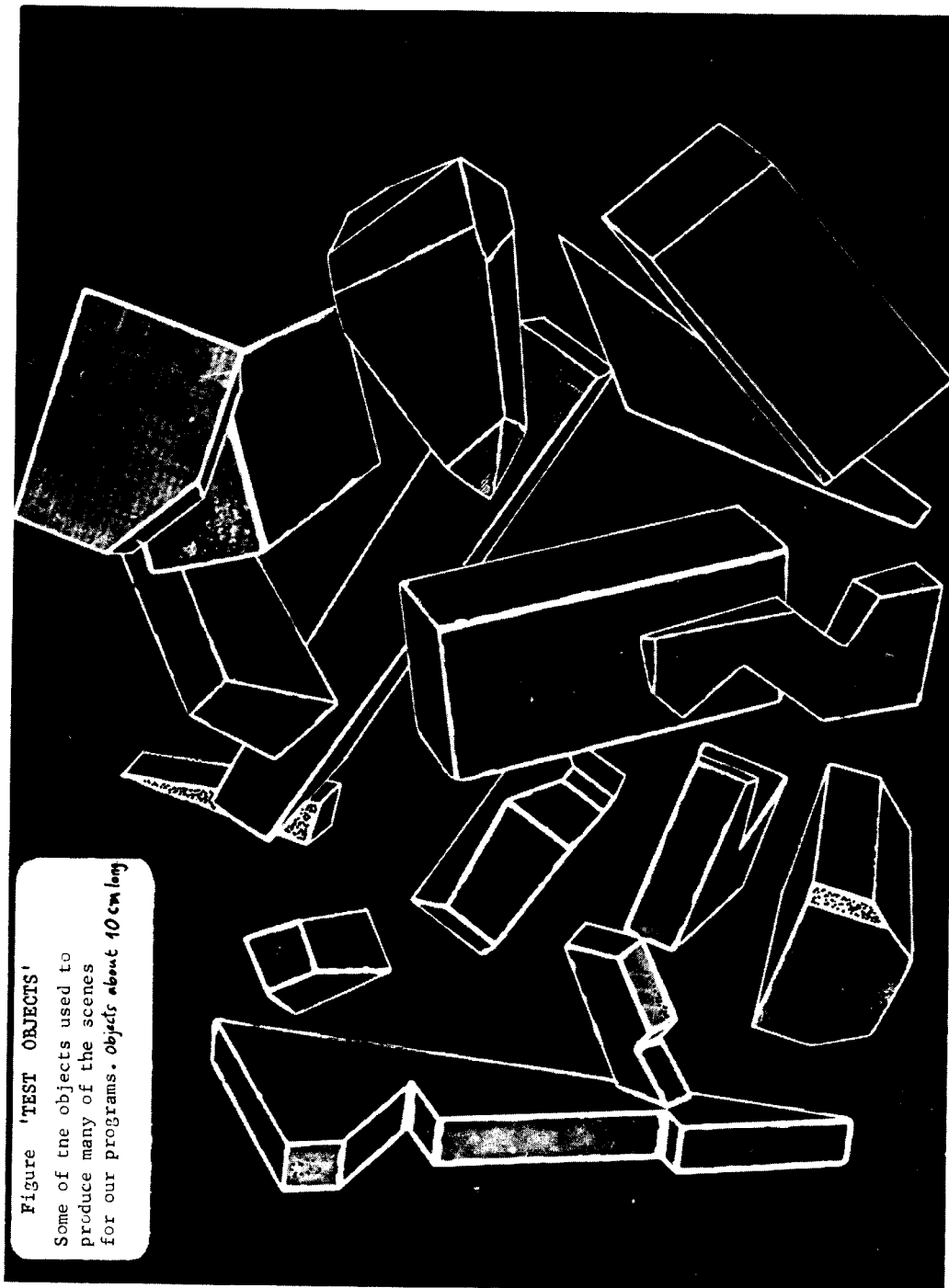


Figure 'TEST OBJECTS'  
Some of the objects used to  
produce many of the scenes  
for our programs. Objects about 10 cm long

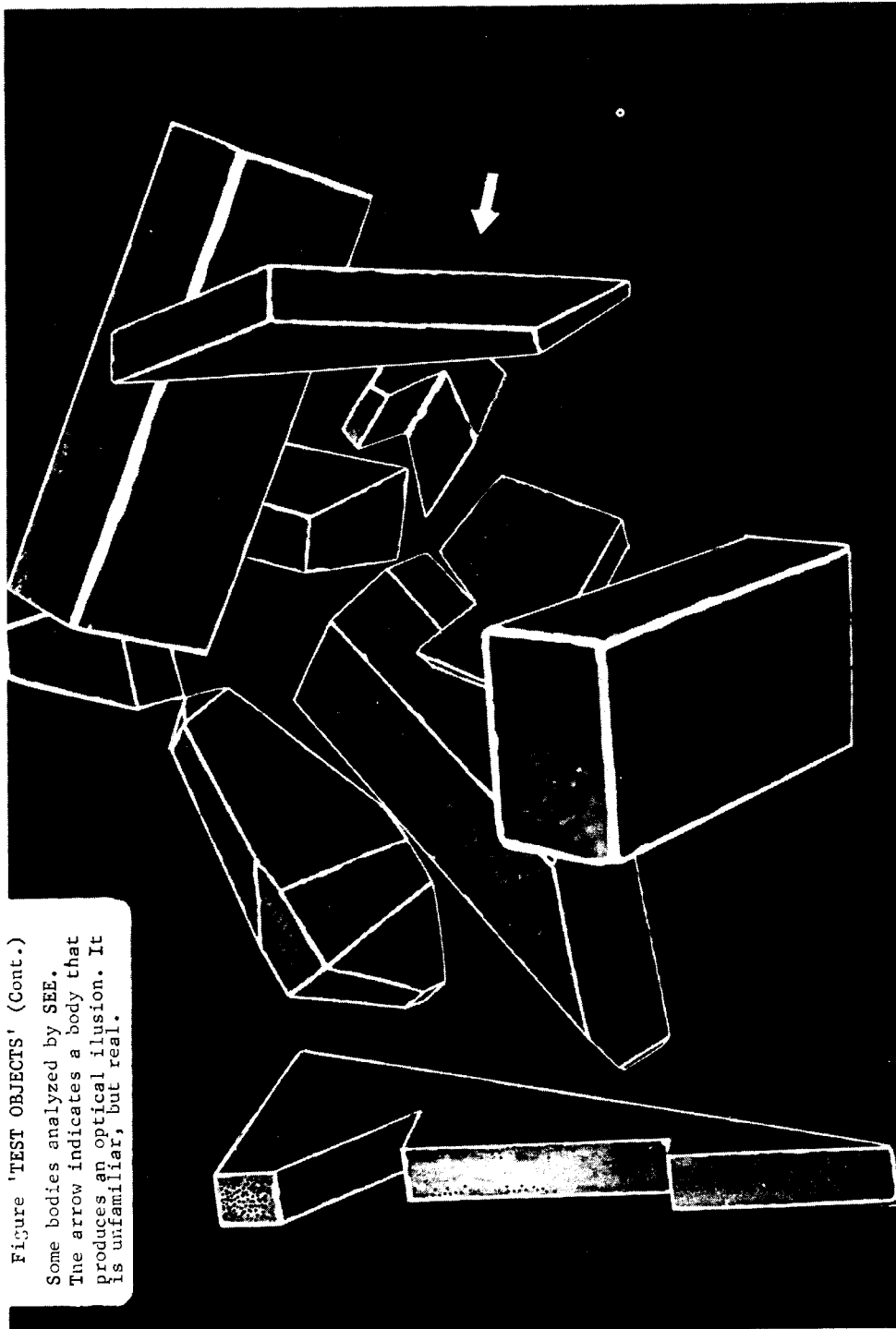


Figure 'TEST OBJECTS' (Cont.)  
Some bodies analyzed by SEE.  
The arrow indicates a body that  
produces an optical illusion. It  
is unfamiliar, but real.

from Messrs. William H. Henneman, Devendra D. Mehta and David Waltz, and is here acknowledged]. The photographs were taken with a depression angle from  $45^{\circ}$  to  $90^{\circ}$  (that is, looking down), 50 mm focal length lens, 35 mm camera (standard equipment).

The size of the prints is approx.  $8\frac{1}{2}$  by 11 inches (21.5 by 28 cm). If some lines were not clear, they were retouched with white ink. If some lines were missing, they were NOT added.

The pictures have names like L2 or R3, a letter and a digit. Most of them are stereographic pairs, taken with both cameras having parallel optical axes, and the sensitive film on the same plane. SEE only analyzes one scene at the time, so the left picture is not consulted when SEE analyzes the right picture, and viceversa.





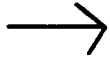


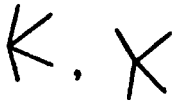


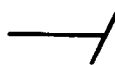






A transparent millimetric mesh is laid on top of the prints, and the coordinates are read by eye and put by hand in the 'Input Format' form. The thickness of each line is about 1 mm (see figure 'TEST OBJECTS'); typically, the size of a scene is 10 or 15 cm: a minimum error of  $\pm 1$  per cent in the coordinates of a vertex is already present. The slopes and directions of short segments suffer, naturally, much greater errors. Also, if two vertices are too close together (about two millimeters) they are merged and codified as one. We are simulating the kind of mistakes that are likely to occur.

Also, some bias is introduced, no doubt, by the human operators. [By reading the coordinates in most of the scenes, immense help was given by Miss Cornelia A. Sullivan and Mr. Devendra D. Mehta; the author acknowledges it.]

Irrespective of the generation method, the scenes that appear in this thesis were drawn in their final form by the PDP-6 computer through a Calcomp plotter, and then inked and finished by hand. Thus, it is possible to perceive in many of them the imperfections of the data that SEE had to analyze.

## MISPLACED VERTICES

The coordinates of a vertex may contain a small error or 'noise'.  
How does this affect the type of a vertex? Does the type change?

L.		→		Not affected
FORK.		→		Not affected
ARROW		→		Not affected
K.		→		Transforms into MULTI.
X.		→		Transforms into MULTI.
T.		→		Transforms into ARROW
				Transforms into FORK.
PEAK.		→		Not affected.
MULTI.		→		Not affected.

Many types are unaffected. Type K vertices transform into MULTI, but since K's are seldom used by SEE, this is no big loss.

X's transform into MULTIs, and we lose two links here, which makes SEE to behave more conservatively. Also GOODT gets affected (though not much).

The serious change are the T's that get transformed into ARROWS or FORKs, when these T's are matching T's. Because they are used for linking otherwise disconnected pieces of a body, their loss generally implies the partition of a body into two. See figure 'DISCONNECTED'.

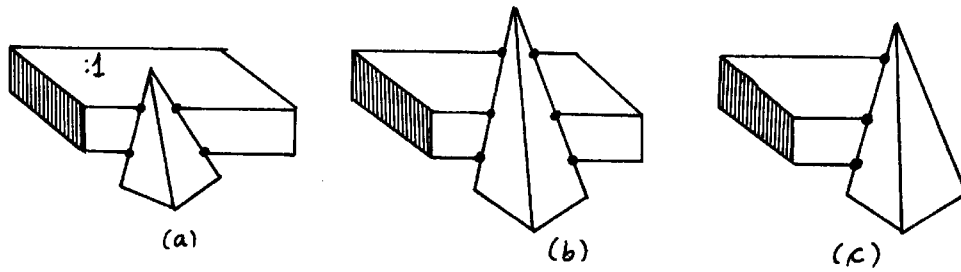


Figure 'DISCONNECTED'

The T's under discussion are marked by small circles (•). In (a), the misclassification of these T's into Arrows or Forks does not break the occluded body, who retains its unity thanks to :1. In (b), the same misclassification does break the occluded body, reporting two objects instead of one, a possible but less desirable answer. If the T's are not matching T's, as in (c), their misclassification does not matter.

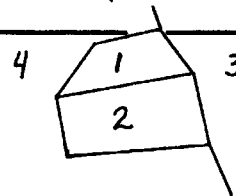
The loss of matching T's makes the program to be more conservative in some cases. In some sense (see 'Desirability Criterion') this is tolerable.

What other perils does the misclassification of the T's bring? We should worry if, due to errors caused by T's, the occluded body joins the occluding one.

DESIRABILITY CRITERION.

- (1) We would like a SEE that never makes mistakes. Since this is not possible, then
- (2) We would like it to make mistakes of only one kind, either join two bodies that should be left separated (intrepid, cavalier behavior), or leave unattached two nuclei that should be reported as a single object (conservative behavior).
- (3) Among the two, we prefer a conservative SEE, because its errors will be easier to correct (cf. Stereo Perception).

The T's should not originate the reporting of :1-2-3 as part of one body



Each T, when perturbed, will go to one of these states: (N) normal, unperturbed; (L) "left",  $E_2$  moves towards  $E_1$ ,  $E_1$  —  $E_2$  becoming a FORK, or (R) "right", when  $E_2$  moves away

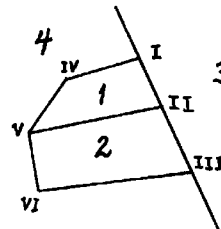




from  $E_1$ ,  $\overline{E_1} \rightarrow E_2$  becoming an Arrow.

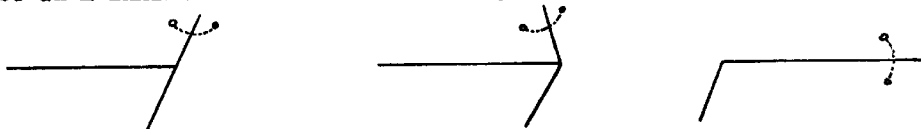
For three T's of an occluded body,  $3^3 = 27$  states are possible. They are shown in next page, in table 'THREE Ts'.

How many of these 27 states will produce mis-links joining 1 with 3 or 2 with 3 or 1 with 4 or 2 with 4 (none of the four regions is necessarily background) ?



None.

The reason is that (see description of NOSABO) a T or an Arrow or an L inhibit the link shown below,



so that (a) An arrow in position (I) [or (III)] suggests linking 1 with 4. This link is inhibited by the L at IV [or VI].

Example: Figure R L L in Table 'THREE Ts'. (page 214).

(b) A Fork in position (I) [or (III)] suggests

- (i) linking 1 with 3. Inhibited because of the T or arrow in vertex II.
- (ii) linking 1 with 4. Inhibited because of the L in IV.
- (iii) linking 4 with 3. Depends on outside considerations. Discussed below.

Example: L R L.

(c) An Arrow in position (II) suggests linking 1 with 2.

Inhibited or allowed according to vertex V. Example: RRL.

(d) A Fork in position (II) suggests

- (i) linking 1 with 3. Link inhibited by the T or arrow of I.
- (ii) linking 2 with 3. Inhibited by the T or arrow in III.
- (iii) linking 1 with 2. Inhibited or allowed according to vertex V.

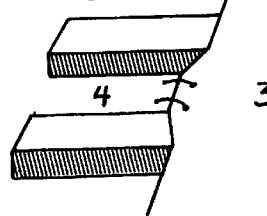
Example: R L N.

Thus, no link is possible, even under these "noisy" circumstances, between 1 and 3 or 2 and 3 or 1 and 4 or 2 with 4. That is, the 27 cases of table 'THREE Ts' are treated correctly.

<p>NNN</p>	<p>NNL</p>	<p>NNR</p>	<p>NLN</p>
<p>NLL</p>	<p>NLR</p>	<p>NRN</p>	<p>NRL</p>
<p>NRR</p>	<p>LNN</p>	<p>LNL</p>	<p>LNR</p>
<p>LLN</p>	<p>LLL</p>	<p>LLR</p>	<p>LRN</p>
<p>LRL</p>	<p>LRR</p>	<p>RNN</p>	<p>RNL</p>
<p>RNR</p>	<p>RLN</p>	<p>RLR</p>	<p>RLR</p>
<p>RNN</p>	<p>RRL</p>	<p>RRR</p>	<p>TABLE THREE T'S</p>

A possibility of bad linking exists between 4 and 3 in this case, if two T's convert into forks and "help each other":

Two links originate the joining of 4 and 3.



Rather than get involved in this sub-problem, we will point out two solutions to the misplaced vertices: (1) by allowing some tolerance in 'parallel' and 'collinear'; (2) by 'straightening out' crooked or twisted segments. We explain.

Equal within epsilon (definition)  $a$  is equal within epsilon to  $b$ , written  $a \stackrel{\epsilon}{=} b$ , iff  $|a - b| < |\epsilon|$ . Generally,  $\epsilon > 0$ .

Tolerances in collinearity and parallelism Two lines are parallel if the sine of the angle formed by them is smaller than SINTO. ( $\text{sine} \stackrel{\text{SINTO}}{=} 0$ )  
Currently, SINTO = 0.15

Lines  $ab$  and  $bc$  are colinear if  $\text{length } ab + \text{length } bc \stackrel{\text{COLTO}}{=} \text{length } ac$ . Currently, COLTO = 0.05

We have implemented these definitions. Better definitions exist. These definitions allow most small inaccuracies in the coordinates of vertices to pass unnoticed. Although they are giving reasonable service, they are only temporary, since by relaxing too much the criterion for parallelism and collinearity, strange things could happen (fig. 'CROSSED').

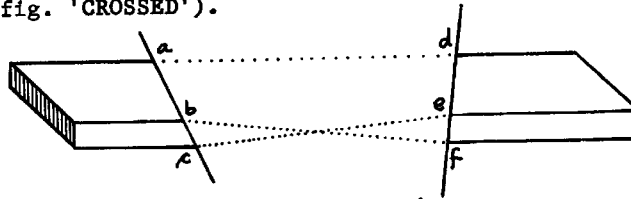


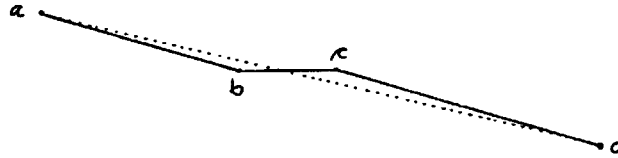
Fig. 'CROSSED'

A too lenient definition of parallel and collinear could give the following matching T's:  $a$  to  $d$ ,  $b$  to  $f$ ,  $c$  to  $e$ .

See also on section 'Analysis of many scenes' comments to L9 and R9T. (page 152, 156).

Straightening twisted segments

The definitive cure is simple:  
reassign the slope of bc to be that of ad, if bc is small, ad large



and the angles at b and c are close to  $180^\circ$ . See also comments to figure R17. This has not been implemented. In this way, all cases of table 'THREE Ts' will be solved. See also comments to scene R4.

Probably the preprocessor will automatically take care of this rectification, since it may prefer to give a long segment ad instead of three almost collinear shorter segments ab, bc, cd.

Since the straightening of a segment replaces some known vertices (which we suppose inaccurate) by other idealized vertices, we may be introducing uncertainty, in the form of non verified hypotheses, to our data. The object in the scene could really be "crooked" or twisted.

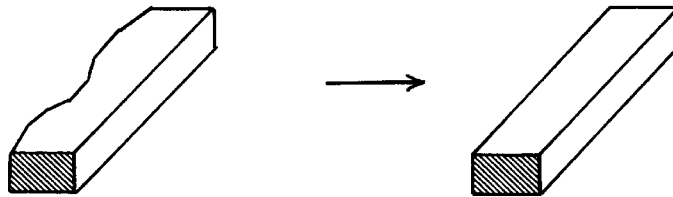


Fig. 'TWISTED'

The object to the left is really bent as shown.  
If we idealize it as in the right, we are falsifying the information about it.

By replacing it by an idealized version, we may be creating problems for its identification, when we want to assign a name to it. But notice that the 'unbent' version or idealization is handier for SEE.

If the information is very bad

Throw it away and read the scene again. A simile indicates that the issue becomes one of allocation of resources: if you receive a written message containing a few wrong characters and missing words, you may use your brains and time

to deduce the omitted portions (by employing the redundancy, for instance). If the dispatch is very garbled, you might as well request a new one.

Summary It is known how to handle small inaccuracies in the position of the vertices.

#### MISSING EDGES

From time to time, an edge will fail to show up in the scene, and the questions are (1) how much harm will be produced, and (2) how can we detect and correct the anomaly. An example appears in page 141.

Illegal Scenes Lines that end abruptly produce illegal inputs, suggesting that segments are missing.

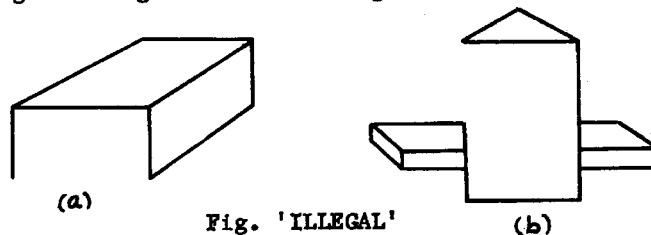


Fig. 'ILLEGAL'

In (a), a vertex has one edge.  
In (b), the network can be separated by erasing just one edge.  
Both are illegal scenes, indicating missing or extra lines.

Also (Figure 'ILLEGAL', (b)) a region can not be a neighbor of itself -- another irregularity that points to deficient data. Cf. comments to scene R3. (page 113).

These constraints can be nicely exploited by a preprocessor.

Line proposer and line verifier A line proposer is a program that suggests places where a line can be missing; a line verifier is essentially a precise line finder that searches a line in only a small portion of the scene, as told by the line proposer.

In the body of this section we will develop several heuristics for use in a line proposer. The verifier is not discussed.

Blum's line proposer An algorithm has been designed by Manuel Blum [1968], that will detect many places where lines are possibly missing. It suspects concave regions. An angle bigger than  $180^\circ$  originates a search for the omitted line in directions parallel to the neighbor

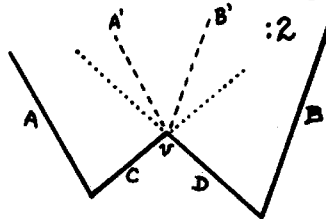


Figure 'BLUM'

Region :2 is suspected to contain undetected lines, because it is concave. Vertex v is chosen because its internal angle is bigger than 180 degrees. From it, Blum's proposer will suggest to the line verifier to look for lines in directions VA' and VB' (broken lines), parallel to the neighbor edges A and B. It also searches (dotted lines) along the continuation to lines C and D.

edges (fig. 'BLUM'). It also originates searches along its own edges. In other conditions, a vertical line is searched.

No harm is done by a bad proposer. Only some time is wasted.

Internal edges If a missing line is totally internal to a body, and is not detected by the line proposer, its absence will at most cause conservative behavior in SEE. In some cases their absence does not confuse SEE (figure 'MISSING').

The majority of internal edges cause concave regions to appear (fig. 'BLUM'). They will be detected by a line proposer.

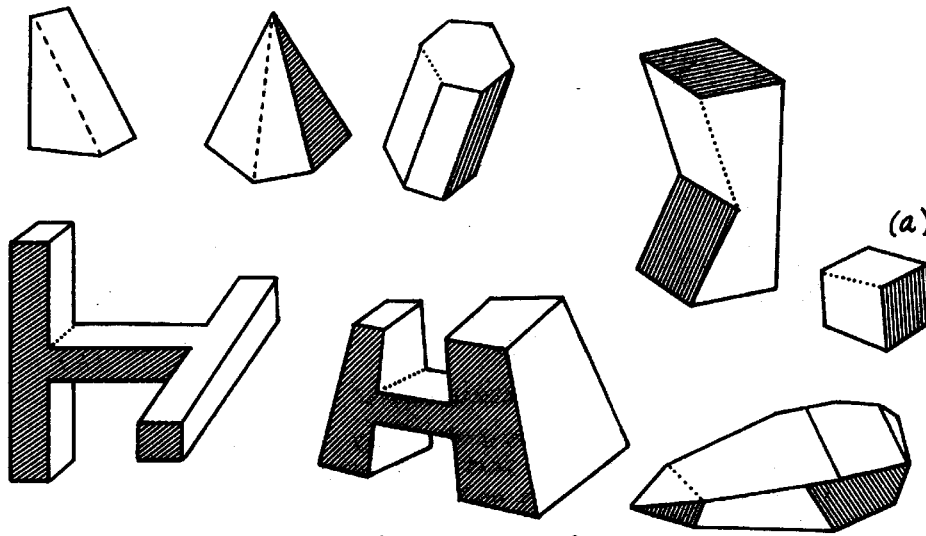


Fig. 'MISSING'

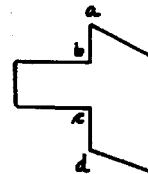
Cases where the disappearance of an internal line (dotted) does not separate the body.

In (a), the object separates into two. This case is recognized by Blum's heuristics. Else, SEE could check for this configuration as a special case.

External edges Edges that separate two bodies are called external. If undetected, their disappearance will cause 'intrepid' errors by SEE, which are undesirable (see 'Desirability criterion' in page 212). Two cases result: (1) Only part of the edge disappears; there is possibility of correction. (2) The whole edge is both external and missing (and the scene is still 'legal'): a mistake will occur, See figure 'External Edges'.

Case (1) Only part of an external edge disappears. It can be detected because

- (a) a concave region is generated, and
- (b) the region has internal angles bigger than  $180^\circ$  where a line "goes through": ab is colinear with cd.



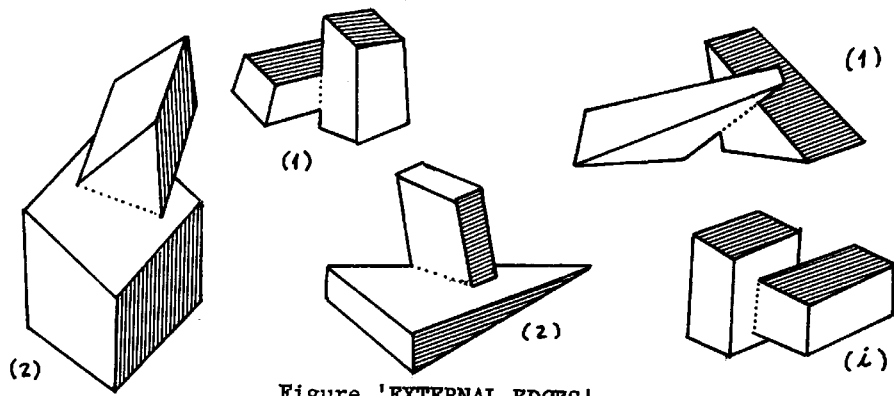


Figure 'EXTERNAL EDGES'

A segment separating two bodies may disappear.  
 (1) If that segment is part of a larger segment, it is possible to sense and correct the anomaly.  
 (2) If a whole external edge is missing, its absence remains undetected, inducing a mistake in SEE. In (i) an external edge disappears, and creates an illegal figure.

Case (2) The complete edge is missing. Then (b) of case 1 fails, and detection is difficult.

SPURIOUS EXTRA LINES

They are lines that "should not be there", such as those caused by edges of shadows.

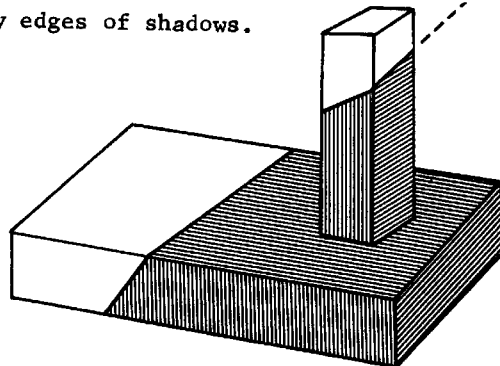


Fig. 'LIGHT AND SHADOW'

Each body becomes two; each one is recognized independently by SEE. Four bodies are found.



Shadows of rectilinear objects travel in planes that (in theory) part an object in two (or more): the illuminated part, and the dark one. Each is a separate object by itself, according to our definition (see 'Several definitions of a body'), since they have plane boundaries. SEE should recognize them.

In practice, we have not tried our program with scenes having lines produced by shadows. A conservative behavior, like in figure 'LIGHT AND SHADOW', is expected.

Some shadows gradually diffuse; multiple lights cause multiple shadows. These problems may have to be solved by assuming or computing the direction or position of the light sources.

#### MERGED VERTICES

Two vertices fused in one will produce diminution in the number of useful links they report, since the resulting vertex will be of type MULTI. Thus, conservative behavior is expected from SEE in these cases (see Fig. L19, L17T, R17, L4, etc. The program does well in them, when not too many coincidences are present).

It is possible to analyze the vertices of type SUGGESTION MULTI and try to decompose them in simpler types (compare figure R19 with WRIST\*). Read comments to R19 and L19.

#### CONCLUSION

On scenes obtained from "real world" data, inaccuracies are expected, and it is required of SEE to work well despite them. Currently, the behavior of the program in these cases is not discouraging, but is not extremely satisfactory, either. The additional work needed depends heavily on obtaining genuine test data, instead of the faked data used in the experiments described.

## BACKGROUND DISCRIMINATION BY COMPUTER

A program determines the regions that belong to the background of a given scene; that is, the regions that are not members of any of the bodies. Examples are given.

Need The program SEE requires to know which regions of the scene belong to the background (cf. 'SEE, a program that finds bodies in a scene'). At present, this information is supplied by the user, as described in sections 'Internal format' (page 64) and 'Input Format' (page 63) of a scene.

In the current vision experiments, it is not difficult to determine the regions that form the background, since they are always black and homogeneous (see first few pictures in this thesis). But in more realistic scenes, there will be a great demand for a background finding program.

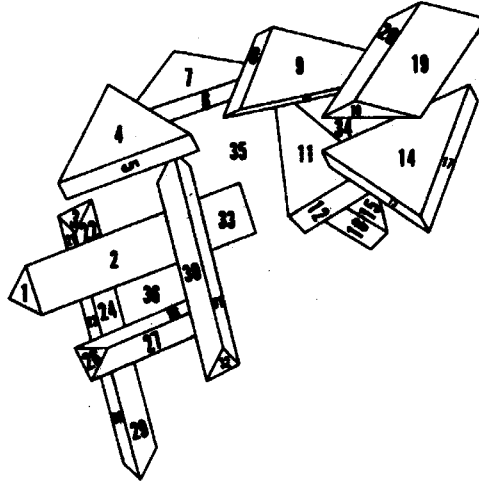
Therefore, it is interesting to try to develop a program to separate the "ground" in the back from the objects in the "foreground", having a limited information consisting of the scene as described in section 'Internal Format', namely, vertices and edges.

That is, we will use in this task only "geometric" properties.

Such program has been written, and works automatically under the command of PREPARA, the function that converts a scene from its 'Input Format' to its 'Internal Format'. When the regions forming the background are not supplied, PREPARA activates our program, named BACKGROUND, and these regions are searched for; otherwise, SEE is supplied with the background regions as declared in 'Input Format'.

Example. Scene 'HARD'. The results obtained are

(SUSPICIOUS ARE NIL)  
 THE BACKGROUND OF HARD IS  
 (:34 :36 :35)  
 (:34 :36 :35)



Three regions are found to be part of the background: :34, :36, and :35. That is correct.

We now proceed to describe the subroutines that make such identification possible.

Suspicious In a first pass, we collect the regions that "may be" background, and call them "suspicious regions". Regions that are not suspicious are LIMPIO (clean).

Ideally, if a region :R contains L's, FORKS, ARROWS or T's in the position below, it is not a part of the background.

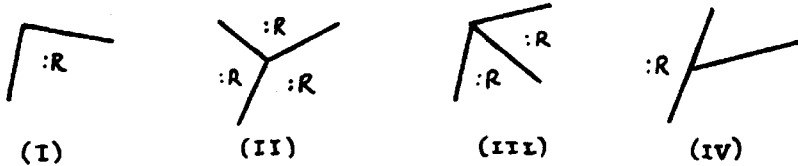
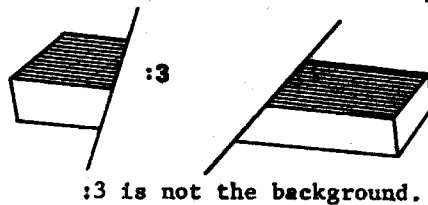


FIGURE 'BACKGROUND'

In an idealized situation, :R can not be part of the background: it is clean, or free of suspiciousness. :R will be called 'LIMPIO' (clean).

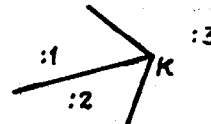
- (I) means that the background [almost] never is the internal part of an 'L' (the region containing the angle smaller than 180 degrees).
- (II) means that the background does not contain FORKS.
- (III) means that the background is not in the "inside" of an ARROW (the background is not a 'proper' arrow').
- (IV) means that the background can not be the flat region of a 'T'; this in turn means that a body can not disappear under the background and then reappear at some other point:



We reinterpret rules (I)-(IV) as follows:

- (I) A region "inside" an L is LIMPIO (clean).
- (II) A region containing a fork is LIMPIO.
- (III) A region "inside" an arrow is LIMPIO.
- (IV) A region "on the flat side" of a T is LIMPIO.

Clean Vertex (definition). A vertex is clean with respect to a region if it indicates, through rules I-IV, that such region is LIMPIO. For instance, K is clean for :1 and for :2, since (III) indicates that :1 and :2 are LIMPIO. K is not clean for :3.



These heuristics are not 100 per cent infallible; also, in a moderately complicated scene, coincidences of vertices are bound to occur, originating violations to I-IV. For instance, in figure CORN (page 150), vertex UU is a Fork belonging to the background, in contradiction with (II).

For completeness, we present a violation to each one of rules I-IV:

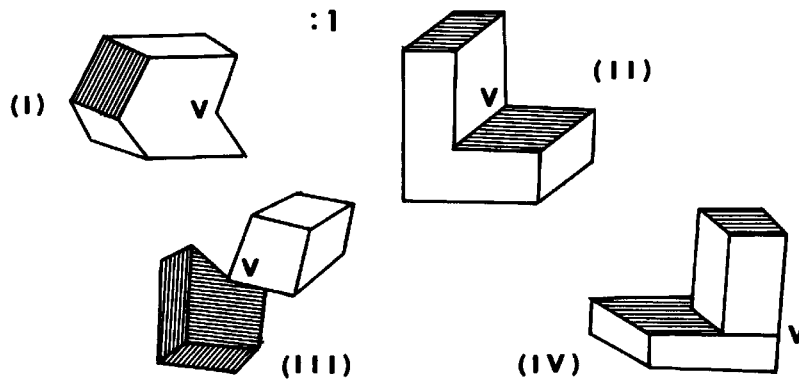


FIGURE 'VIOLATIONS'

:1 is the background. In all four cases, vertex V violates rule specified at the bottom of figure. They are rare cases. The situation indicates that rules I-IV provide noisy information, which has to be dealt with carefully. That is what is done.

The vertices of each region are analyzed under rules (I)-(IV). To allow for coincidences of vertices and rare cases (like those in figure 'VIOLATIONS'), it is permitted for a suspicious region to have a small number of clean vertices.

The number of clean vertices is compared with a quantity that is a small fraction of L (the number of vertices on the boundary); currently, that fraction is  $L/9$ .

- == If the number of clean vertices, that is, vertices satisfying I-IV is bigger than  $L/9$ , we call that region LIMPIO ("clean"). In addition, (a) If L is large (bigger than 25, currently), that region is BIGFACE, such as :21 of scene L19 (page 144); (b) Otherwise, it is only LIMPIO (normal case).
- '== If it is not bigger than  $L/9$ , then it is SUSPICIOUS. Also, (a) If L is large (bigger than 25), the region is BACKGROUND, (b) Otherwise is only SUSPICIOUS (normal case).

That is, a region LIMPIO has to have at least  
 $1 + [\text{one vertex of each nine}]$   
 "clean" vertices.

Example. Region :3 has four 'clean'  
 vertices (four vertices indicate that :3  
 is LIMPIO) --- It can not be SUSPICIOUS.

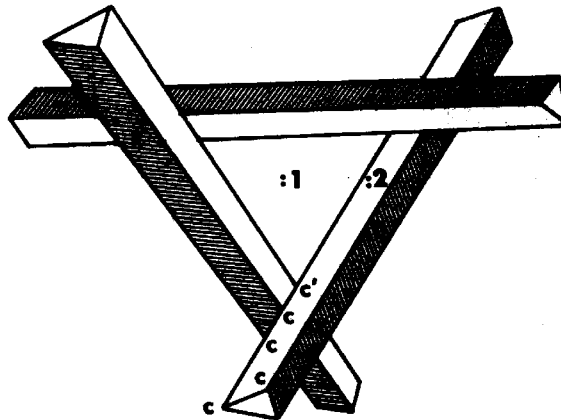
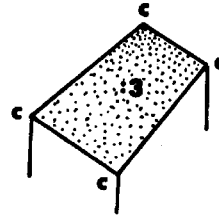


Figure 'EQUILIBRIUM'

(This scene is correctly analyzed by SEE)  
 All the three vertices of :1 are not clean;  
 :1 will become Suspicious (a candidate for  
 background). Five of the seven vertices of  
 :2 are clean, so :2 is LIMPIO. Note that  
 vertex C' is clean for :2 and not clean  
 for :1.

For example, when we apply the function SUSPICIOUS (see listings)  
 to every region of scene SPREAD, the suspicious regions turn out to be:

Suspicious only: :35 :18 :34 :2 :3 :12 :11 :33 :37  
 :47 :48 :46.

Background: :48.

Summary By analysis of its vertices, each region is either LIMPIO or  
 SUSPICIOUS. The suspicious regions with more than 25 vertices are  
 classified right away as BACKGROUND: a suspicious region with many  
 edges is probably background.

The selection is done entirely using "local" properties: a  
 region is classified according to information supplied exclusively  
 by its own vertices.

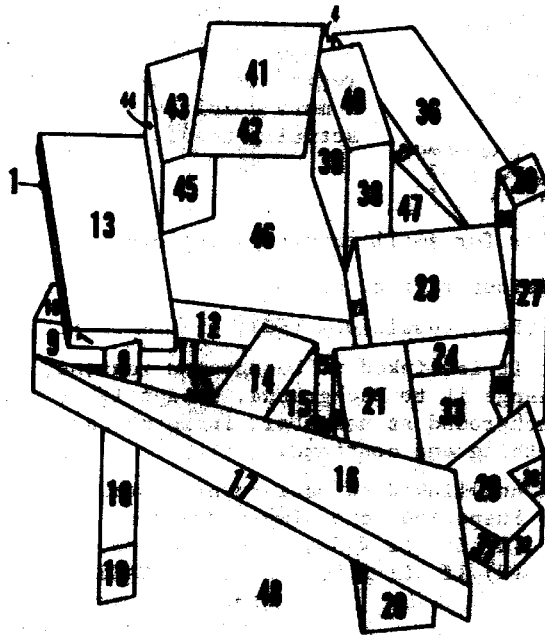


FIGURE 'S P R E A D'

Each region is classified as LIMPIO, SUSPICIOUS or BACKGROUND.

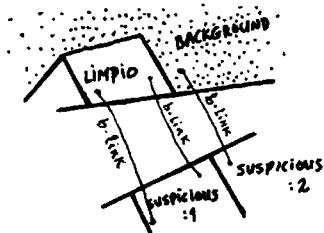
More global indications Our goal is to decide which of the suspicious regions are LIMPIO, and which ones are BACKGROUND.

- Since two background regions can not be contiguous ( the background can not be neighbor of itself), suspicious regions that are contiguous with the background are cleaned and put in the LIMPIO status.

In our example, :48 is background and therefore its suspicious neighbor :18 gets cleaned and becomes LIMPIO.

- Links are established through the matching T's. We call them b-links.

Ideally, a suspicious region linked to a LIMPIO region gets cleaned, a suspicious region linked to the background gets converted to background too.



Idealizing, suspicious region :1 becomes LIMPIO, and suspicious region :2 becomes background. A more complicated procedure is actually used.

In practice, we allow for small errors as follows:

For each suspicious region, we notice if it is b-linked to background (BA), suspicious (SO), or Limpio (LI).

BA == == If it is b-linked to background regions, we change it to Background, except if it has a background as neighbor, in which case we do nothing and continue.

( ) SO LI If not b-linked to background, but b-linked both to Suspicious and Limpio regions,  
 (1) If  $LI < SO$ , continue, do nothing.  
 (2) If  $LI \geq SO$ , classify this region as limpio (LI is the number of LIMPIO regions b-linked to the current region under consideration).

( ) SO ( ) If b-linked only to suspicious, continue, do nothing.

( ) ( ) LI If b-linked only to Limpio, change it to Limpio. Note: Sometimes I write Limpio, sometimes LIMPIO, they mean the same.

( ) ( ) ( ) If not b-linked, continue, do nothing.

We keep applying these rules until no change is observed. In this way, we have eliminated several suspicious regions.

In SPREAD, the suspicious regions were 35, 18, 34, 2, 3, 12, 11, 33, 37, 47, 48, 46. :48 is known to be the background (that was done in page 226), so it is no longer suspicious. :18 is a neighbor of the background (:48), and got cleaned in the page before this one.

:11 is b-linked with the LIMPIO :9 and with the suspicious :3. Therefore, :11 changes to LIMPIO.

:3 is b-linked with the Limpio :11, so the suspicious :3 becomes Limpio.

:12 is b-linked to the Limpio :10, and gets cleaned.



:46 is b-linked to the background :48, and gets made background, since :46 is not, at this moment, a neighbor of background.

:34 is b-linked to the background :48, and gets made background, since :34 is not a neighbor of background.

:37 is b-linked to the LIMPIO region :4, and transforms into LIMPIO.

:35 is b-linked to the region :34, which is background, so that the suspicious region :35 becomes background instead. <sup>It is also b-linked to 48.</sup>

:2 is a suspicious region b-linked to the region :35, which is part of the background. According to our rules, :2 becomes part of the background. *:2 is also b-linked to the background :48.*

At the end, only regions :33 and :47 remain suspicious:

(SUSPICIOUS ARE (:33 :47))

== We collect all these 'stubborn' suspicious regions and label them background, except those which are neighbors of background. A better procedure may be to make the exception in SUGGESTION those regions that are neighbors of suspicious regions. That is, two neighboring suspicious regions prevent each other from becoming background. I have not explored this possibility.

In the example SPREAD, :33 and :47 are made background.

== If no region is background at this point, make one of the "big-faces" background. There is room here for improvement.

== If no background yet, make background the region with most vertices. This is not yet implemented.

In our example, the (final) background regions are:

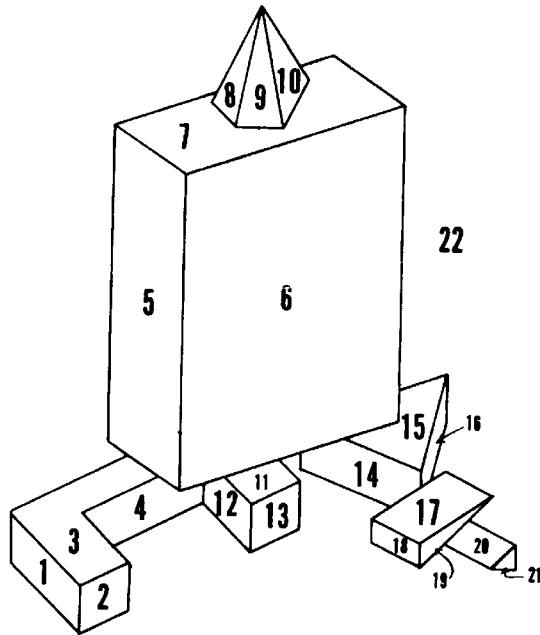
:33 :47 :35 :34 :2 :48 :46.

← BACKGROUND OF 'SPREAD'.

Other examples of background finding.

Scene CORN

LEENA  
FOOP  
SLIPGENERATOR  
TYPEGENERATOR  
MATES  
NEXT  
SEARCHING FOR BACKGROUNDS OF CORN  
(SUSPICIOUS ARE NIL)  
THE BACKGROUND OF CORN IS  
(\*22)



Scene BRIDGE

(\*30 IS BIGFACE)  
(SUSPICIOUS ARE NIL)  
THE BACKGROUND OF BRIDGE IS  
(\*30)  
(\*30)

Scene MOMO One mistake (:31) is produced here.

LEENA  
FOOP  
SLOPGENERATOR  
TYPEGENERATOR  
MATES  
NEXTIE  
SEARCHING FOR BACKGROUNDS OF MOMO  
(SUSPICIOUS ARE (:31))  
THE BACKGROUND OF MOMO IS  
(:6 :31 :40)

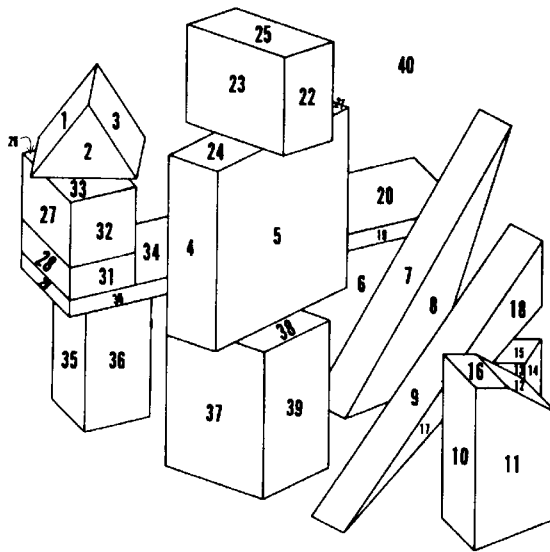


FIGURE —'MOMO.'

The problem is ambiguous Like in the case of body isolation (section 'The Concept of a Body'), the problem of determining the regions that belong to the background of a scene (regions that belong to no body) is ambiguous; many solutions are possible, as long as no two background regions are contiguous.

Among the multitude of solutions there exists a preferred one, which is "the" standard (common, familiar) interpretation chosen by people.

Our program tries to choose also, among the many solutions, the standard one.

Summary A lenient algorithm finds regions (by analyzing the types of their vertices, and their neighborhood relations) that may possibly be background, and labels them "SUSPICIOUS". With the idea of re-classifying the suspicious regions as 'LIMPPIO' (clean, no background) or 'BACKGROUND', a system of b-links is introduced. These b-links provide more global information about the scene.

Members of the suspicious set are assigned to one of the other two sets (limpio or background), while the algorithm tries to minimize the b-links between Background and Limpio regions.

Conclusion Fair results are obtained with the algorithm just described. Sometimes, regions are obtained as Background that are genuine components of a body ("Limpio") and vice versa.

Refinements are needed, but since in our present vision experiments the background is a homogeneous black area (see first few pictures of this thesis), no emphasis is shown right now.

## STEREO PERCEPTION

Summary So far we have discussed the identification of objects in a scene and ignored the problem of locating them in a three-dimensional space.

There are several ways to achieve this. We will discuss here one of them: the use of more than one view of the same scene.

A natural first step is to establish the correspondence between points in the two views; that is, given a point in one scene (left), to find the corresponding point in the other scene (right). Theorems S-1 below and S-2 on page 234 express criteria for this "stereo matching".

SEE can independently decompose the left and right scene into the bodies forming them, leaving as a problem to determine which of the objects in the right scene corresponds to an object

in the left scene. This can be done because each object will appear in both views with the same maximum height and minimum height (highest and lowest values of the y-coordinate of points belonging to that object); comparisons are easily made by replacing the objects by "intervals" consisting of these two numbers.

Further disambiguation can be achieved by the use of the function (WHERE  $X_L, Y_L, X_R, Y_R$ ), which determines the (x, y, z) 3-dim position of a point of which its two 2-dim locations  $(X_L, Y_L)$  and  $(X_R, Y_R)$  are known. {Griffith, AI Memo 143}.

### THEOREM S-1

If both cameras are identical, their optical axes parallel and the films or sensitive surfaces or retinas lie in the same plane, then a simple necessary condition for two image points, one in each retina, to have come from the same 3-dim point, is that both image points (left and right) have the same y-coordinate, measured in the direction perpendicular to the line joining the optical centers.

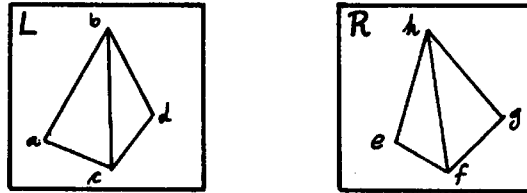


Figure 'POINTS'

Given two images of the same scene, before we can proceed to situate it in 3-dim space, it is necessary to know which points of the left scene correspond to points of the right scene: we have to discover the genuine pairs in it, a small subset of the cartesian product  $(a, b, c, d) \times (e, f, g, h)$ . It is desirable to have an algorithm that avoids an exhaustive search on this product.

Genuine Pair (definition). A pair of points  $(P_L, P_R)$  produced by a real 3-dim point of the scene in consideration.

Theorem S-2 below gives conditions that a genuine pair must meet. A particularization will produce theorem S-1 above.

THEOREM S-2 The left image  $P_L$  and the right image  $P_R$  of a point  $P$  have associated with them a variable, computable from  $(X_L, Y_L)$  or from  $(X_R, Y_R)$ , that will acquire the same value on  $P_L$  and on  $P_R$ . It is invariant under change of scene.

For the case where the optical axes are parallel, this variable is simply the y-coordinate  $(Y_L = Y_R)$  or height of the image.

For the case where the optical axes meet, this variable is  $\gamma$ , an angle that plane  $P_L-C_L-P_R-C_R$  makes with  $\Gamma$ , the plane containing the optical axes.

Any monotonic function of  $\gamma$  will be just as good. (cf. figure 'GENUINE PAIRS').

From the theorem, the algorithm (referred to in fig. 'POINTS') that we may use to establish correspondence between points in the two views is:

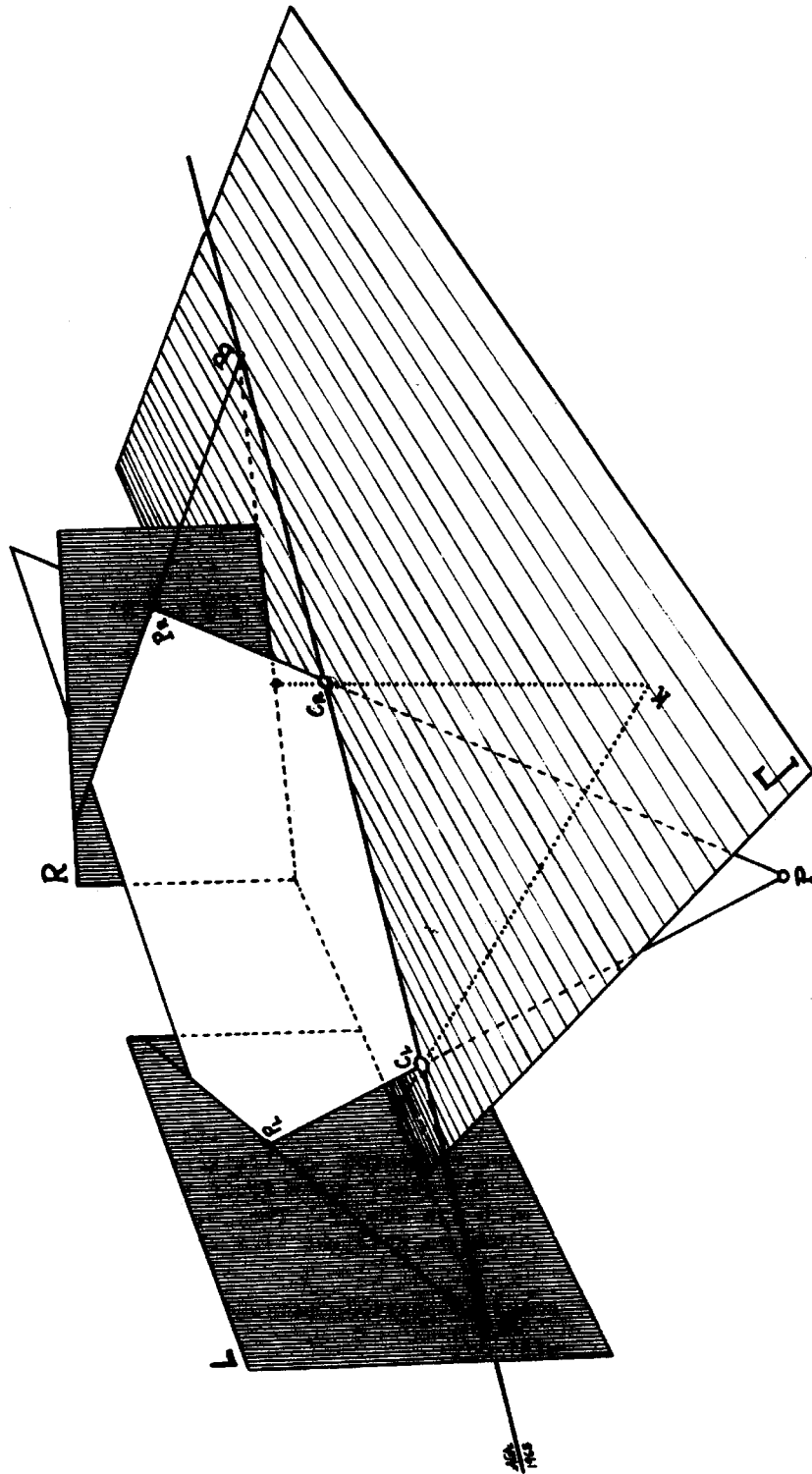


FIGURE 'GENUINE PAIRS'

Compare only points with the same  $\gamma$   
 (or the same y-coordinate).

Points with different  $\gamma$  can not  
 come from a genuine pair.

For each body, the knowledge of the 3-dim location of a few of its  
 vertices will be sufficient to position that body in real space,  
 achieving in this way the goal of this section.

See Digression 1 in section 'The concept of a body', for a  
 different approach.

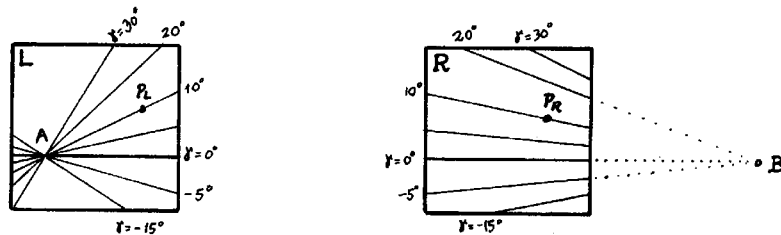


Figure 'gamma - PARAMETRIZATION'

From geometrical considerations and the coordinates of a  
 point  $P_L$  in L, it is possible to attach to the line A- $P_L$   
 an angle  $\gamma$ . Similarly, an angle is obtained for lines of R.  
 It can now be said that a genuine pair ( $P_L, P_R$ ) must  
 have the same  $\gamma$ 's for  $P_L$  and  $P_R$ .

$\gamma$  is a physical quantity, namely the angle that  
 the plane passing by the image  $P_L$  and the optical  
 centers  $C_L$  and  $C_R$  makes with the "horizontal" plane  $\Gamma$ .  
 ( $\Gamma$  contains the optical axes). Clearly, for  $P_L$  and  
 $P_R$  to be produced by a point P in 3-dim space, the  $\gamma$   
 of  $P_L$  must be equal to the  $\gamma$  of  $P_R$ . This is a necessary  
 condition that is easy to check.

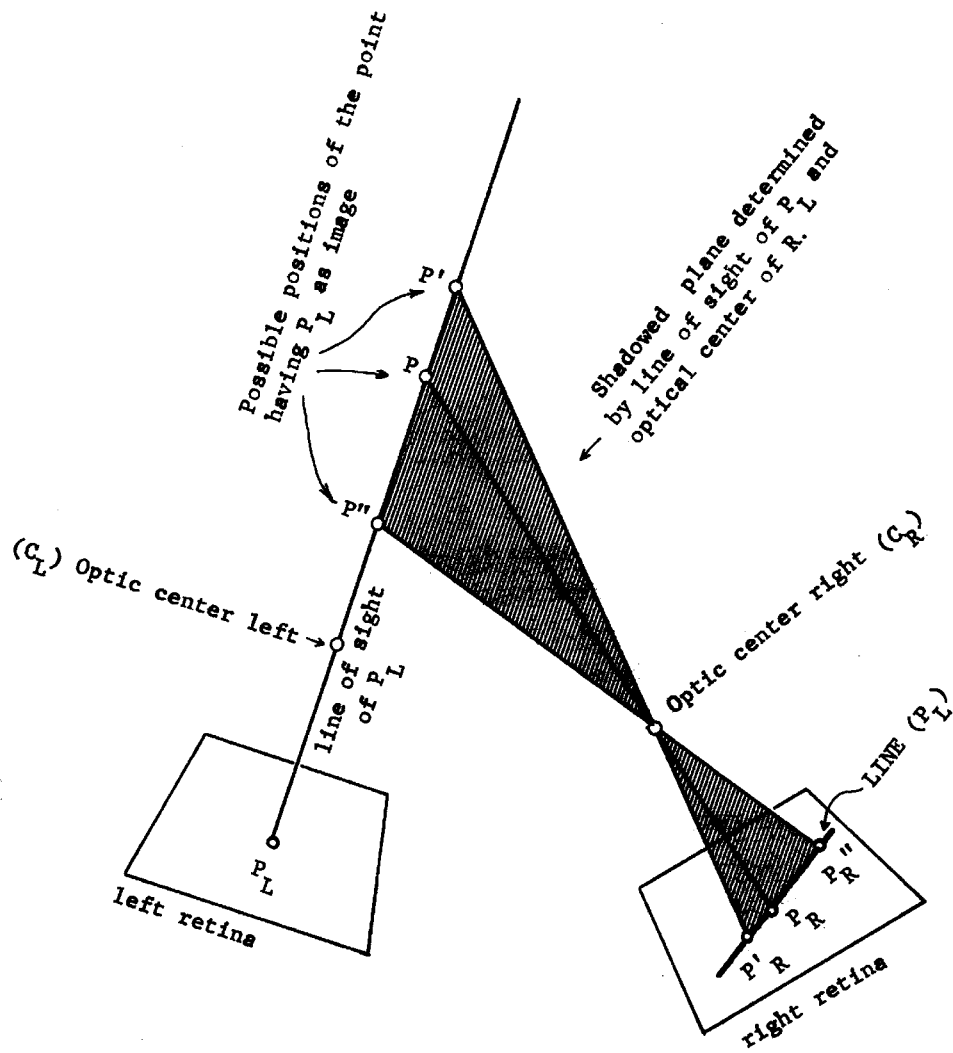
A real point P of the scene produces a left image  $P_L$  (which has  
 a certain value of  $\gamma$ ) and a right image  $P_R$  with the same value of  $\gamma$   
 (figure 'gamma-PARAMETRIZATION').

Thus, given a point in one scene, we  
 have to search for its genuine pairs  
 in the other scene among the points  
 with its same  $\gamma$ . They will be found  
 along an straight line through A or B.

Parametrization of the scene is possible not only by using  $\gamma$ ;  
 a monotonic function of  $\gamma$  will do.

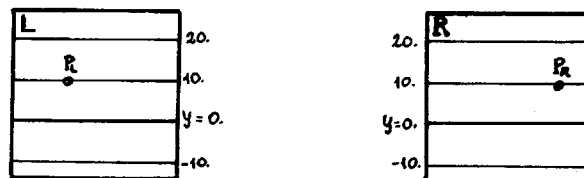
For computational efficiency, it may be advisable to store the  
 points of the scenes into arrays according to the value of their  $\gamma$ 's.





The function LINE maps points of L into lines of R. An image point  $P_L$  may have come from different 3-dim points  $P, P', P'' \dots$  all of them situated in the line of sight of  $P_L$ . The right images of  $P, P', P'', \dots$  all fall in a straight line, which is the intersection of the shaded plane [called plane  $P_L-C_L-P-C_R-P_R$  in fig. 'Genuine Pairs'] and the right retina.

When the optical axes are parallel In this case, points A and B on line  $C_L-C_R$  (fig. 'Genuine Pairs') travel to infinity, and lines  $P_L-A$  and  $P_R-B$  become horizontal (parallel to  $C_L-C_R$ ). The situation looks like



A genuine pair ( $P_L, P_R$ ) will have the same y-coordinate for both of its elements (10.0 in this case).

So that, given a left image point  $P_L$ , we have to search only among the points of R with its same height, to find "the"  $P_R$  that will make a genuine pair ( $P_L, P_R$ ).

But several genuine pairs may be found. Because on each horizontal line on R, many points may lie.

#### USE OF SEE IN STEREO PERCEPTION

We can use the invariance of the variable described in Theorem S-2 to locate objects in three dimensional space, from a pair of stereo views (we will suppose parallel axes; other case is similarly treated) as follows:

- (1) Make an analysis of the left scene with SEE, identifying the bodies.
- (2) Id. for right scene.
- (3) Reduce each body to an interval formed by two numbers, its maximum and minimum height, specifying "closed" if the absolute extremal of the body is known, "open" if not.

In this way we reduce each scene to a set of intervals (see figure 'INTERVALS').

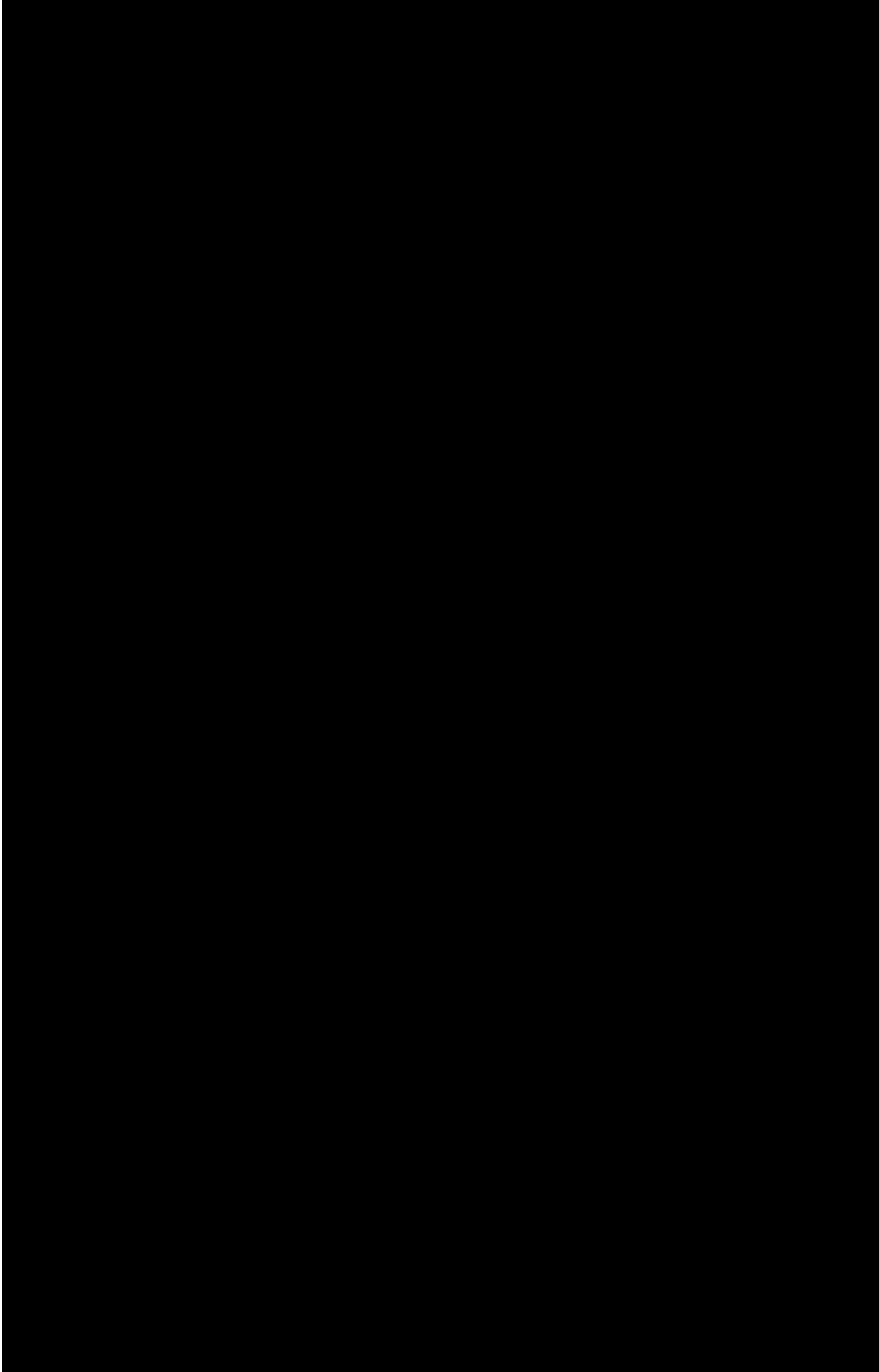
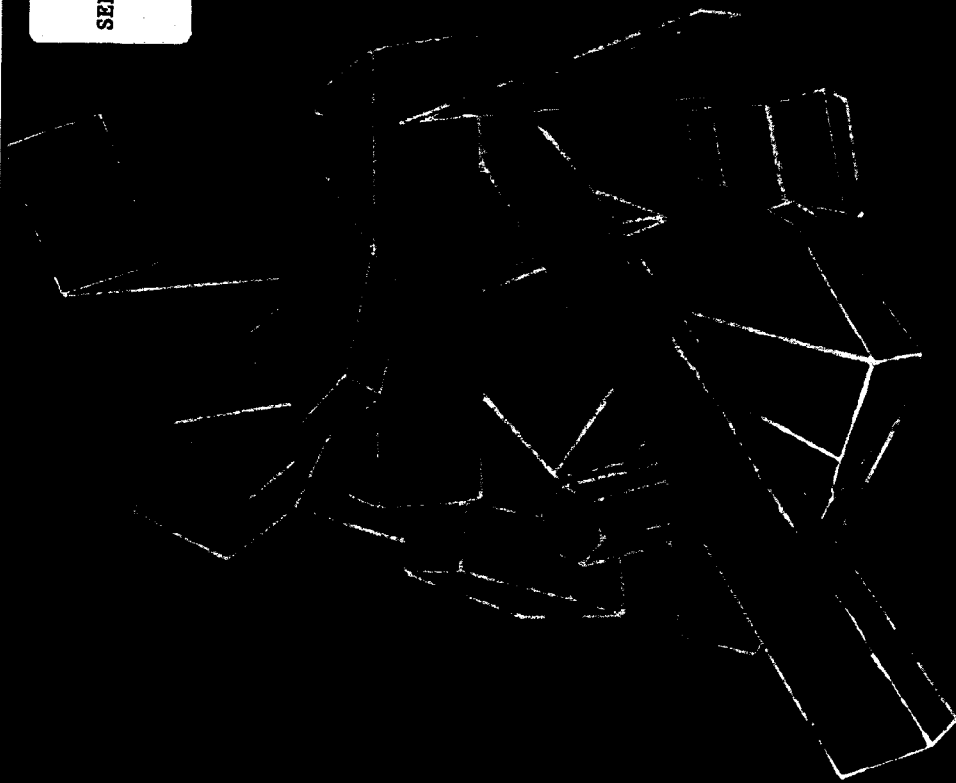


Figure 'R 1 3'  
SEE simplifies stereo perception.



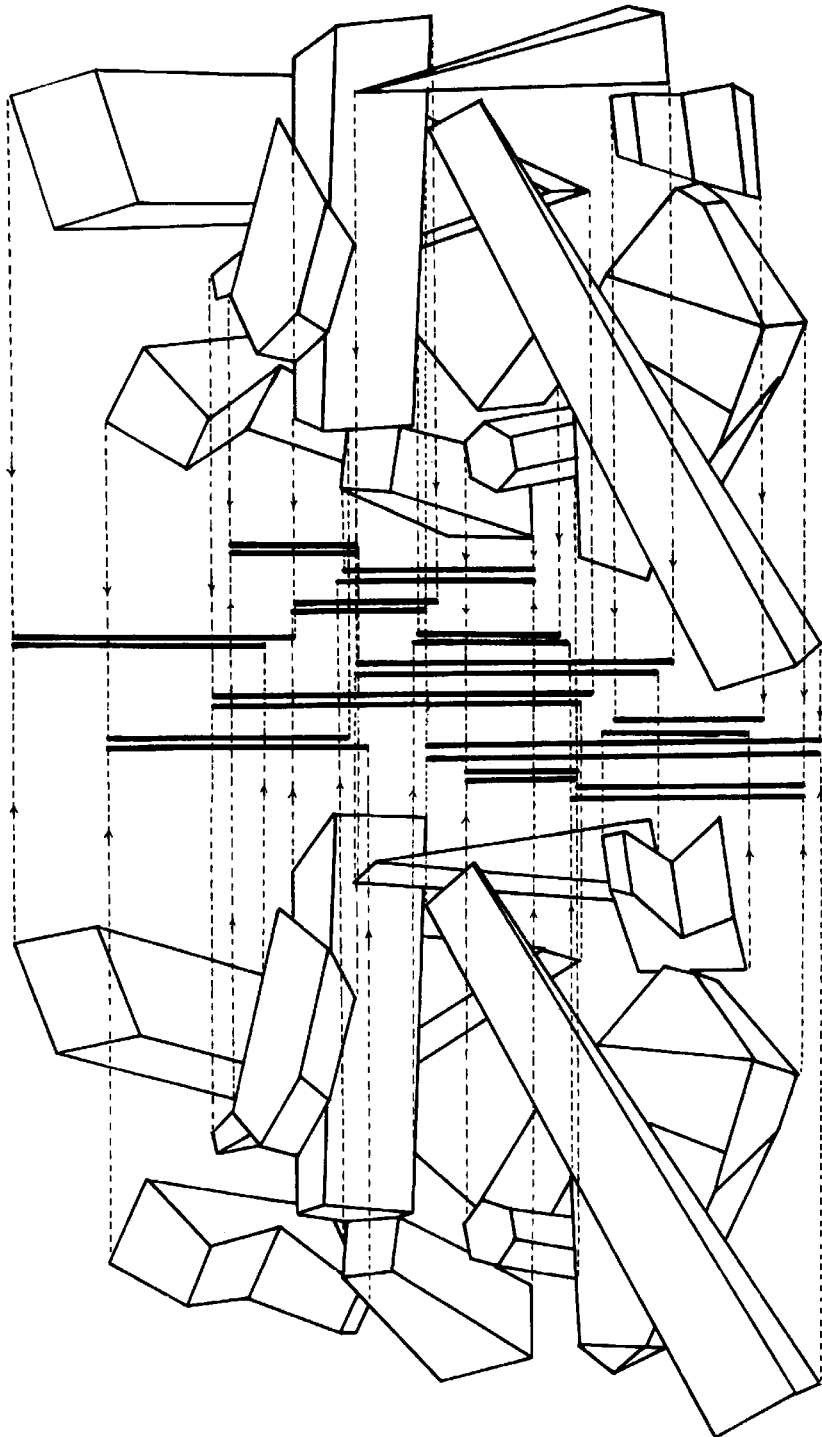
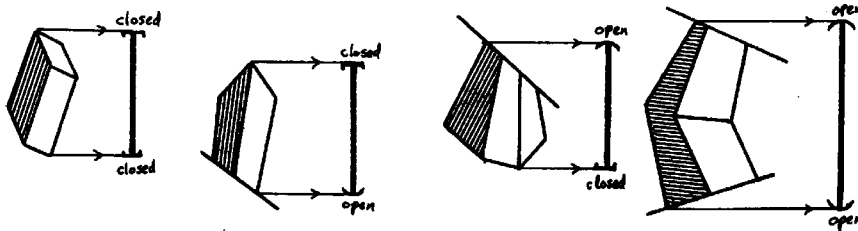


FIGURE 'INTERVALS'



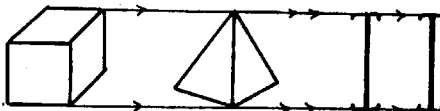
Each body is reduced  
to an interval.

- (4) Use these intervals to select which left body will go with what right body. The answer is simple (because it is unique) even in moderately crowded scenes.

It is simple to take into account the fact that an open end of an interval indicates that the interval can extend further at such end.

Sources of difficulties are:

- (a) Two bodies have the same interval, meaning they have identical maximum heights and minimum heights. This is possible.



Quite easy: reduce some faces to intervals and compare them.

- (b) A body is seen in left scene but not in right scene (figures L12, R12).
- (c) SEE partitions one body in two in one scene, but not in the other.

The "open" and "close" indications will help here.

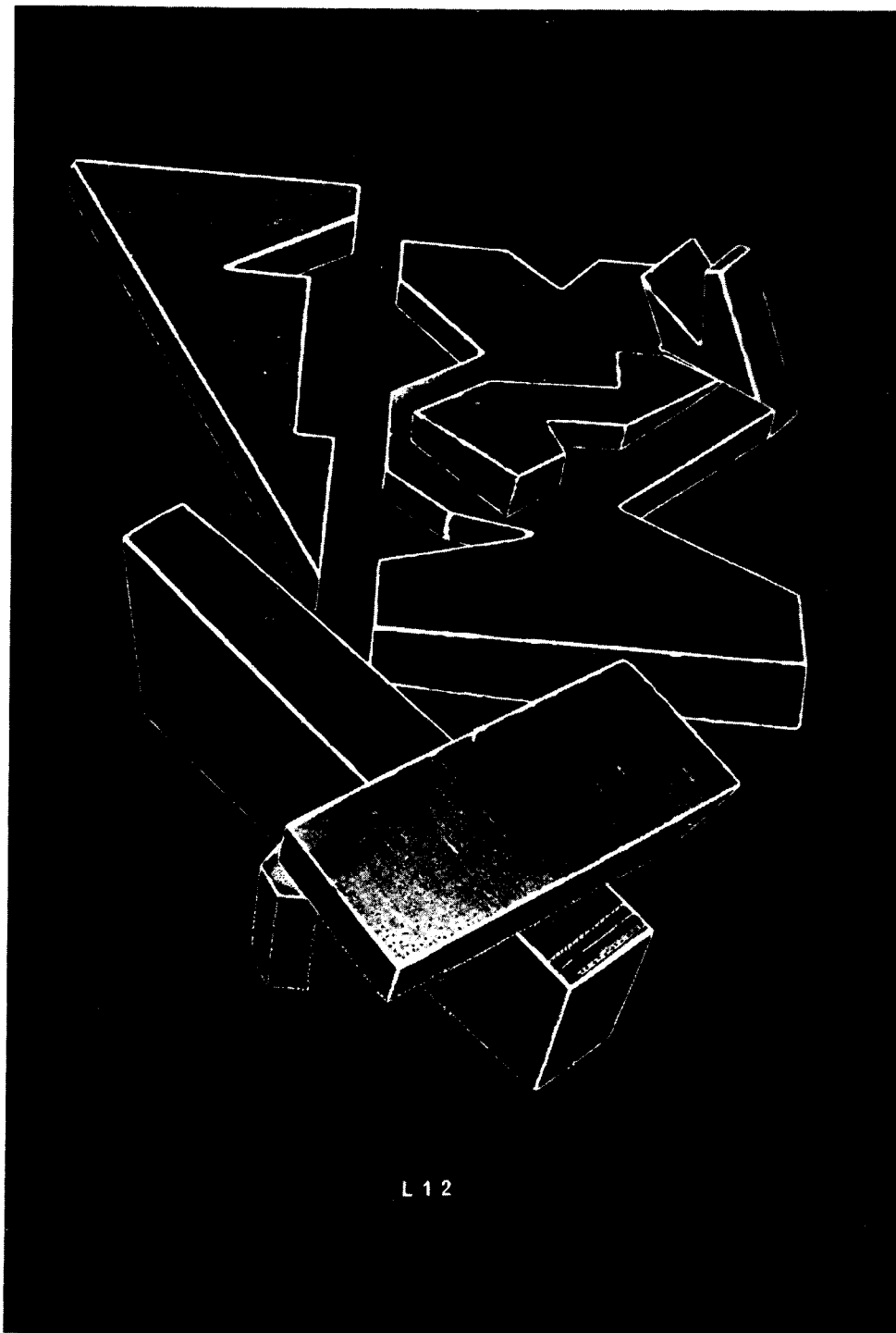
Also, remember that we are using, when comparing these intervals, just a very small part of the total information concerning each body. When the selection is narrowed down to two or three candidates ["left-body 1 is either right-body 2 or right-body 5"], one can use

- (1) the WHERE function of Griffith (op cit),
- (2) as in (a) above, the intervals for each face of the objects, so as to chose as "genuine pair" those two objects with more agreement in the intervals of their faces;
- (3) perhaps a face of unusual shape is enough for discrimination, if it appears both in left and right scenes, or the number of vertices below the center of gravity, or ...

**summary**

In summary, I should like to point out that, while much has been stated within the somewhat constricting framework of this article, much remains to be stated. Certain, but not all, important classes of presentations have been treated, and there remain horizons as yet unexplored. Conceivably, the author will attempt, *ex nihilo nihil fit*, to establish a more general perspective in the course of a subsequent article. (D.M. Jones, Delineation Nov 68). ■

Also, the reader is referred to other articles on the same topic.



L 12



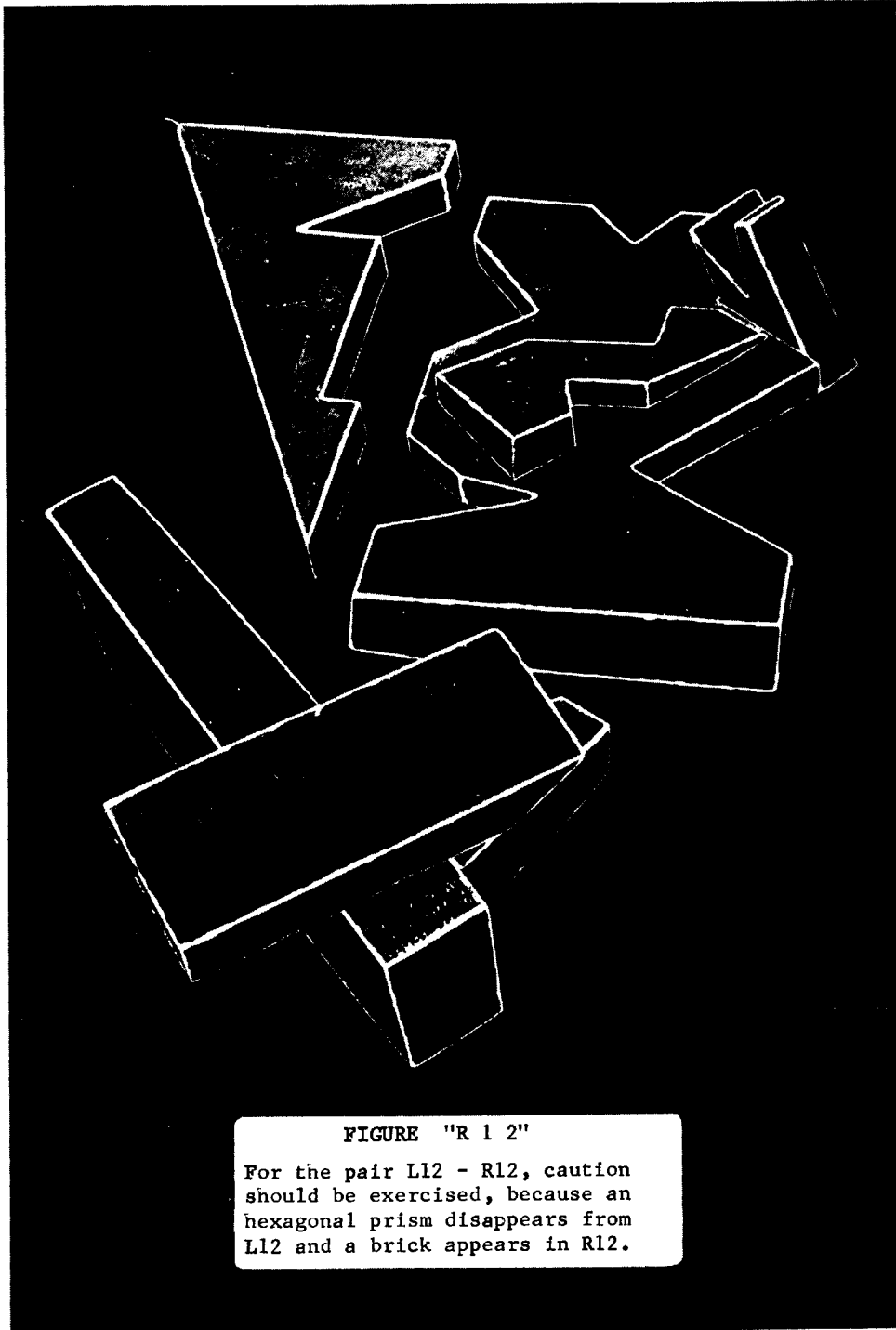


FIGURE "R 1 2"

For the pair L12 - R12, caution should be exercised, because an hexagonal prism disappears from L12 and a brick appears in R12.

Scene L10 - R10 SKE analyzes independently (pages 125 and 128) the left and right scenes, obtaining the following bodies:

```

(BODY 1. IS :5 :1 :4 :12)           LEFT SCENE (L10)
(BODY 2. IS :6 :15 :7 :11 :14)
(BODY 3. IS :8 :9 :10 :3)
(BODY 4. IS :2 :13)

                                (BODY 1. IS X:3 X:5 X:6 X:14)
RIGHT SCENE (R10)              (BODY 2. IS X:13 X:1 X:11 X:9 X:15)
                                (BODY 3. IS X:8 X:2 X:10)
                                (BODY 4. IS X:4 X:7 X:12)

```

For each of the eight bodies, we compute its minimum height and its maximum height, obtaining the following intervals:

L10	R10
:5 :1 :4 :12 → [66,105)	[67,154] ← X:3 X:5 X:6 X:14
:6 :15 :7 :11 :14 → [79,120]	[78,119] X:13 X:1 X:11 X:9 X:15
:8 :9 :10 :3 → [68,152]	[65,103] ← X:8 X:2 X:10
:2 :13 → [21,82)	[22,82) ← X:4 X:7 X:12

These intervals are compared (left with right), trying to find pairs with discrepancies between their values tolerably small [if the interval has an open end, differences can be larger]. For 'L10 - R10', these are

```

[66,105) = [65,103)
[79,120] = [78,119]
[68,152] = [67,154]
[21,82)  = [22,82)

```

that corresponds to the following identification of bodies:

```

:5 :1 :4 :12 corresponds to X:8 X:2 X:10
:6 :15 :7 :11 :14 corresponds to X:13 X:1 X:11 X:9 X:15
:8 :9 :10 :3 corresponds to X:3 X:5 X:6 X:14
:2 :13 corresponds to X:4 X:7 X:12

```

Once these correspondences between objects in the two images are found, the function (WHERE ...) {Griffith} will position these bodies in three-dimensional space, achieving our goal.

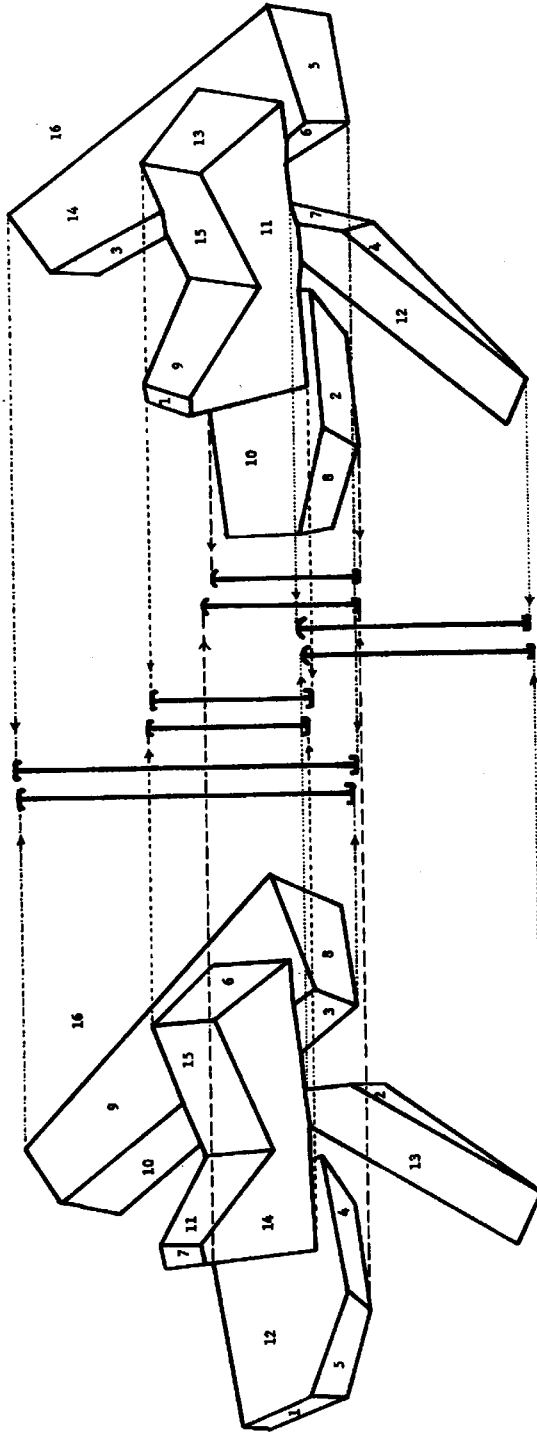


FIGURE 'L10-R10'

In order to find the three-dimensional position of these bodies in space, we proceed as follows: First, we analyze the left scene, and find (according to page 125, 'RESULTS FOR L10') four bodies: 5-1-4-12, 6-15-7-11-14, 8-9-10-3, and 2-13. Then, we analyze the right scene (see 'RESULTS FOR R10' in page 126), and find the following four bodies: 43-85-56-83A, 413-411-41-49-815, 40-82-810, and 54-57-812. Then, each one of these bodies is reduced to intervals consisting of two numbers (represented by heavy vertical lines in this drawing), the maximum and minimum height. Left and right intervals are compared and grouped in pairs consisting of intervals with the least discrepancy in their values at the ends. These pairs indicate the matching or correspondence among bodies. For this pair of scenes, the correspondence is: 5-1-4-12 with 40-82-810, 6-15-7-11-14 with 413-411-41-49-815, 8-9-10-3 with 43-85-56-83A, and 2-13 with 54-57-812. Once this correspondence is known, geometric considerations alone (see Griffith, AF Memo 143) permit us to find their three-dimensional positions.

## C O N C L U S I O N S

### LOOKING BEHIND

When I started to work on these problems, the idea was to describe an object by using a model, and with this model in memory, to search the scene looking for sub-parts of it that would fit the description.

This work ended (as far as this thesis is concerned) with a program that finds bodies without having a model of them.

But that is good.

We did not know at the beginning that this could be done.

### LOOKING AHEAD

- |    |                              |   |
|----|------------------------------|---|
| a. | Suggestions for further work |   |
| b. | Comments                     |   |
| c. | Recommendations              | All these matters are normally encountered  |
| d. | Summary                      | grouped in a chapter at the end of the work |
| e. | Conclusions                  |   |
| f. | Evaluation                   |   |
| g. | Extensions and Implications  |   |

I can only partially lump all these important matters in one final section; many times I cite them in context, that is, next to the figure or subject that evokes them, or with which they are most closely related. As a result, they are spread through the body of this dissertation.

Also,

- (1) The box SUGGESTION appears through this thesis near a

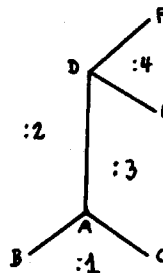
partially unsolved or partially formulated problem, and/or its partially outlined or partially new solution.

- (2) In page ~~256~~ there is a list of such suggestion boxes.
- (3) The remaining portion of this section and, in general, the sections close to the end of this work, abound in statements of type (a.) through (g.).
- (4) I have tried to start each section with a brief, and end it with a summary or conclusion.
- (5) The section 'Introduction' (page 10 ) specifies the problems treated in this thesis, and the section 'Preliminary view of Scene Analysis' (page 14 ) produces a general view of available methods.

General notation To put, remove, etc., links, we may develop a notation that will look like

**SUGGESTION**

```
(WHEN A (Y A) (B :1 C :3 D :2)
      D (K (A F ..)) (A :3 E :4 F :2)
THEN
  PUT LINK KIND 3 :3 :4
  NO LINK :1 :2 )
```



"When A is a vertex of type 'Y', and D is a vertex of type 'K', and A and D are joined as specified, then

put a link of kind 3 between region :3 and :4, and do not put a link between :2 and :1."

The general notation is


```
(WHEN P E E')
```

"when predicate P is satisfied, evaluate expression E (execute E), otherwise execute E' (which may be missing)".

In this notation, the predicate P corresponds to a geometric pattern or configuration, and the expressions E and E' to the establishment or removal of links.

In **SEE**, this part is handled by LISP functions (hand-coded), one for each particular heuristic. The suggestion is to develop this general notation, and an interpreter for it. This will speed up programming and checking, but will slow down the execution to some extent.

Use The main use of the new notation or language is for trying new heuristics. Actually, it is not difficult to hand-code the new heuristic in LISP (see function **EVERTICES** in listings), because everything reduces to calls to **NOSABO**, **TROUGHTES**, **GEV**, **SUME**, etc. I was thinking that a simple **MACRO** of Lisp could transform from notation (WHEN P E E') to LISP functional calls.

Since what the notation or language is really doing is expressing as a linear string a two-dimensional configuration , a more ambitious project would be to use the light pen and draw this configuration, and then have our interpreter or compiler produce the LISP program. This may look a little like **AMBIT-G** {Christensen}.

### Assigning a name to an object

Problem. SEE has separated a scene into bodies. What are they? Is there a pyramid among them? Where are the parallelepipeds?

To answer this, information can be supplied to the program, in the form of a symbolic description or model of the object we are trying to find. A model is an idealized account of a class of objects, all receiving the same name, like "triangular pyramid" or "house". Models may have parameters that acquire values after a given instance of the model has been found in a scene. Examples are "height" or "length of bottom side".

Some programs that follow the above procedure to name objects in a scene are described and discussed in a Master's Thesis {Guzmán}. There are difficult problems to be solved if we are to make the system able to recognize occluded objects in many situations.

One could, of course, bypass SEE and look for particular objects, as it is done by Polybrick {Hawaii 69}, a program that finds parallelepipeds.

Do not use over-specialized assumptions. Use more information In trying to solve a problem, people will apply quite different methods. They may also suppose quite different assumptions, some of which may not hold. Due to particular experience, environment, preferences, etc., some subjects may be using over-specialized assumptions, instead of requesting more data, more information to solve the problem. We may bias our views and risk arriving at conclusions (of the "common sense" type) which are valid only on restricted segments of populations, or in particular conditions or situations.

Holes. For instance, if most of the readers of this thesis [technical specialists, who have learned to read, are interested in graphical processing and computers, etc; who may not be considered a representative cross-section of Homo Sapiens] perceive "objects" a, b and c of figure 'HOLES' as holes [Winston], we may be tempted to conclude that this is a general property, and rush to write a

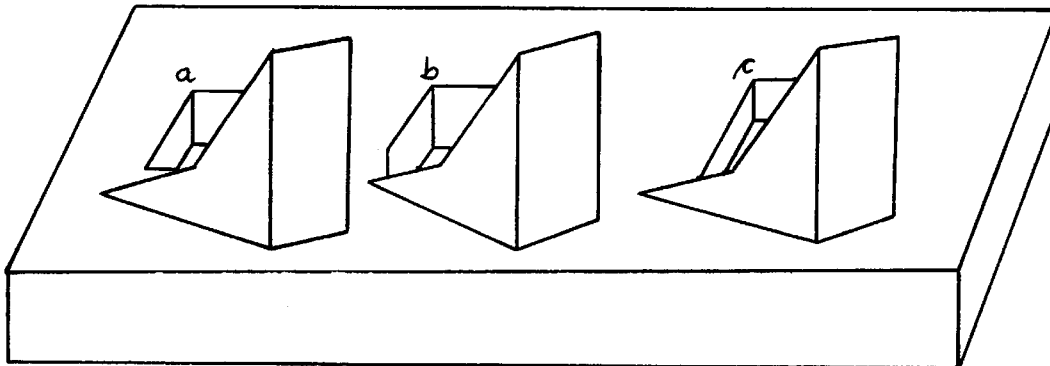


Fig. 'HOLES'

The *idea* that objects a, b, c have to be interpreted by all men, and hence by a program, as holes in the larger box, is dangerous. {cf. AI Memo 163}

subroutine to find such orifices. Perhaps other sectors of our population would simply say, with respect to a, b, c, of figure 'HOLES' that "there is not enough information to make a decision" (see also section 'On optical illusions'). Or they may come with

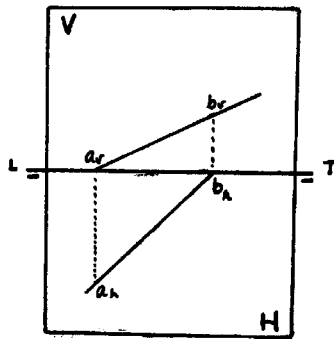


different answers, using their set of assumptions which may be different from ours, since their experience is different too. The Ames' Room (see Box, page 201) and Gregory (see Box) warn us of this.

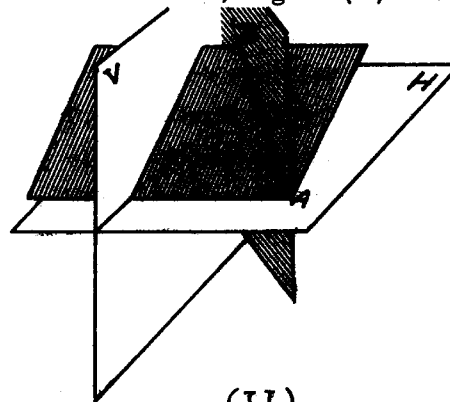
Other example of over-specialization For people familiar with Descriptive Geometry, it is easy to see that figure 'DESCRIPTIVE' (I) shows a straight line in the first octant. For them, indeed, it is easy to visualize this line in three dimensions and have a fairly good idea of its position and orientation in space, just from figure (I).

Other persons would need a more conventional figure, such as figure 'DESCRIPTIVE' (II), to visualize the same line, to get the same idea.

What happened was that the first group of persons were using specialized knowledge, their mind were trained, figure (I) was familiar to them, etc.



(I)



(II)

Figure 'DESCRIPTIVE'

Conclusion Before looking for heuristics and shortcuts, before making assumptions, deductions, etc., let us be sure that there is enough data to solve our problem.

Human perception versus computer perception Given a two-dimensional line-drawing of a three-dimensional scene, the problem of finding bodies in it is inherently ambiguous: many 3-dim scenes can generate the same 2-dim scene.

Multiple solutions are possible. More over, the metatheorem of page 39 guarantees that a solution always exists, and provides ways to construct it. We call this solution "trivial"; in effect it is trivial to write a computer program that will invariably find it.

From the multitude of possible solutions, human beings select one, which is \* different from the trivial, and call it "normal" or "common" or "standard" or "reasonable" interpretation of the scene.

Our program SEE also selects one of the many solutions. How does its selection compare with the human choice?

== When the scene is "clear", in the sense of evoking human unanimity, SEE will \* also select that same answer. Example: Figure 'TOWER'.

== As the scene or drawing gets complicated or ambiguous, mortal behavior deteriorates; opinions split, optical illusions may emerge (indicating contradictory evidence perceived), several plausible answers are emitted.

The answer of SEE in these cases will \* be found among the humanly plausible selections. In some cases, it may not agree with the majority.

== Finally, people make mistakes. They will see an object that is not there, or will fail to see an object, or classify it as "impossible".

But SEE also errs. It sometimes succeeds where people fail, more often it is the other way around.

---

\* In an overwhelming majority of cases.

## TABLE "ASSUMPTIONS"

### ASSUMPTIONS MADE BY THE PROGRAM

These assumptions have to be obeyed for SEE to give good results:

- == The objects are three-dimensional solids formed by planes <sup>(1)</sup>.  
No needles or cardboards allowed.
- == They produce a two-dimensional image or projection where all lines are straight <sup>(2)</sup>.
- == Faces have no drawings, marks, labels, etc., imprinted on.
- == Objects do not have holes in them.

---

<sup>1</sup> See section 'On optical illusions' for conditions for partial lifting of this assumption.

<sup>2</sup> See section 'On curved objects' for conditions for partial lifting of this assumption.

### ASSUMPTIONS NOT MADE BY THE PROGRAM

These assumptions are not necessary for the correct functioning of SEE; it will work well with or without them.

- == Only prisms are allowed.
- == The scene is a parallel projection, or isometric drawing.
- == The objects are convex.
- == The model or description of the object has to be known to SEE.
- == The objects have to appear unoccluded or unobstructed in the view.
- == The objects have "weight" in the vertical direction and will fall if not supported.
- == The background is known in advance (See 'On background discrimination by computer').

I repeat, these assumptions are **NOT** obeyed by our program.

LIST OF SUGGESTIONS

PAGE

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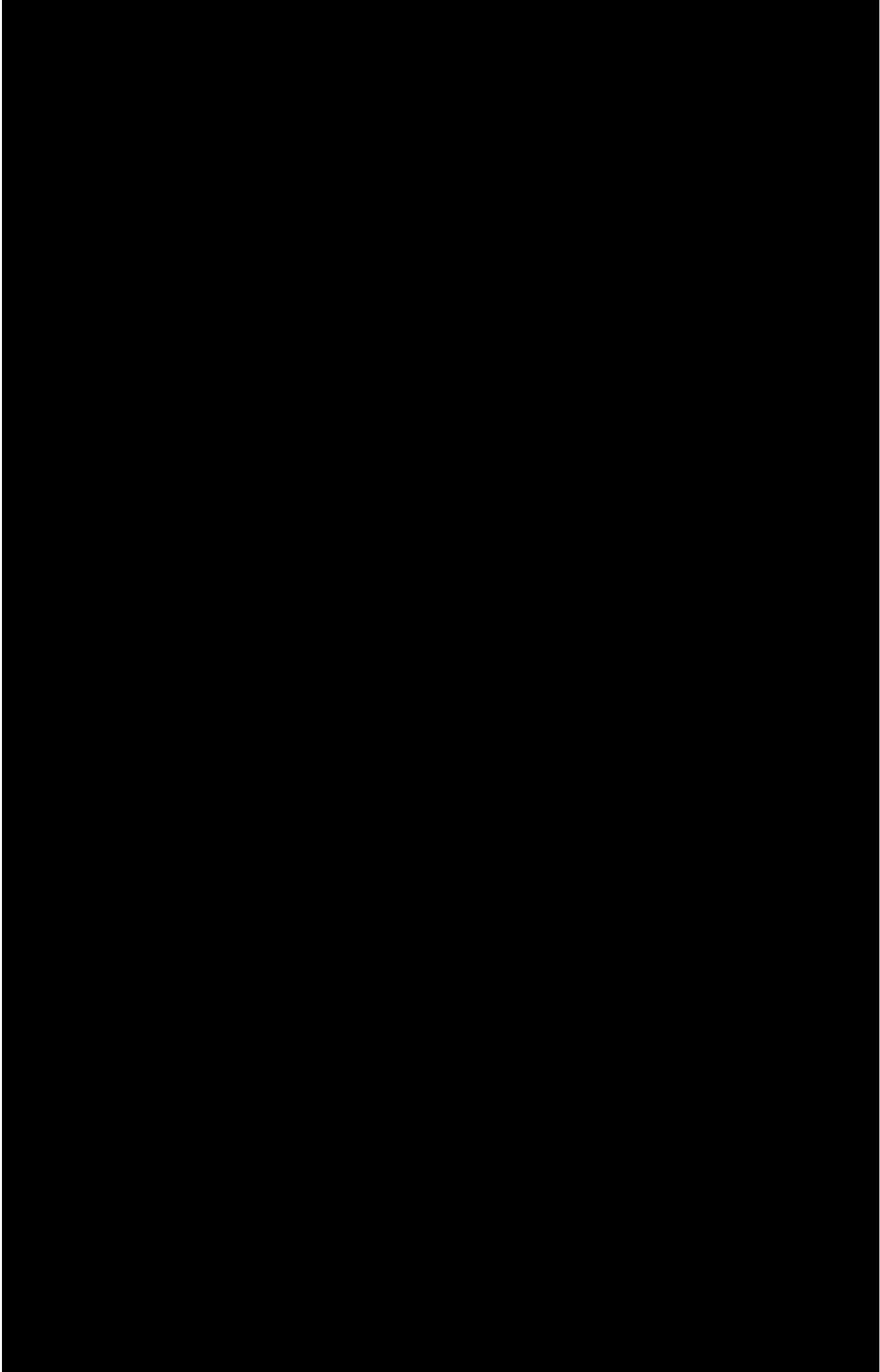
205

221

229

248

250



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NOTES: Reports with AD numbers (such as AD-652-017, page 286) can also be obtained as follows:

Government contractors may obtain copies of this report from the Defense Documentation Center, Document Service Center, Cameron Station, Alexandria, Virginia 22314. Orders will be expedited from DDC if placed by your librarian, or some other person authorized to request documents.

Other U.S. citizens and organizations may obtain copies of this report from the Clearinghouse for Federal Scientific and Technical Information (CFSTI), Sills Building, 5285 Port Royal Road, Springfield, Virginia 22151.

Comm.ACM = Communications of the Association for Computing Machinery.

Proc. FJCC = Proceedings of the Fall Joint Computer Conference

Proc. SJCC = Id. Spring. (Spartan Books, or Thompson Books, Co. Washington, D. C.)

## ANNOTATED LISTING OF THE FUNCTIONS USED

You do not have to know these things in order to use SEE (reading 'How to use the program' in page 76 is enough) or to understand what it does (it is explained in 'SEE, a program that finds bodies in a scene', page 88); these things are put here merely for completeness and to make easier the understanding of the inner workings of SEE.

A listing is a formal description There is a stronger reason, however. A listing of the programs is a formal description, an algorithm, an exact statement in a formal language of what we may have been describing, perhaps inaccurately, in a natural language (English). It becomes the starting point of serious discussions. The reader who is skeptical at some point, or did not understand some English statement, can always clarify his doubts in the listing. To be understandable, the listing has to have annotations, comments.

A mathematician is not forced to explain his work always in natural language, but rather he is allowed to employ abstract notations, symbolisms, formalizations of his thoughts (indeed, it is preferable this way). A programmer should not hide his listings (he should not be forced to re-state his algorithms in natural language exclusively { 68}) and force his readers to use the ambiguous channels of his natural language communication.

And this brings another point. Not only a programmer should not hide the listing (unless there are <sup>new</sup> bugs or incomplete subroutines), but he should not hide the programs (unless they are banal); by this I mean honest and reasonable efforts should be made to facilitate future potential users the access to these programs. Include:

- Documentation
- Listings, tape or card deck names, etc.
- Test data
- Printout of an interaction with such test data, including loading, compilation, execution, results.
- Time spent (by machine and by man).

See also R. Kain's letter {C. ACM March 67}.



FREE FILES 16    FREE BLOCKS 100  
 BACK    MACRO 2  
 -TECO    OUTPUT 8  
 SUFTIME 230C04 340  
 SO 3 8  
 SORT    LAP2 10  
       TECO 3  
 \*  
 FREE FILES 7    FREE BLOCKS 40  
 RESULT 888.87 40  
 SEECMP 870L8 48  
 DISPLAY CUM87 9  
 RESULT 888.87 20  
 SEE 1 100  
 SEECMP 87 40  
 RESULT 888.87 14  
 EXPFORM TSCERS 7  
 SEE 58 36  
 RESULT 888.83 41  
 SORT    LAP2 10  
 TRAC 11 10  
 RESULT 888.87 31  
 REB44R CH,MR8 11  
 SEE 59 36  
 REB44R L-HARD 8

THE DIRECTORY OF TAPE GUZMAN \*

\* irraduant  
 ← This file contains a backup of all the english (ASCII) files of TAPE GUZMAN F, as of Dec 23, 1968  
 \* irraduant

23 DICIEMBRE 1968    Adolfo Guzmán Arce

(This tape is shown below.

FILE DIRECTORY OF TAPE GUZMAN F → It contains the programs and results.  
 Results of SEE on some LVAR, LI, RI, VARI, U, S, V, L, V, T, etc. Data are in tapes GUZMAN C and GUZMAN CVT.  
 and used to display a scene, or to dump it on the Calcomp plotter.

Results of SEE applied to Tower, Corn, Herd, Wind.  
 SEE 1 is a binary dump of LISP (44 blocks) + All SEE programs To load it: **LI 81, SEE 12, SE** → The file SEE 1 is not  
 One of the two files needed to create SEE. To load it into LISP: (UNLOAD SEECMP 57) SE ... 88 ... SE disregard ← EQ%  
 Results of SEE applied to some AS, PER, M, L, etc. Use these  
 Example of 'FORMAT' A scene or internal format of scene 83. error messages  
 Load this file by (UNLOAD SEE /54) EQ into LISP. Also load SORT LAP2 and SEECMP 87. (Use about 3,000  
 Results of scenes Bridge, spread, LE, memo, Home, Wind, Arch; they were obtained with SEE 88 and record 53. words of filename  
 If you do not have a SORT function, load this file. At the end, say (terminal T) replace  
 Tracing LISP functions.  
 Results of SEE 88 and SEECMP 87 applied to scenes spread, memo, bridge, IT (or cases), corn, home, tower.  
 Results of MACH and WAIETM  
 HIGHEST VERSION of SEE as of Dec 23 1968.  
 Results of SEE on "THAT" and "HARD": All these results appear in this thesis in section "ANALYSIS OF MACHY  
 SERIES".

In the next listing we show the files SEE 58 and SEECMP 57, which contain all the functions needed (except SORT) to create "SEE".  
 They are written in the LISP programming language.

TO USE THE PROGRAM,  
 SEE PAGE 78

```

SEE 56 P In type (user) P.
Version number 56.
(SETG PRONA (QUOTE (SEE /56)))
(DEFPROP SUSPICIOUS (LAMBDA (R)
  IPROC (LS FORKS ARROWS IS KB XS PEAKS MULTIS VA NA L)
  (SETG L (LENGTH (SETG S) (SETG N KVERTICES)))
  (CUENTA S)
  (COND (SB (BREAK WITH R LS FORKS ARROWS))
    (COND (NA (PRINT (LIST NA S (QUOTE (ERROR SUSPICIOUS))))
      (GREATERP
        (PLUS (LENGTH (HAVING (FUNCTION (LAMBDA (K) (EG N (CAADR (SETG K TYPE)))))) LB))
        (LENGTH (HAVING (FUNCTION (LAMBDA (K) (NOT (EG R (CADDR (CADDR (CADDR (SETG K TYPE)))))))
          (LENGTH (HAVING (FUNCTION (LAMBDA (K) (UNDEF K K))) IS)))
          (QUOTIENT L 9.))
        (GO LIMPLO)))
    SUSPICIOUS
    (COND ((GREATERP L 25.) (PUTPROP R (QUOTE BACKGROUND) (QUOTE BACKGROUND)))
      (PUTPROP R (QUOTE SUSPICIOUS) (QUOTE SUSPICIOUS))
      (RETURN T)
      LIMPLO
      (COND ((GREATERP L 25.) (PUTPROP R (QUOTE BIFACE) (QUOTE BIFACE)) (PRINT (OU ((EV R) IS BIFACE))))
        (MEMPROP R (QUOTE SUSPICIOUS))
        (RETURN ()))
      (RETURN ()))
  EXPR)
(DEFPROP GETWA (LAMBDA (K)
  (SETG K BACKGROUND))
  EXPR)
(DEFPROP PUBA (LAMBDA (R)
  (COND (NULL (HAVING (FUNCTION (GETWA) (SETG R NEIGHORS))) (PUTPROP R (QUOTE BACKGROUND) (QUOTE BACKGROUND))))
  EXPR)

```

To be classified as simple,  
 some regions have to  
 have at least 4 + 1 number  
 of each of "j-sides" vertices.  
 Big faces are simple, too.

T if R has no background neighbors, marking also R as background









```

K
(FUNCTION
 (LAMBDA (J) (MEMQ (CAR V) (CAR J))))
(NCNC (CAR K) (CAR S)) Merge betn. by increasing (car K)
(PLACU K
 (COMPACTIFY (APPEND (CDR K) (CDR S))))
(RPLACA S ()) } S: // : . The, also affixes R, because
(RPLACU S ()) } : belongs to R.
)

(GETU (CAR V) SLNK))))
(GETU (CAR K) SLNK))))
SMB))
RESULTS
(PRINT (QUOTE RESULTS))
(SETU U 0)
(COND (S3 (PUTPROP S
 (NCNC (MAPCAR (FUNCTION (LAMBDA (N) (FOBODY (CAR W)))) S3) (GETO S BODIES))
 (QUOTE BODIES))
 (PRINT (QU (THE FIRST (EV U) BODIES ARE (EV* S3))))))
(MAPC (FUNCTION
 (LAMBDA (J)
 (OR (NULL (CAR J))
 (SINGLE (CAR J))
 (GETU (CAR J) BACKGROUND)
 (AN' (CPROP S (FOBODY (CAR J)) (QUOTE BODIES)) ())
 (PRINT (QU (BODY (EV U) IS (EV* (CAR J)))))))
 R)))
)
EXPR)
(DEFPROP FOFBODY (LAMBDA (B)
 (LIST (SETU U (AUDI U)) (QUOTE BREGIONS) B) )
 EXPR)
(DEFPROP DIPJ (LAMBDA ()
 (LET (QUOTE DIA) (QUOTE (EXPR FEXPR SUBR FSUBR))) )
 EXPR)
(SETU LIMP 1)

```

*we are almost done ; ; contains nuclei which were incremented by locally regions.*

*ready from each nucleus.*

*The non-singla-region bodies are also announced*

*T of the display functions are in core*

*T for show display*



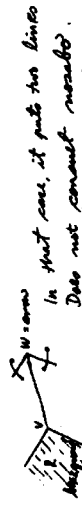
```

(DEFPROP KONFORK (LAMBDA (M N)
  (AND (GET R BACKGROUND)
    (SUME M SE)
    (EQ (EQ O) (QUOTE ARROW))
    (EQ (EQ S) V)
    (GEV (EQ S) (EQ T))
    (GEV (EQ O) (EQ T))))
EXPR)

(DEFPROP NUVA (LAMBDA L (DO J L
  (SUBJ J) (EQ J O)
  (COND ((GETO (ANS J) BACKGROUND) (RETURN ())))))
EXPR)

(DEFPROP PARL (LAMBDA (Y X M V)
  (PRAVING (FUNCTION GETKSA) (GETU Y NEIGHBORS))
  ((LAMBDA (A K L)
    (AND (PBACK (PROG2 () A (SETO A (CAR (LAST A))))))
    (PBACK (PROG2 ((SETO A (CTHEFIRST (GETO X FOOP) (FUNCTION CONTAINS V))) (SETO A (CAR (LAST A))))))
    M
    V))))
EXPR)

```



In that case, it puts two lines  
Does not construct numbers.  
Here v is free variable, could be any type of writer.  
If R is background and w is an arrow with v in the initial Tail. Use EG.

regress  
 $T$  if some of  $a, b, c, \dots$  are background  
 $(\text{make } a \text{ b } c \dots) = T$  if some of  $a, b, c, \dots$  are background  
 always  $F$  parallel to  $w$   
 $v$  not longer  $w$   
 $x$   $y$   $z$   $w$   
 always  $F$  parallel to  $w$

```

(DEFPROP TESTUDY (LAMBDA (C B)
  (COND ((AND (NOVA (EM 7.) C)
    (STUDY V)
    (OR (NOT (EQ (SEF O) (QUOTE T)))
      (AND (NOT (EQ (SEF S) V)) (OR (NOT (STUDY B)) (LESP O V))))
      (PARL (EM 7.) C B V))
    (GEV (EM 7.) C))))
EXPR)

(DEFPROP CU (LAMBDA (A) (CDAR A)) FEXPM)

```

Study is not working now.

Get with general argument

7



1. Clean old scene (under name 'scene'; if value of name is 'final'; clean scene 'final')  
 2. Transform a few input format to internal format

```

(DEFPROP PREPARA (LAMBDA (A)
  (PROB (BACKGROUND M Z)
    (SETO BACKGROUND (QUOTE BACKGROUND))
    (SETO A
      (LAMBDA (B) (COND ((CDR A) (REMPROP M BACKGROUND) B) (T B)))
      (CONS (ATOM (CAR A)) (CAR A)) (T (CADAR A))))))
  CLEAN
  (CLEAN (SETO SCENE REGIONS) NEIGHBORS VERTICES FOOP BACKGROUND SUSPICIOUS WIFACE BLINK)
  (CLEAN (GETS SCENE VERTICES) XCOR YCOR KIND NVERTICES NREGIONS SLOP TYPE NEXTE)
  (MAPC (FUNCTION (LAMBDA (J) (REMPROP (CADR J) (QUOTE FAS)))) YES)
  (SETO YES (.... (copy many) ....))
  (SETO BLINK ()))
  (CLEAN (LIST SCENE) REGIONS VERTICES BACKGROUND)
  (COND (OPR (BREAK IN PREPARA)))
  INITIALIZE
  (SETO SCENE A)
  (PRINT (QUOTE (LLEN A)))
  (LLEN (EVAL A))
  (MAPC (FUNCTION (LAMBDA (K) (PUTPROP K BACKGROUND BACKGROUND))) (SET A BACKGROUND))
  (PRINT (QUOTE FOOP))
  (MAPC (FUNCTION
    (LAMBDA (K)
      (PROG2 (PUTPROP K
        (APPLY (QUOTE NCONC)
          (MAPCAR (FUNCTION CULL)
            (PUTPROP K (FOOP (GETO K NVERTICES) K) (QUOTE FOOP))))
        (QUOTE NEIGHBORS))
        (PUTPROP K
          (APPLY (QUOTE NCONC)
            (MAPCAR (FUNCTION (LAMBDA (J) (CALL (CDR J))) (GETO K FOOP)))
            (QUOTE NVERTICES))))))
    (GETO SCENE REGIONS))
  (SETO B (GETO SCENE VERTICES))
  (PRINT (QUOTE TYPEGENERATOR))
  (MAPC (FUNCTION (TYPEGENERATOR) B))
  (PRINT (QUOTE MATES))
  (MAPC (FUNCTION MATES) B)
  (SETO Z T)
  (MAPC (FUNCTION MATES) M)
  (PRINT (QUOTE NEXTE)))
  (MAPC (FUNCTION NEXTE) YES)
  (LOND (INULL (SET SCENE BACKGROUND))) (PRINT (SU (SEARCHING FOR BACKGROUNDS OF (EV A)))) (IF (NULL) (LOOK FOR BACKGROUND.
  (RETURN 105)))
  (RETURN 105)))
  FLAPR)
  (DEFPROP UNDER (LAMBDA (R)
    (PROG2 (UNDEA (GETO R NVERTICES)) (UNDEA* T8) )
    (EXPR)
    (DEFPROP UNDER* (LAMBDA (S)
      (CONS (INULL B) S) (UNDE1 (CAR S) R) (CONS (EG 5.) (CONS (EG 6.) (UNDE* (CDR S)))) (T (UNDE* (CDR S))))))
      (EXPR)
      (DEFPROP UNDE1 (LAMBDA (U R)
        (LOND (SUME B EG) (EG (EG B) (QUOTE T)) (EG (EG 7.) R) (GOODT B) (SUME B EG)))
        (EXPR)

```

*Set foo*

*put vertices*

*Generate types  
Generate classes of T's*

*Generate matching T's or nexte.  
If (NULL) look for background.*

3

R.S. regions. True if they are overlaid - Good neighbors - at the same level -  
 Reflect if one passes under the other  $\frac{K}{S}$  or  $\frac{R}{E}$   
 The common boundary should not contain L's, forks, arrows, K's, X's, peaks, multis.

(DEFPROP GOODPAL (LAMBDA (K S)  
 (NOT (OR (MEMBER R (UNDER S))  
 (MEMBER S (UNDER R))  
 (AND (CUENTA (BOUNDARY R S)) (I))  
 LS  
 FORKS  
 ARROWS  
 KS  
 XS  
 PEAKS  
 MULTIS  
 (HAVING (FUNCTION  
 (LAMBDA (K)  
 (COND ((ISUME K EM) (AND (OR (EQ (EM S) R) (EV (EM S) S)) (INSABO (EM S) (EM S) (EM 2))))))  
 (S))))))

Also should not contain  $\frac{K}{S}$  or  $\frac{R}{E}$  an impediment

(DEFPROP BOUNDARY (LAMBDA (R S)  
 (COND ((MEMBER S (SETS R NEIGHBORS)) ((LAMBDA (FOOP) (CHOUNI (CAR (LAST FOOP)) FOOP))  
 ((LAMBDA (V) (CTHEFIRST (SETG R FOOP) (FUNCTION CONTAINS))) S))))))  
 EXPR)

(DEFPROP GROUND1 (LAMBDA (E L)  
 (COND ((NULL L) L)  
 ((EV (CAR L) S) (CONS E (CONS (CADR L) (GROUND1 (CADR L) (CDR L))))))  
 (T (GROUND1 (CADR L) (CDR L))))))  
 EXPR)

(DEFPROP COMPLEMENT (LAMBDA (S U)  
 (COND ((NULL S) S) (MEMBER (CAR S) U) (COMPLEMENT (CDR S) U)) (T (CONS (CAR S) (COMPLEMENT (CDR S) U))))))  
 EXPR)

Remove 'quote' for compilation.

(QUOTE (SPECIAL 37A88UCP 37A88UCG))  
 (DEFPROP FORALL (LAMBDA (37A88UGL 37A88UCP 37A88UCG)  
 (FORALL\* 37A88UGL))  
 EXPR)

(DEFPROP FORALL\* (LAMBDA (37A88UGL)  
 (COND ((NULL 37A88UGL) 37A88UCG)  
 ((37A88UCP (CAR 37A88UGL)) (CONS 37A88UCG (CAR 37A88UGL))) (FORALL\* (CDR 37A88UGL))))))  
 EXPR)

(DEFPROP FURFIRST (LAMBDA (37A88UGL 37A88UCP 37A88UCG)  
 (FURFIRST\* 37A88UGL))  
 EXPR)

(DEFPROP FORFIRST\* (LAMBDA (37A88UGL)  
 (COND ((NULL 37A88UGL) 37A88UCG)  
 ((37A88UCP (CAR 37A88UGL)) (LIST 37A88UCG (CAR 37A88UGL))))  
 (T (FORFIRST\* (CDR 37A88UGL))))))  
 EXPR)

(QUOTE (UNSPECIAL 37A88UCP 37A88UCG)) Remove 'quote' for compilation.

(DEFPROP THEFIRST (LAMBDA (S/37A88UGL S/37A88UCG)  
 (HAVING S/37A88UGL S/37A88UCG))  
 EXPR)

(Thefirst (L P)) = a list with the first element of L satisfying predicate P  
 = (flaming P L)

(DEFPROP CTHEFIRST (LAMBDA (S/37A88UGL S/37A88UCG))

9

```
(COND ( (SETU #/+*JUL (TIMEFIRST #/+*JUL /-#JUL) (CAR #/+*JUL) (T (BREAK 1 OTHERFIRST NULL))))
  (EXP)
  (DEFPROP CONTAINS (LAMBDA (J)
    (MEMQ V J) )
    (EXP)
```

(10)

END OF FILE SEE 58 F















*Remove repeated elements from its argument. Modify list structure.*

```

(DEFPROP COMPACTIFY (LAMBDA (A)
  (MAP (FUNCTION
    (LAMBDA (A)
      (COND ((OR (NULL A) (NULL (CDR A))))
            ((MEMBER (CAR A) (CDR A)) (REPLAC A (CDR A)))
            (A)))
    A))
  A))
)

(SETO RPAR (QUOTE /)) (SETO LPAR (QUOTE (/))) (SETO STET (QUOTE STET)) (SETO / (QUOTE /)) } handles for PRINTP
(SETO PREC (/))

(DEFPROP PRINTF (LAMBDA (A) (PROG2 (TERPRI) A (PRINTP A) (PRINTC (QUOTE /)) (EXPR)
  (PRINTP A))
  A))
)

(DEFPROP PRINTP (LAMBDA (A)
  (COND ((NULL A))
        ((ATOM A) (AND PREC (PRINC PREC)) (PRINC A) (PRINC /) A))
        ((EQ (CAR A) STET) (PRINC (CDR A)))
        ((PRINTP (CAR A)) (PRINTP (CDR A))))))
  A))
)

(DEFPROP PBACK (LAMBDA (F)
  (COND ((NULL F) ())
        ((AND (GET (CAR F) BACKGROUND) (MPARA K L A (SLOP A (SETO A (CDR F))))))
        (T (PBACK (PROG2 (SETO A (CDR F)) (CDR F))))))
  A))
)

(DEFPROP SINGLEBODIES (LAMBDA (A)
  (AND (NULL (CDR A))
        (NULL (CDR A))
        (SETO % (CDR A))
        (SETO % (FHAVING (FUNCTION (LAMBDA (X) (AND (NOT (EQ X A)) (MEMBER % (CDR X)))))) R))
        (PRINT (QU (SINGLEBODY ASSUMES (EV (CAR %)) (EV (CAR A)) SAME BODY)))
        (INCOND (CAR %) (CAR A))
        (REPLAC A ()))
  A))
)

(DEFPROP PELIN (LAMBDA (A L)
  (COND ((NULL L) T)
        ((OR (EQ A TYPE) (EQ (CAR L) TYPE)) (PELIN (CAR L) (CDR L)))
        (T (OR (INOSABO V (GET (GETO V KIND) A)) (SEV A (CAR L))) (PELIN (CAR L) (CDR L))))))
  A))
)

(DEFPROP TRIANG (LAMBDA (R)
  (COND ((AND (EQ 3 LENGTH (SETO % (SETO R KVERTICES))))
        (EQ 2 LENGTH (SETO % (HAVING (FUNCTION (LAMBDA (K) (EQ (QUOTE T) (CAR (SETO K TYPE)))))) %)))
        (OR (NOT (EQ R (CDR %))) (SETO % (REVERSE %)))
        (SUME (CAR %)) (EV)
        (SUME (CDR %)) (EV)
        (EQ (EV 1) R)
        (EQ (EV 1) R))
        (LIST R (CAR %) (CDR %; K))))
  A))
)

(DEFPROP TRIALINK (LAMBDA (L)
  (MAP (FUNCTION
    (LAMBDA (J)
      (COND ((OR (NULL A) (NULL (CDR A))))
            ((MEMBER (CAR A) (CDR A)) (REPLAC A (CDR A)))
            (A)))
    A))
  A))
)

(DEFPROP PRINTF (LAMBDA (A)
  (PROG2 (TERPRI) A (PRINTP A) (PRINTC (QUOTE /)) (EXPR)
    (PRINTP A))
  A))
)

(DEFPROP PRINTP (LAMBDA (A)
  (COND ((NULL A))
        ((ATOM A) (AND PREC (PRINC PREC)) (PRINC A) (PRINC /) A))
        ((EQ (CAR A) STET) (PRINC (CDR A)))
        ((PRINTP (CAR A)) (PRINTP (CDR A))))))
  A))
)

(DEFPROP PBACK (LAMBDA (F)
  (COND ((NULL F) ())
        ((AND (GET (CAR F) BACKGROUND) (MPARA K L A (SLOP A (SETO A (CDR F))))))
        (T (PBACK (PROG2 (SETO A (CDR F)) (CDR F))))))
  A))
)

(DEFPROP SINGLEBODIES (LAMBDA (A)
  (AND (NULL (CDR A))
        (NULL (CDR A))
        (SETO % (CDR A))
        (SETO % (FHAVING (FUNCTION (LAMBDA (X) (AND (NOT (EQ X A)) (MEMBER % (CDR X)))))) R))
        (PRINT (QU (SINGLEBODY ASSUMES (EV (CAR %)) (EV (CAR A)) SAME BODY)))
        (INCOND (CAR %) (CAR A))
        (REPLAC A ()))
  A))
)

(DEFPROP PELIN (LAMBDA (A L)
  (COND ((NULL L) T)
        ((OR (EQ A TYPE) (EQ (CAR L) TYPE)) (PELIN (CAR L) (CDR L)))
        (T (OR (INOSABO V (GET (GETO V KIND) A)) (SEV A (CAR L))) (PELIN (CAR L) (CDR L))))))
  A))
)

(DEFPROP TRIANG (LAMBDA (R)
  (COND ((AND (EQ 3 LENGTH (SETO % (SETO R KVERTICES))))
        (EQ 2 LENGTH (SETO % (HAVING (FUNCTION (LAMBDA (K) (EQ (QUOTE T) (CAR (SETO K TYPE)))))) %)))
        (OR (NOT (EQ R (CDR %))) (SETO % (REVERSE %)))
        (SUME (CAR %)) (EV)
        (SUME (CDR %)) (EV)
        (EQ (EV 1) R)
        (EQ (EV 1) R))
        (LIST R (CAR %) (CDR %; K))))
  A))
)

(DEFPROP TRIALINK (LAMBDA (L)
  (MAP (FUNCTION
    (LAMBDA (J)
      (COND ((OR (NULL A) (NULL (CDR A))))
            ((MEMBER (CAR A) (CDR A)) (REPLAC A (CDR A)))
            (A)))
    A))
  A))
)

```

*Remove repeated elements from its argument. Modify list structure.*

*Prints A without parentheses. No space before or after. No  $\backslash$ . The value of  $\backslash$  (normally  $\backslash$ ) is printed after each atom. The value of prec (normally  $\backslash$ ), in this case nothing gets printed) is printed before each atom. If A = (...set p q...) then p is printed as it is (with parentheses, etc) and without an space after it.*

*A is a nucleus (1:2) (ans 004) only one line only one face or region*

*L = (3 4 5 6 7) regions. links somebody specifically except the two lines to region TYPE*

*Look in R for another nucleus having the same link. Merge them Kill nucleus A*

*links somebody specifically except the two lines to region TYPE*

*and a is anything except 'T' otherwise.*

```
(MAP (FUNCTION  
  (LAMBDA (K)  
    (AND (PARALLELCAR J) (CADR J) (CADR (SETQ K (CAR K))) (CAR K))  
         (PARALLEL (CAR J) (CADDR J) (CADDR K) (CAR K))  
         (NOT (OPPOSITE (CADDR J) (CADDR K) (CAR J) (CADR J)))  
         (NOT (OPPOSITE (CADR J) (CADR K) (CAR J) (CADDR J)))  
         (LEV (CADDR J) (CADDR K)))  
    (COND (J (PROG2 () (SETQ J (CAR J))))))  
  )  
  L))  
EXPR)
```

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*default value for equals*  
 (SETO CERO 0.01) (SETO SJINTO 0.15) (SETO SHASE 2.0) (SETO COLTO 0.05)

*small arguments as here 5 times*  
 (DEFPROP TYPEGENERATOR (LAMBDA (N)

((LAMBDA (L KIND)

((LAMBDA (K)

(PUTPROP N

((LAMBDA (K1 K2 K3 K4)

((LAMBDA (K5 K6 K7 K8)

(COND ((EQL (SETO L (LENGTH KIND)) 4.)

(COND ((CROSSP N K2 N K4) (LIST (QUOTE L) (LIST K3 K1)))

(T (LIST (QUOTE L) (LIST K1 K3))))

((EQL 6.)

(COND ((MPARA N (CADR KIND) N (SLOP N (CADDR KIND)))

((MPARA N (CADR KIND) N (SLOP N (CADDR KIND)))

((MPARA N (CADDR KIND) N (SLOP N (CADDR KIND)))

((MPARA N (CADDR KIND) N (SLOP N (CADDR KIND)))

((MPARA N (CADDR KIND) N (SLOP N (CADDR KIND)))

((MPARA N (CADDR KIND) N (SLOP N (CADDR KIND)))

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((MPARA N (CADDR KIND) N (SLOP N (CADDR KIND)))

((MPARA N (CADDR KIND) N (SLOP N (CADDR KIND)))

((MPARA N (CADDR KIND) N (SLOP N (CADDR KIND)))

19



```

(DEFPROP EQUAL1 (LAMBDA L
  (LESSP (ABS (DIFFERENCE (ARG 1) (ARG 2)))) (COND ((EQL L 3) (ARG 3)) (T CER0))))
  (EXPR)
  (DEFPROP COLINEAL (LAMBDA L (PROG
    (N A D) (SET0 D 0.0)
    (SET0 A (ARG (SET0 N 1)))
    E
    (COND ((EQL N L) (RETURN (EQUAL1 (LENGTH A (ARG N)) D COLTO))))
    (SET0 D (+ D (LENGTH (ARG N) (ARG (SET0 N (ADD1 N))))))
    (GO E)))
  (EXPR)
  (DEFPROP CROSSP (LAMBDA (A B C D)
    (GREATERP (+ (CROSS A B C D)) 0.0))
  (EXPR)
  (DEFPROP LENGTH (LAMBDA (A B)
    (LAMBDA (S)
      (SORT (+ (PLUS (TIMES (SET0 S (DIFFERENCE (SET0 A XCOR) (SET0 B XCOR)))) S)
              (TIMES (SET0 S (DIFFERENCE (SET0 A YCOR) (SET0 B YCOR)))) S))))
    (S))
  (EXPR)
  (DEFPROP REMOVE (LAMBDA (E L)
    (COND ((NULL L) L)
          ((EQUAL (CAR L) E) (CDR L))
          (T (CONS (CAR L) (REMOVE E (CDR L))))))
  (EXPR)
  (DEFPROP THROW (LAMBDA (K)
    (PROG (A)
      (COND ((AND (NULL Z) (LESSP (LENGTH (CAR K) (CADR K)) (SHASE))) (SET0 W (CONS V W)) (GO E)))
      (SET0 A (TES))
      (COND ((NULL A) (SET0 TES (CONS (LIST (LIST (CAR K) (CADR K)) (SET0 S (GENSYM)))) TES))
            (CPROP S S K (QUOTE PAS))
            (GO E))
      (MPARA (CAR K) (CADR K) (CAAR A) (CADAAR A)) (CPROP (CADR A) K (QUOTE PAS)) (GO E)))
    (SET0 A (CDR A))
    (GO B)
    (RETURN ())))
  (EXPR)
  (DEFPROP CLEAN (LAMBDA (/-SAPAS)
    (MAPC (FUNCTION (LAMBDA (K) (MAPC (FUNCTION (LAMBDA (J) (REMPROP K J)))
      (CDR /-SAPAS)))) (EVAL (CAR /-SAPAS))))
  (EXPR)
  (DEFPROP SEV (LAMBDA (A B)
    (OR (EQL A B)
        (SET0 A BACKGROUND)
        (SET0 B BACKGROUND)
        ((LAMBDA (S) (AND (CPROP 'A S (QUOTE BODY)) (CPROP B S (QUOTE BODY))))
         (GENSYM))))
  (EXPR)
  (SET0 SPR ()))

```

*(equals x y e) = T if |x-y| < e, () otherwise. (equals xy) = (equals x y expr) variable*  
*(colineal a b c d e) = T if all three vectors are colinear*  
*(cross a b c d) vectors. True if the cross-product is (+)  $\frac{a \cdot b \cdot c}{d}$*   
*(length a-b) length of a-b. always (+)*  
*(remove e l) = l without the first occurrence of element e  
E may be any Lisp expression.  
New Garval.*  
*k = atom value of throw is () always.  
Pick k in TES*  
*(clean b a, a, ..., a) b is evaluated (assumed a list) a, ..., a are not evaluated (quantity above). (number b<sub>1</sub>)*  
*puts a global witness between a and b  
except if a=b*  
*flashes all of this.*



True if

```
(DEFPROP PROPERARROW (LAMBDA (R V)
  (COND ((EQ (PROG2 (SUME V EG) (EG D)) (QUOTE ARROW)))
        (NOT (EQ R (EG 7))))))
EXPR)
```

```
(DEFPROP SINGLET (LAMBDA (L) (AND L (NULL (CUR L)))) EXPR)
```

```
(DEFPROP OBTU (LAMBDA (A B C) (COND
  ((LESS (DOT A N C N) D 0) (SETU B B B) A)
  (T (SETU B A) B))) EXPR)
```

```
ISETO FE (QUOTE /
```

Value is one of A or B, the one having an obtuse angle with the NC  
The other one (the point) is stored in ::



← Form feed.

23 DICIEMBRE 1968

Atlefo Guzmán Arenas

(23)



#### BIOGRAPHICAL NOTE

Adolfo Guzmán Arenas was born in Ixtaltepec, Oax., México on July 22, 1943. He entered the Escuela Superior de Ingeniería Mecánica y Eléctrica (ESIME) of the Instituto Politécnico Nacional in 1961 and, after defending the thesis "CONVERT - Design of a language for symbolic manipulation of data and of its corresponding processor", received from them the degree "Communications and Electronics Engineer" in 1965. During all his stay in the ESIME, he was receiving a scholarship from the Politécnico. He is a Registered Engineer (I. C. E.), according to Mexican law .

During 1964 (his last year in college) he held a part time programming job at the Computing Center of the Politécnico; he was sent to University of Florida (Gainesville), Stanford University (Cal.) and System Development Co. (Cal.) to learn different computing systems and languages. The first half of 1965 was spent at the Physics Department of the Centro de Investigación y Estudios Avanzados of the Politécnico, as a "technical assistant."

For his graduate studies, Adolfo Guzmán entered the Electrical Engineering Department of the Massachusetts Institute of Technology in September 1965, becoming also a member (research assistant) of the Project MAC staff, a computer-oriented inter-departmental laboratory, and became associated with the Artificial Intelligence Group of M. I. T.

After completing a thesis "Some Aspects of Pattern Recognition by Computer" he was awarded the degree of Master of Science in Electrical Engineering in 1967.

He has accepted a position as an Assistant Professor in the Department of Electrical Engineering at M.I.T. beginning February 1969. Within his research interests are computer applications and problem solving, man-machine interaction, heuristic programming and graphical information processing, the latter being the subjects of his doctoral dissertation.

He is a member of the Association for Computing Machinery and the Institute of Electrical and Electronic Engineers.

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13. ABSTRACT Methods are presented: 1) to partition or decompose a visual scene into the bodies forming it; 2) to position these bodies in three-dimensional space, by combining two scenes that make a stereoscopic pair; 3) to find the regions or zones of a visual scene that belong to its background; 4) to carry out the isolation of objects in 1) when the input has inaccuracies. Running computer programs implement the methods, and many examples illustrate their behavior. The input is a two-dimensional line-drawing of the scene, assumed to contain three-dimensional bodies possessing flat faces (polyhedra); some of them may be partially occluded. Suggestions are made for extending the work to curved objects. Some comparisons are made with human visual perception.  The main conclusion is that it is possible to separate a picture or scene into the constituent objects exclusively in basis of monocular geometric properties (in basis of pure form); in fact, successful methods are shown.		
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